

Lecture 2: Single and di-hadron measurements and energy loss modelling

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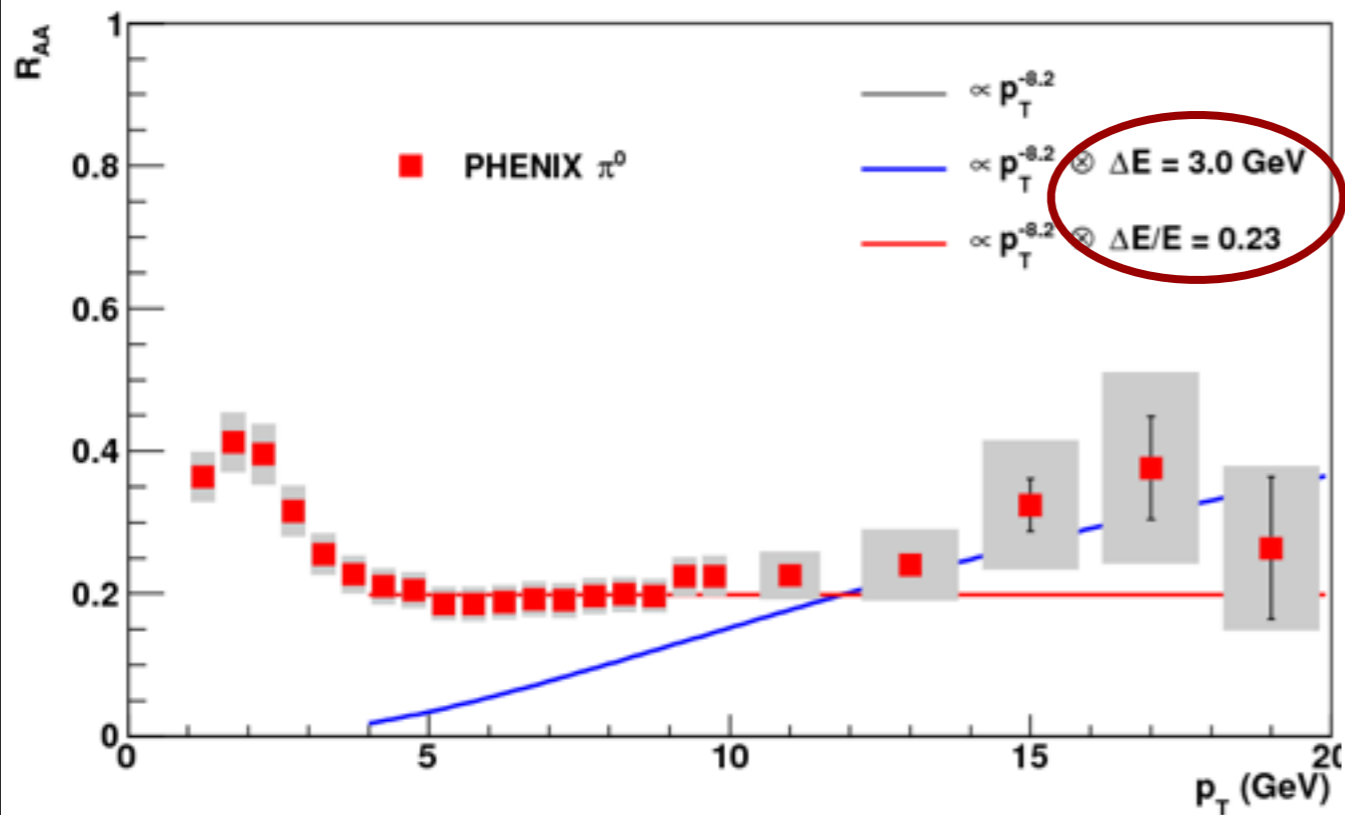


