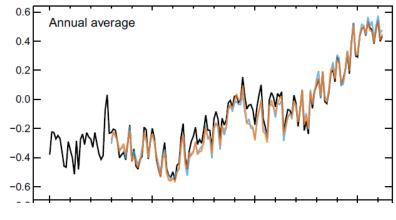
Implications of Variability for Economic Assessments of Climate Change: Physical Stochasticity in Integrated Assessment Models

David Stainforth, London School of Economics

In collaboration with: Raphael Calel, Georgetown University Nick Watkins, Warwick University and LSE Sandra Chapman, Warwick University

Workshop on Climate and the Economy, Soesterberg, 16 July 2019



IPCC, WG1, SPM, Fig 1.













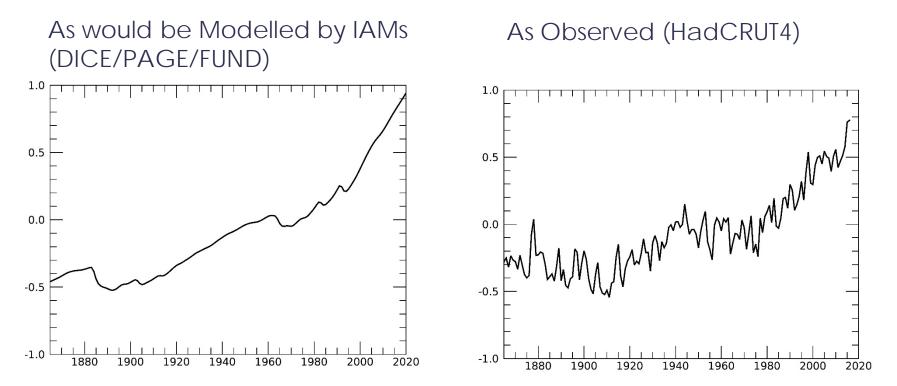
THE LONDON SCHOOL OF ECONOMICS AND POLITICAL SCIENCE

Warnings

- Work in progress
- I'm presenting

The Starting Point

Historic Global Mean Temperature Anomalies

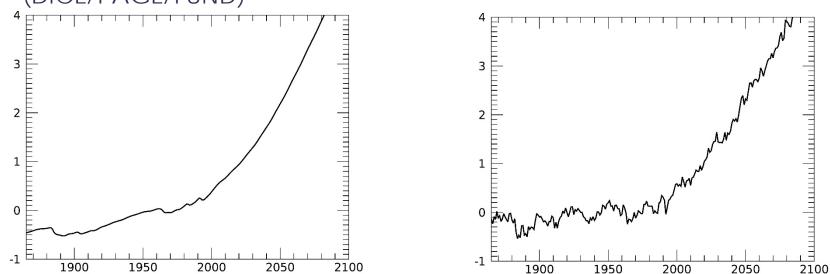


The Starting Point

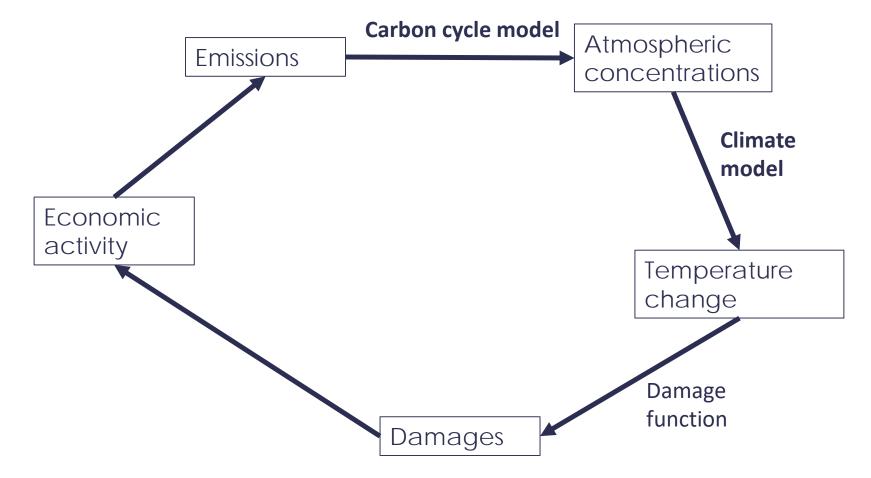
Historic And Future Global Mean Temperature Anomalies

As would be Modelled by IAMs (DICE/PAGE/FUND)

