

3f. Casimir element of K_0

See (2.34)

Definition

```
In[ * ]:= CasK = WW0 ** WW0 + WW1 ** WW1 + WW2 ** WW2
CasKZ = CasK /. XWtoZsub // Simplify
```

```
Out[ * ]= WW0 ** WW0 + WW1 ** WW1 + WW2 ** WW2
```

```
Out[ * ]= -2 i WW0 + WW0 ** WW0 + Z12 ** Z21
```

Is it central?

```
In[ * ]:= CasKZ ** WW0 - WW0 ** CasKZ
CasKZ ** Z12 - Z12 ** CasKZ // Expand
CasKZ ** Z21 - Z21 ** CasKZ // Expand
CasKZ ** CKi - CKi ** CasKZ /. nul -> 0 // Expand
```

```
Out[ * ]= 0
```

```
Out[ * ]= 0
```

```
Out[ * ]= 0
```

```
Out[ * ]= 0
```

In the next checks we use the routines defined later on (carried out in initialization)

```
In[ * ]:= Clear[h, p, r, q]
eR[CasK, Phi[h, p, r, q], subtriv]
eR[CasKZ, Phi[h, p, r, q], subtriv]
```

```
Out[ * ]= -p (2 + p) Phi[h, p, r, q]
```

```
Out[ * ]= -p (2 + p) Phi[h, p, r, q]
```

```
In[ * ]:= eR[CKi, Phi[h, p, r, q], subtriv]
```

```
Out[ * ]= -i h Phi[h, p, r, q]
```

```
In[ * ]:= eR[WW0, Phi[h, p, r, q], subtriv]
```

```
Out[ * ]= -i q Phi[h, p, r, q]
```