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From RHIC to LHC

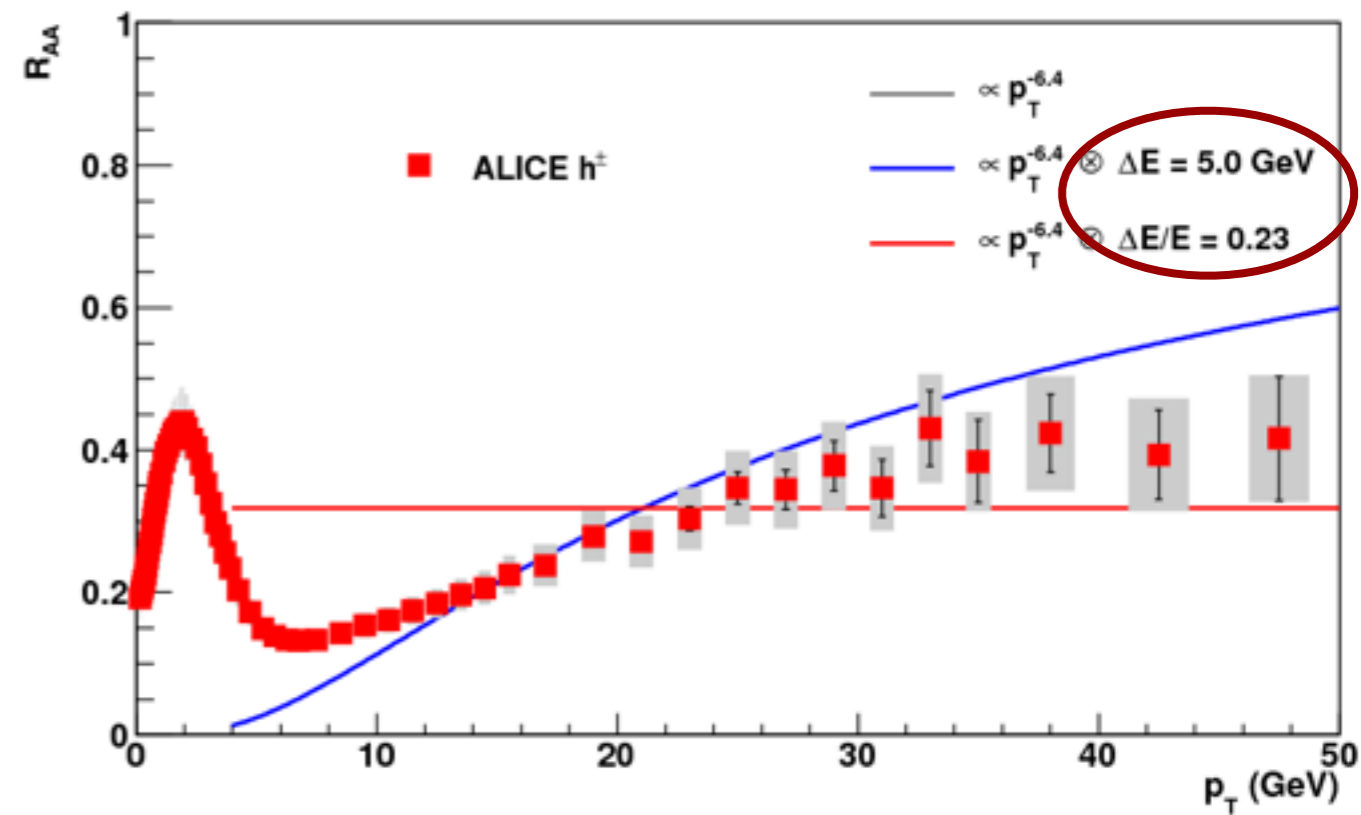
RHIC



RHIC: $n \sim 8.2$

$$(1 - 0.23)^{6.2} = 0.20$$

LHC



LHC: $n \sim 6.4$

$$(1 - 0.23)^{4.4} = 0.32$$

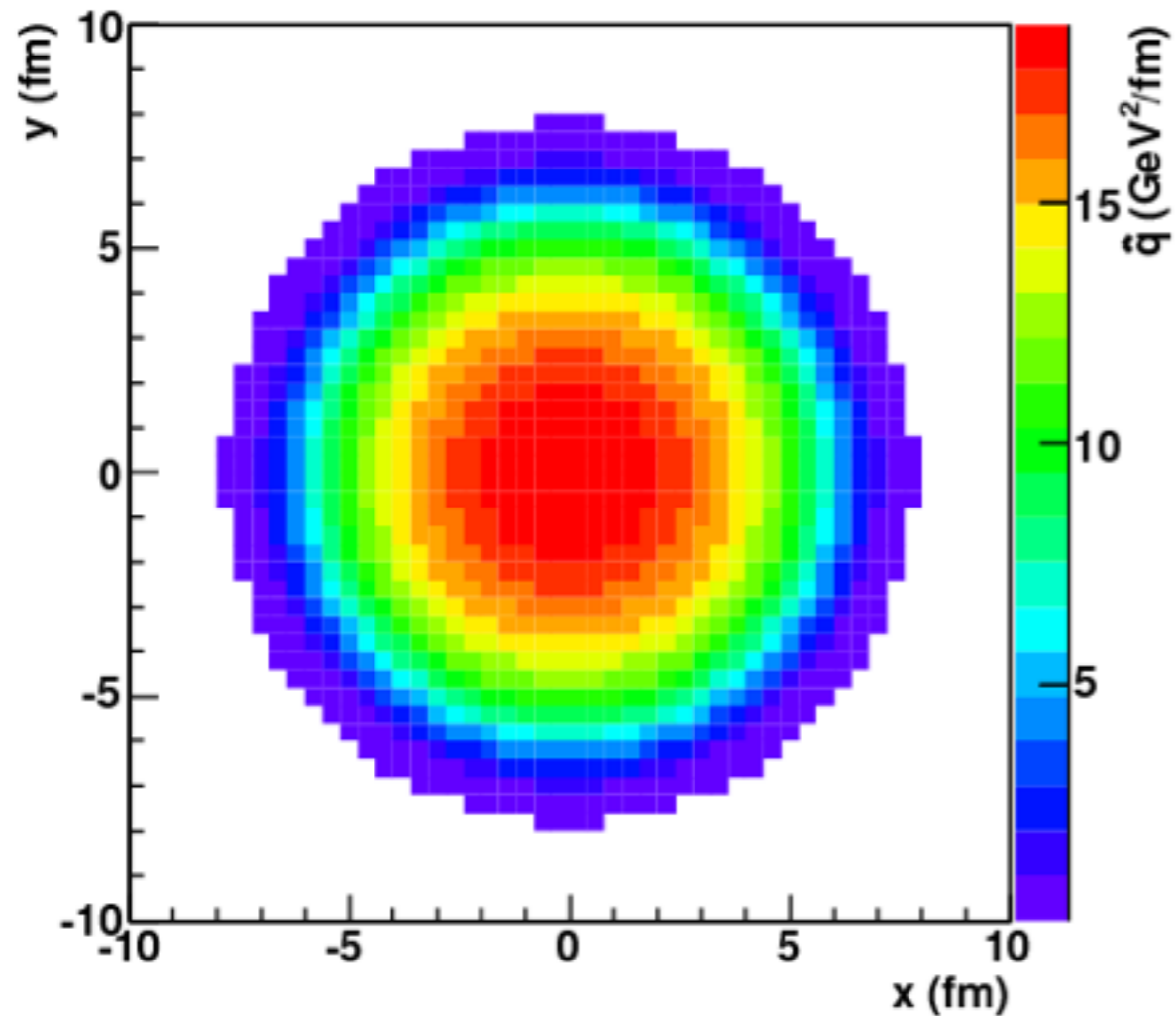
Remember: still 'getting a sense for the numbers'; this is not a model!

