

## Group theory – Hand in sheet 1

Let  $G$  be group. An element  $g \in G$  satisfies  $g^2 = e$  precisely when  $g = g^{-1}$ . Show that if  $G$  is finite and contains an even number of elements, then the number of nonidentity elements which satisfy  $g^2 = e$  is odd.