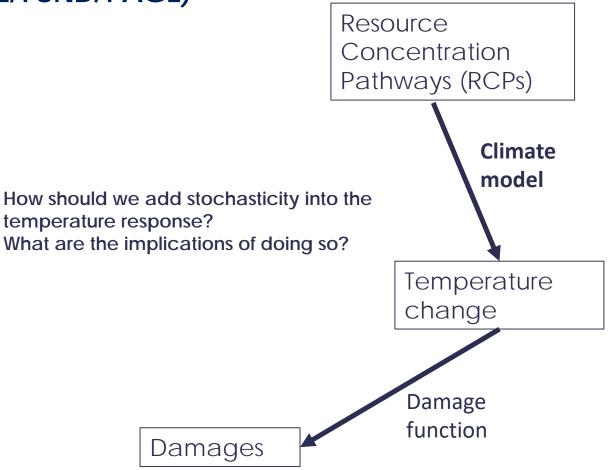
Example CMIP5 simulation



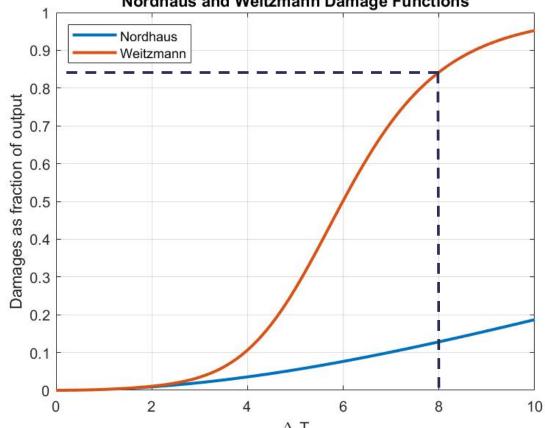
Simple IAMs (DICE/FUND/PAGE)



Simple IAMs (DICE/FUND/PAGE)

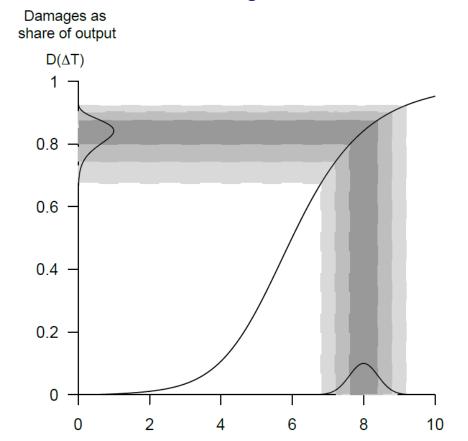


Damage Functions



Nordhaus and Weitzmann Damage Functions

Damage Functions and Uncertainty in ΔT

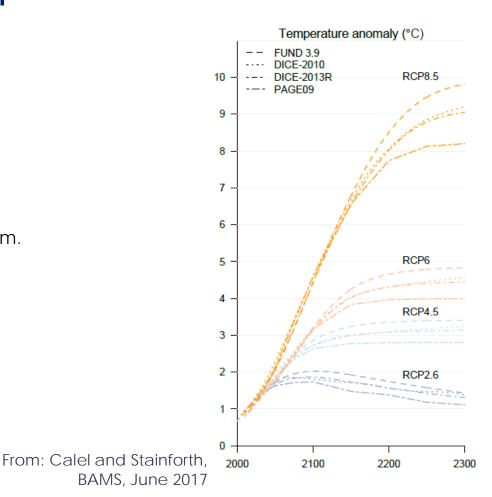


 ΔT

A simple energy balance model

$$C_{eff} \frac{d\Delta T}{dt} = F(t) - \lambda \,\Delta T$$

- ΔT : Change in global mean temperature
- F: Radiative forcing by comparison to ~ 1750
- C_{eff}:Effective heat capacity of the climate system.
- λ: Feedback parameter



See, for instance: Andrews and Allen 2008; Senior and Mitchell 2000; Dickinson 1986

A simple stochastic energy balance model

$$C_{eff}d\Delta T = F(t)dt - \lambda \Delta T dt + \sigma_Q dW_t$$

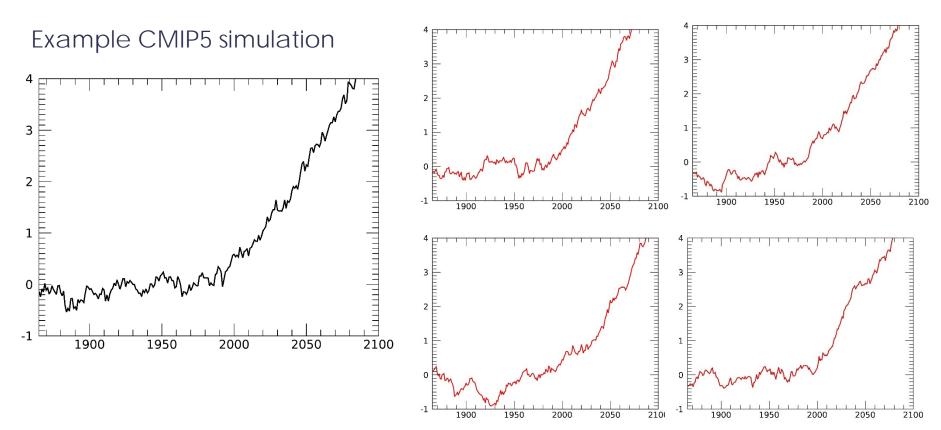
or equivalently

$$C_{eff}d\Delta T = F(t)dt - \lambda \Delta T dt + \sqrt{\sigma_Q^2 dt} N_t^{t+dt}(0,1)$$