Towards a more complete picture

- Energy loss not single-valued, but a distribution
- Geometry: density profile; path length distribution
- Energy loss is partonic, not hadronic
 - Full modeling: medium modified shower
 - Simple ansatz for leading hadrons: energy loss followed by fragmentation
 - Quark/gluon differences

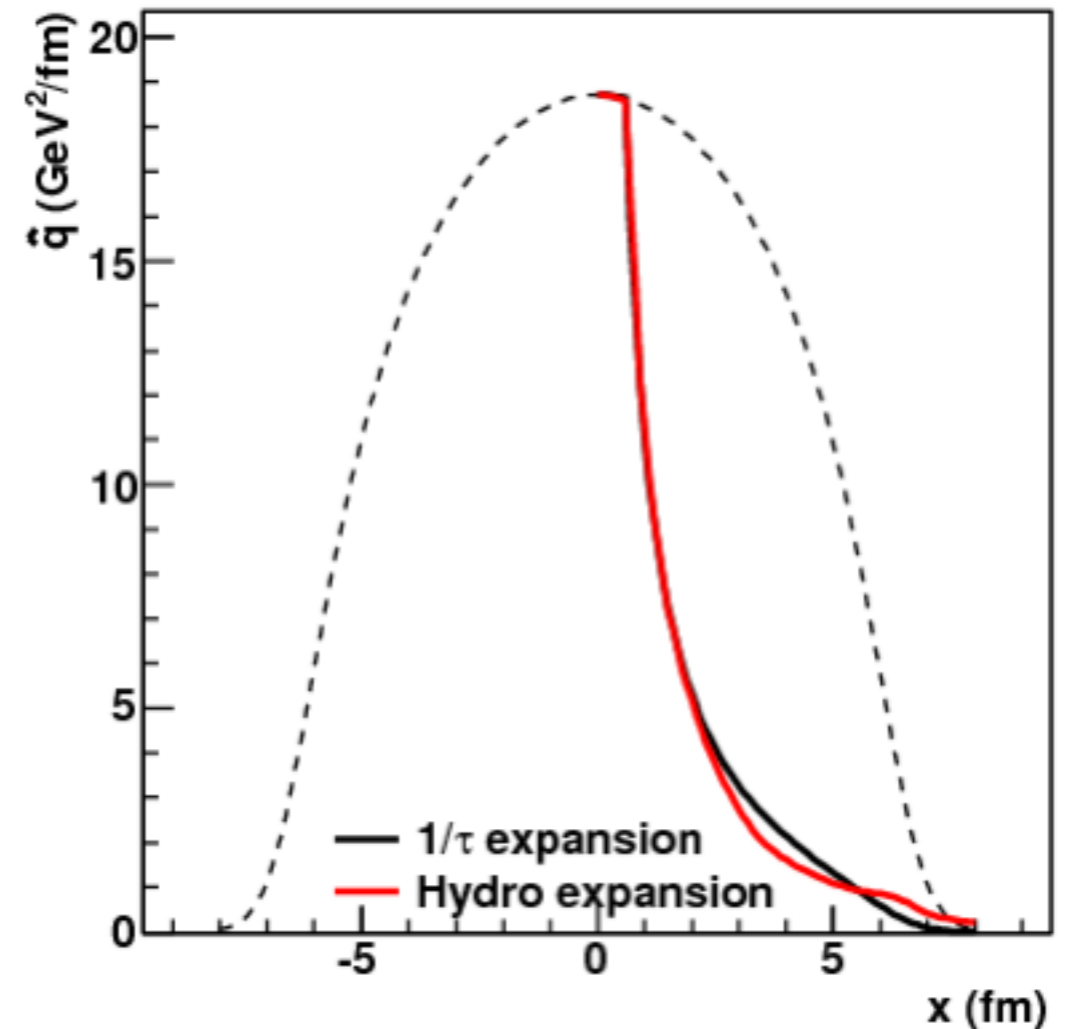
Geometry

Density profile



Profile at $\tau \sim \tau_{\text{form}}$ known

Density along parton path



Longitudinal expansion
dilutes medium
⇒ Important effect

Space-time evolution is taken into account in modeling

A simplified approach

$$\frac{dN}{dp_T} \Big|_{hadr} = \left(\frac{dN}{dE} \Big|_{jets} \right) \otimes P(\Delta E) \otimes D(p_{T,hadr} / E_{jet})$$

Parton spectrum Energy loss distribution Fragmentation (function)

known pQCDxPDF extract 'known' from e⁺e⁻

This is where the information about the medium is

$P(\Delta E)$ combines geometry
with the intrinsic process

– Unavoidable for many observables

Notes:

- This is the simplest ansatz – most calculation to date use it (except some MCs)
- Jet, γ -jet measurements 'fix' E , removing one of the convolutions

