

## 20e. Computations for Lemma 4.15

```
In[ = ]:= Clear[kp, s, eps]
muups = (1/2 + kp + s ≤ 0)
muom = (1/2 - kp + s ≤ 0)

Out[ = ]=  $\frac{1}{2} + kp + s \leq 0$ 

Out[ = ]=  $\frac{1}{2} - kp + s \leq 0$ 
```

### Part i)

$\varepsilon = 1$

```
In[ = ]:= muups /. s → nu/2 /. kp → -Max[p, mθ[j]] - (j + 1)/2 // Simplify
Out[ = ]= nu ≤ j + 2 Max[p, mθ[j]]
```

$\varepsilon = -1$

```
In[ = ]:= muups /. s → nu/2 /. kp → -mθ[j] - (-j + 1)/2 // Simplify
Out[ = ]= j + nu ≤ 2 mθ[j]
```

### Part ii)

$\varepsilon = 1$

```
In[ = ]:= muups /. s → nu/2 /. kp → -mθ[j] - (j + 1)/2 // Simplify
Out[ = ]= nu ≤ j + 2 mθ[j]
```

$\varepsilon = -1$

```
In[ = ]:= muups /. s → nu/2 /. kp → -Max[mθ[j], p] - (-j + 1)/2 // Simplify
Out[ = ]= j + nu ≤ 2 Max[p, mθ[j]]
```

### Part iii)

$\varepsilon = 1$

```
In[ = ]:= muom /. s → nu/2 /. kp → -Max[mθ[j], p] - (j + 1)/2 // Simplify
Out[ = ]= 2 + j + nu + 2 Max[p, mθ[j]] ≤ 0
```

$\varepsilon = -1$

```
In[ = ]:= muom /. s → nu/2 /. kp → -mθ[j] - (-j + 1)/2 // Simplify
Out[ = ]= 2 + nu + 2 mθ[j] ≤ j
```

## Part iv)

$\varepsilon = 1$

In[ 0]:= muom /. s → nu / 2 /. kp → -mθ[j] - (j + 1) / 2 // Simplify

Out[ 0]= 2 + j + nu + 2 mθ[j] ≤ 0

$\varepsilon = -1$

In[ 0]:= muom /. s → nu / 2 /. kp → -Max[mθ[j], p] - (-j + 1) / 2 // Simplify

Out[ 0]= 2 + nu + 2 Max[p, mθ[j]] ≤ j