- ΔT : Change in global mean temperature
- F: Radiative forcing by comparison to ~ 1750
- C_{eff}:Effective heat capacity of the climate system.
- λ: Feedback parameter

More realistic simulations?

Hasselmann model trajectories

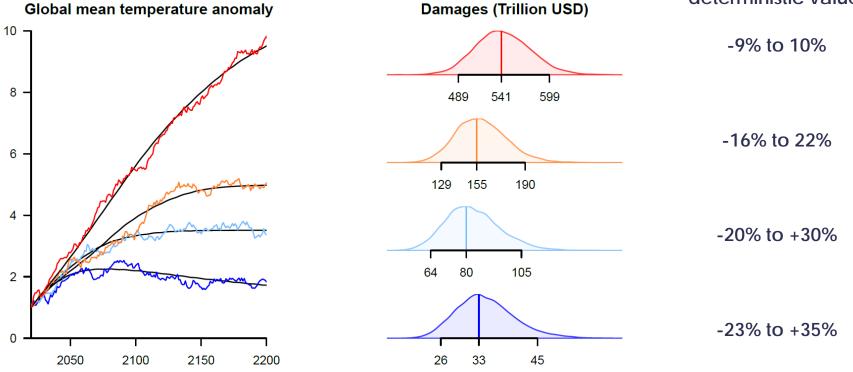


The economic and simulation assumptions

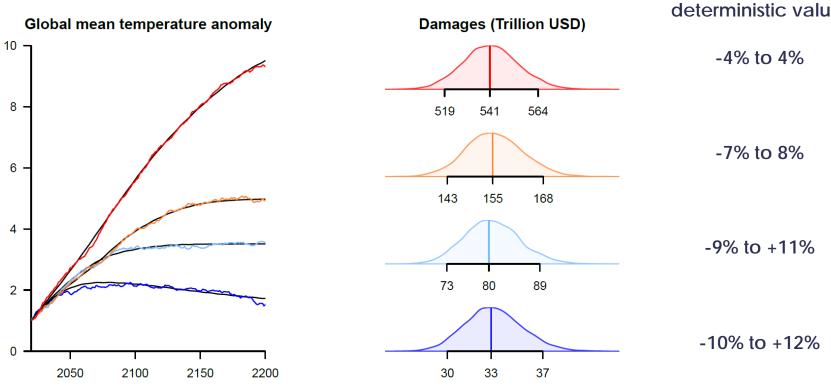
- Start date of simulations: 2020
- Initial per capita consumption: \$10,666 (Aggregate consumption: \$80 Trillion)
- Initial population: 7.5B
- Growth rate: 2%/yr
- Pure rate of time preference: 4.4%
- Linear utility function
- Population growth as in DICE 2016.
- Damage function: Weitzman
- Size of trajectory ensembles: 8000
- Fixed lambda = 1.2 Wm⁻²K⁻¹
- Fixed $C_{eff} = 0.8E9 Jm^{-2}K^{-1}$

Economic Consequences

5-95% range as a fraction of the deterministic value:

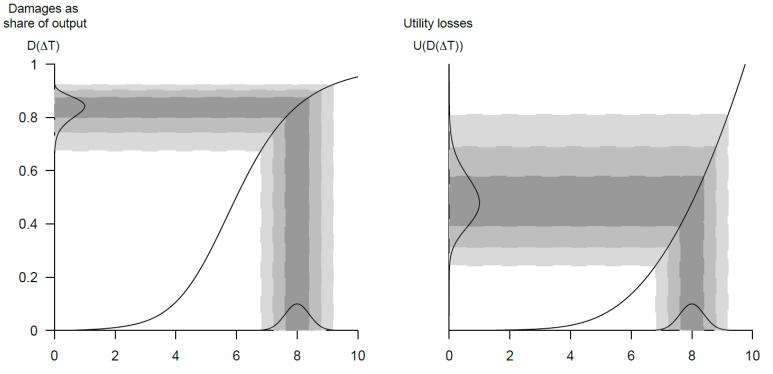


With smaller variability



5-95% range as a fraction of the deterministic value:

Expected Utility

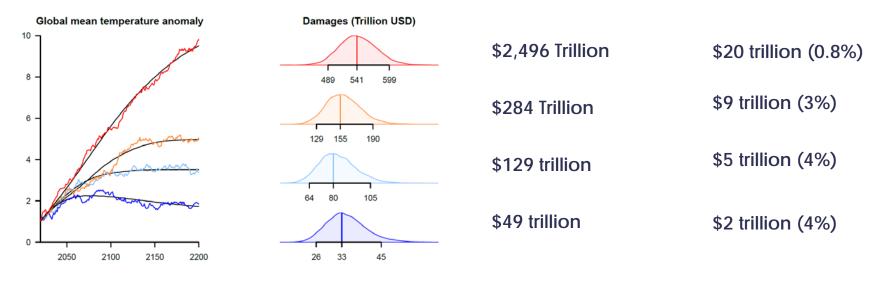


 ΔT

Expected Utility

Change in total utilityadjusted dollar value of consumption under deterministic trajectory.

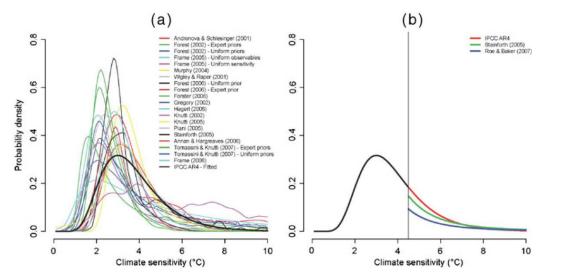
Additional change due to stochasticity (fractional additional change w.r.t. deterministic case)



$$U = \frac{\left(C * D(\Delta T)\right)^{1-\eta} - 1}{1-\eta}$$

η= 1.45, ρ = 1.5Discount rate, r, = 4.4%

Does physical uncertainty matter?



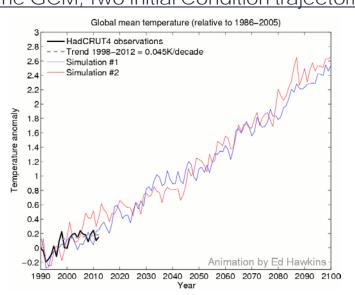
"Tall Tales and Fat Tails", Calel, Stainforth and Dietz, Climatic Change, 2013

 Table 2
 Value of 500 ppm policy with varying effective heat capacity

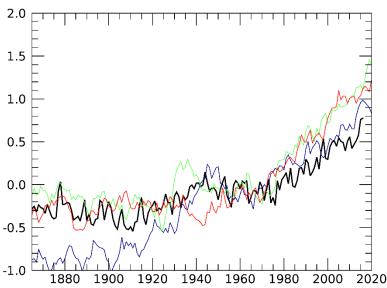
Climate sensitivity	Increase in stationary equivalent (%)		
distribution	$0.6 \text{ GJm}^{-2}\text{K}^{-1}$	$1.2 \text{ GJm}^{-2}\text{K}^{-1}$	$1.8 \mathrm{GJm}^{-2}\mathrm{K}^{-1}$
IPCC AR4	1.26	0.80	0.47
Stainforth et al. (2005)	49.63×10^{3}	19.96×10^{2}	0.75
Roe and Baker (2007)	75.74×10^{5}	43.88×10^{4}	76.70

Fitting Observations

 We want models that can reproduce the past but a "bad" match with past observations for individual simulations isn't necessarily indicative of a bad model.
 Do we have sample sizes to evaluate properly?



One GCM, Two Initial Condition trajectories

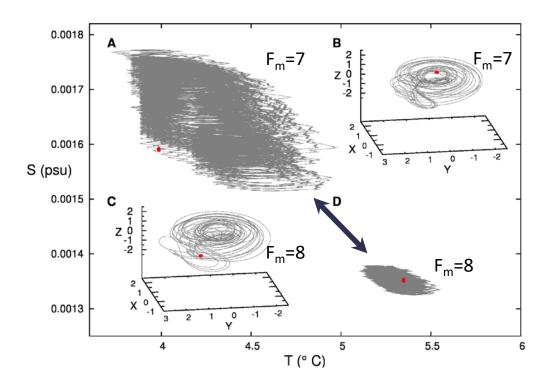


Hasselmann model trajectories

Plot from Ed Hawkins, Reading University

The Essence of Predicting Climate and Predicting the Consequences of Climate Change

- Extrapolation to a new, previously unobserved state of the system.
- 21st century climate to some extent parallels the quantification of the transient behaviour as we move from one attractor to another.



Daron and Stainforth, Env.Res.Lett., 2013