Situation at RHIC, ca 2008

3 main calculations; comparison with same medium density profile

ASW: $\hat{q} = 10 - 20 \text{ GeV}^2/\text{fm}$

HT: $\hat{q} = 2.3 - 4.5 \text{ GeV}^2/\text{fm}$

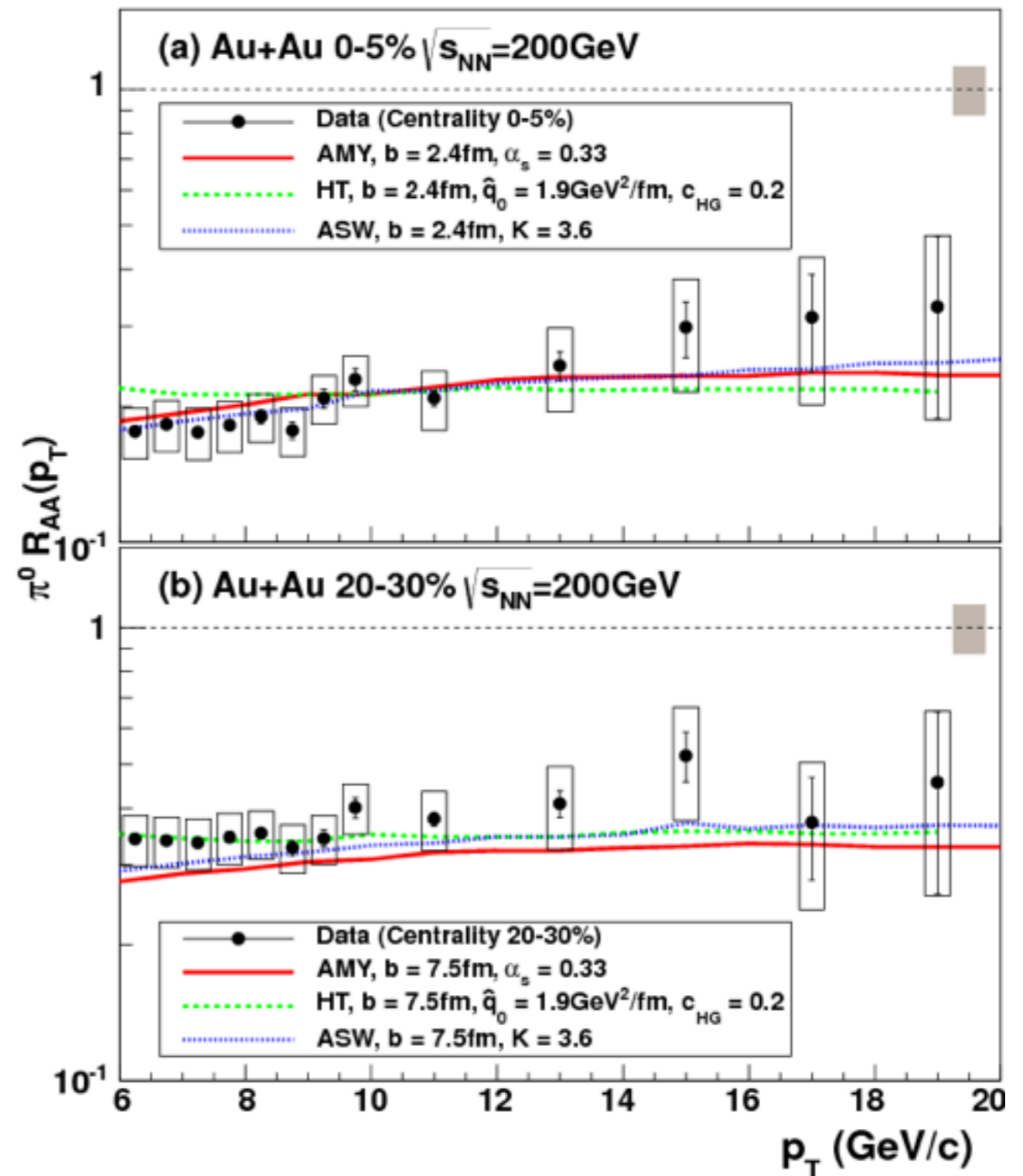
AMY: $\hat{q} \approx 4 \text{ GeV}^2/\text{fm}$

Large density:

AMY: $T \sim 400 \text{ MeV}$

Transverse kick: $qL \sim 10\text{-}20 \text{ GeV}$

Large uncertainty in absolute medium density



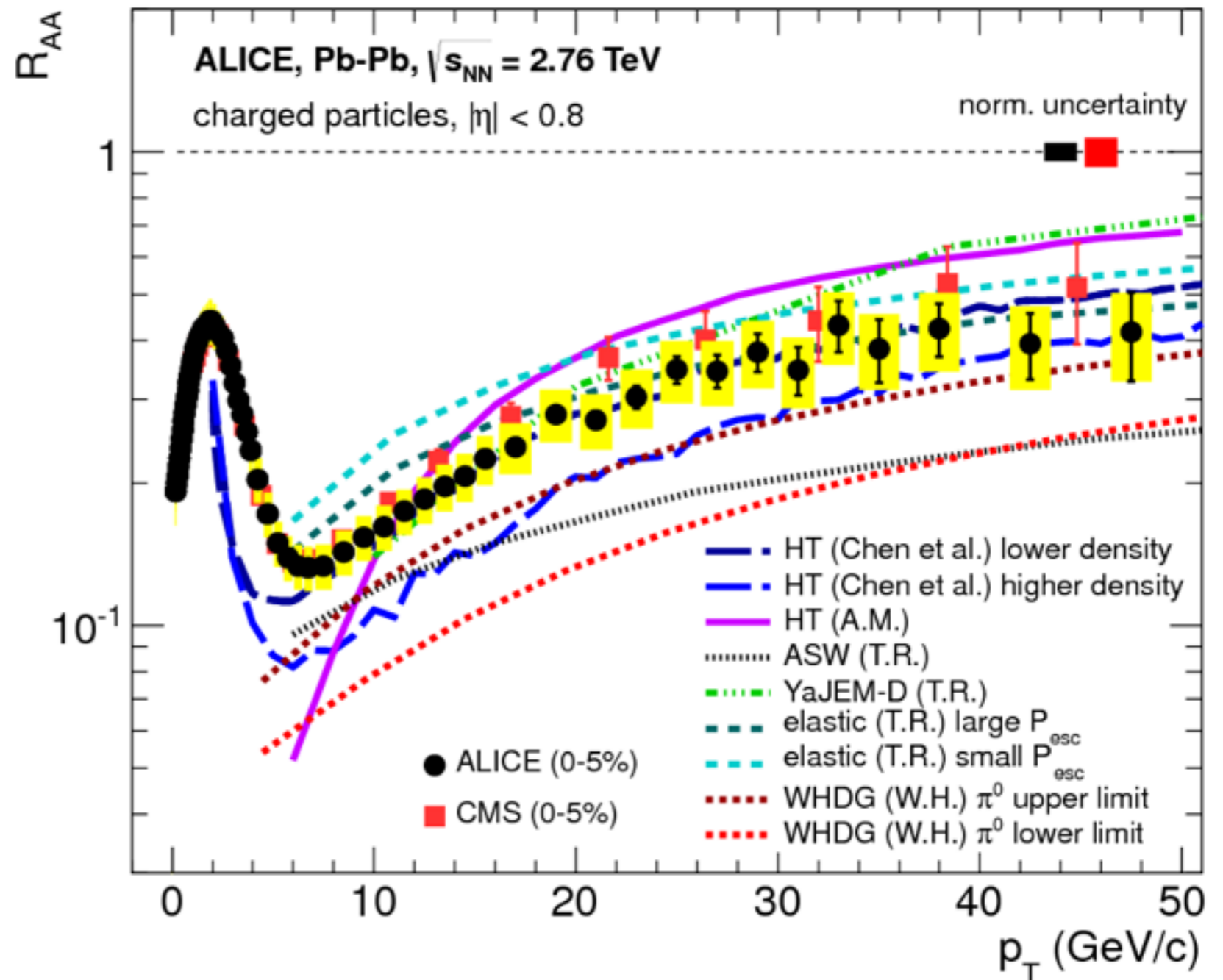
R_{AA} at LHC & models

ALICE: arXiv:1208.2711

CMS: arXiv:1202.2554

Broad agreement
between models and
LHC R_{AA}

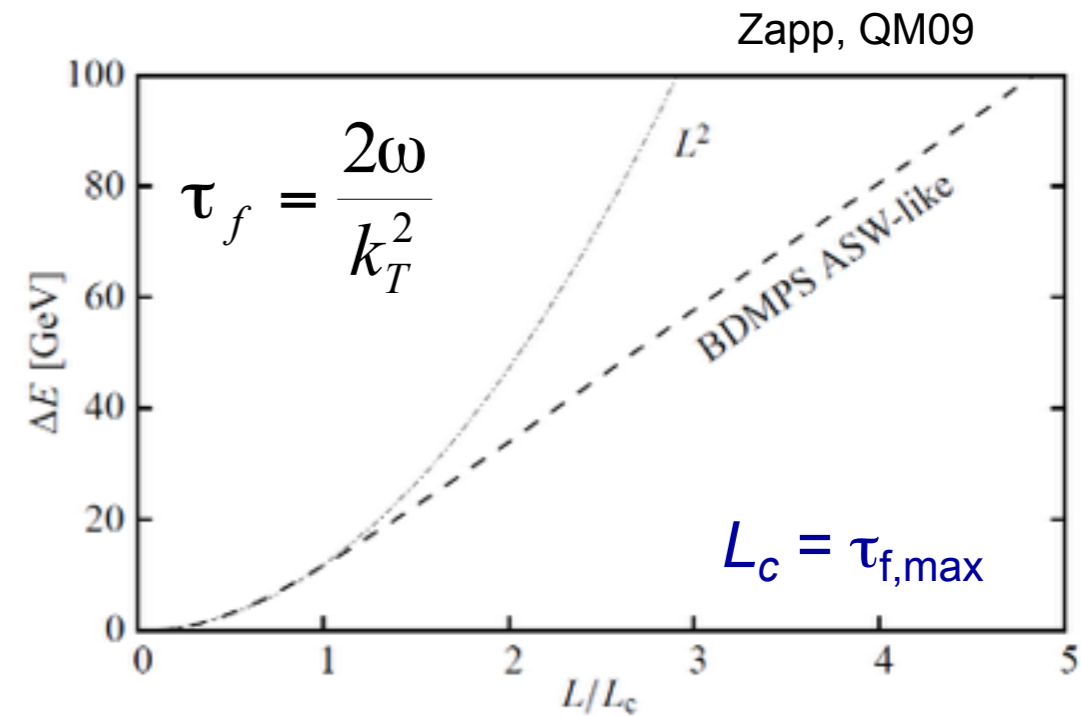
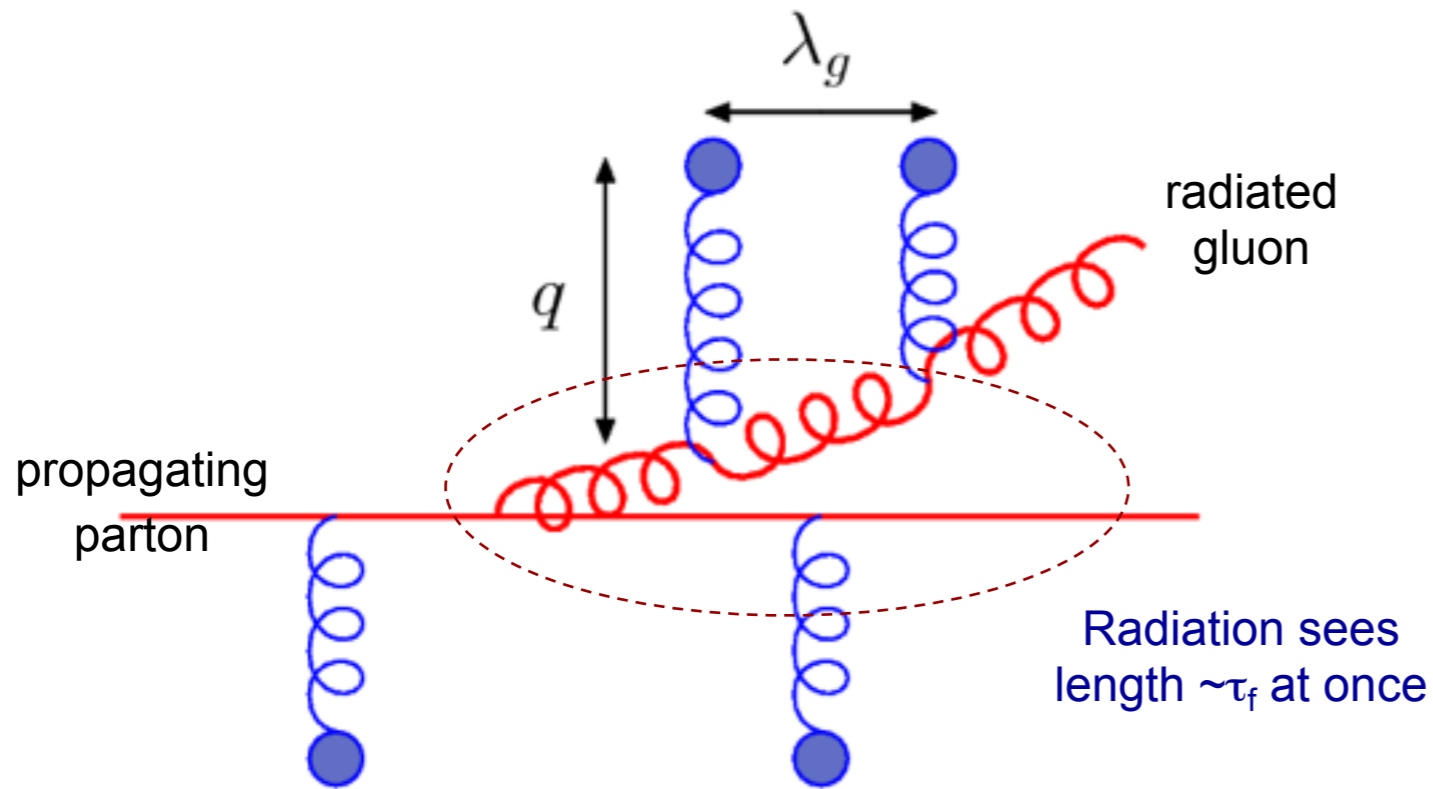
Extrapolation from RHIC
tends to give too much
suppression at LHC



Many model curves: need more constraints and/or selection of models

Medium-induced radiation

Landau-Pomeranchuk-Migdal effect
Formation time important



Energy loss depends on density: $\lambda \propto \frac{1}{\rho}$

and nature of scattering centers
(scattering cross section)

Transport coefficient $\hat{q} \equiv \frac{\langle q_{\perp}^2 \rangle}{\lambda}$

If $\lambda < \tau_f$, multiple scatterings
add coherently

$$\Delta E_{med} \sim \alpha_s \hat{q} L^2$$

Four formalisms

Multiple gluon emission

- **Hard Thermal Loops (AMY)**
 - Dynamical (HTL) medium
 - Single gluon spectrum: BDMPS-Z like path integral
 - No vacuum radiation
- **Multiple soft scattering (BDMPS-Z, ASW-MS)**
 - Static scattering centers
 - Gaussian approximation for momentum kicks
 - Full LPM interference and vacuum radiation
- **Opacity expansion ((D)GLV, ASW-SH)**
 - Static scattering centers, Yukawa potential
 - Expansion in opacity L/λ
($N=1$, interference between two centers default)
 - Interference with vacuum radiation
- **Higher Twist (Guo, Wang, Majumder)**
 - Medium characterised by higher twist matrix elements
 - Radiation kernel similar to GLV
 - Vacuum radiation in DGLAP evolution

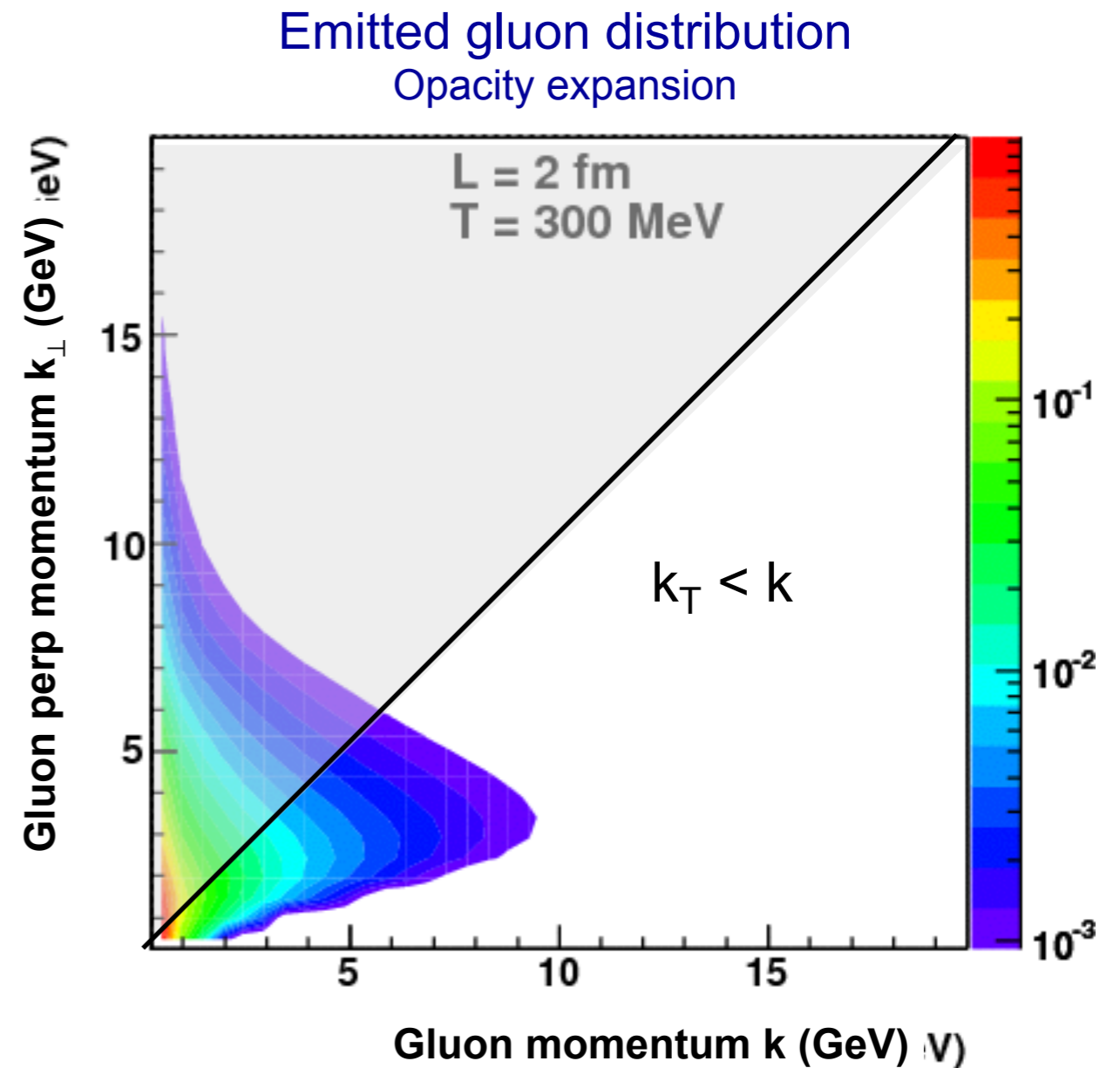
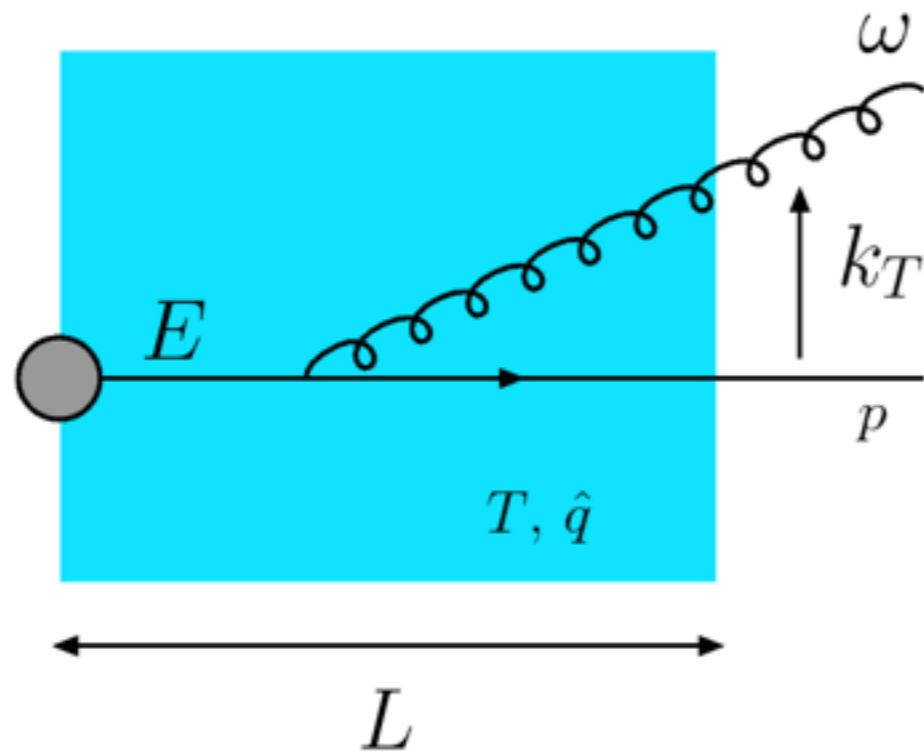
Fokker-Planck
rate equations

Poisson ansatz
(independent emission)

DGLAP
evolution

See also: arXiv:1106.1106

Large angle radiation



Calculated gluon spectrum extends to large k_{\perp} at small k
Outside kinematic limits

GLV, ASW, HT cut this off 'by hand'

Effect of large angle radiation

Opacity expansion formalisms

Expand in powers of $\frac{L}{\lambda}$

Different definitions of x :

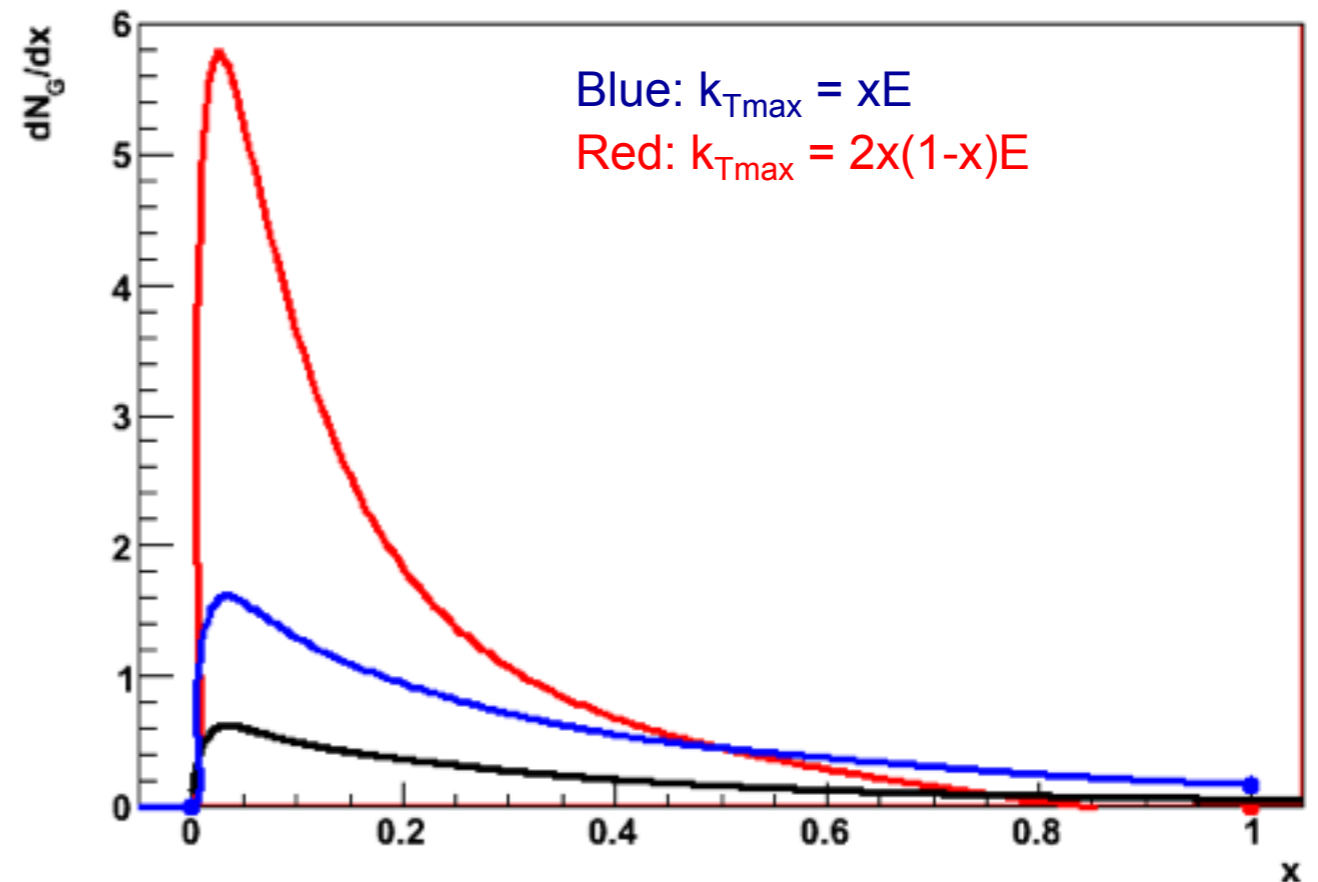
ASW: $x_E = \frac{\omega}{E}$ GLV: $x_+ = \frac{\omega_+}{E_+}$

Different large angle cut-offs:

$k_T < \omega = x_E E$

$k_T < \omega = 2 x_+ E$

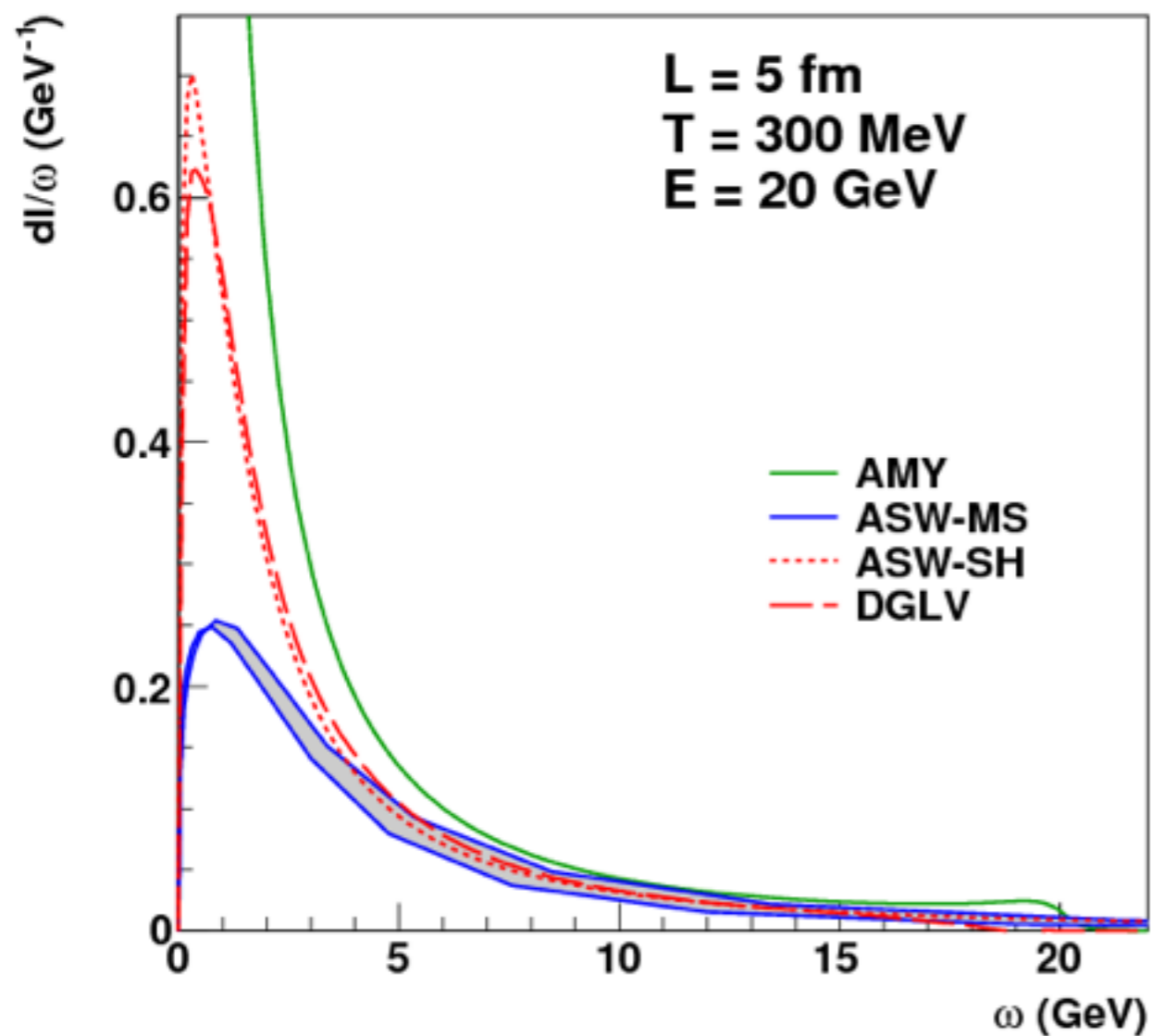
Single-gluon spectrum



Factor ~2 uncertainty
from large-angle cut-off

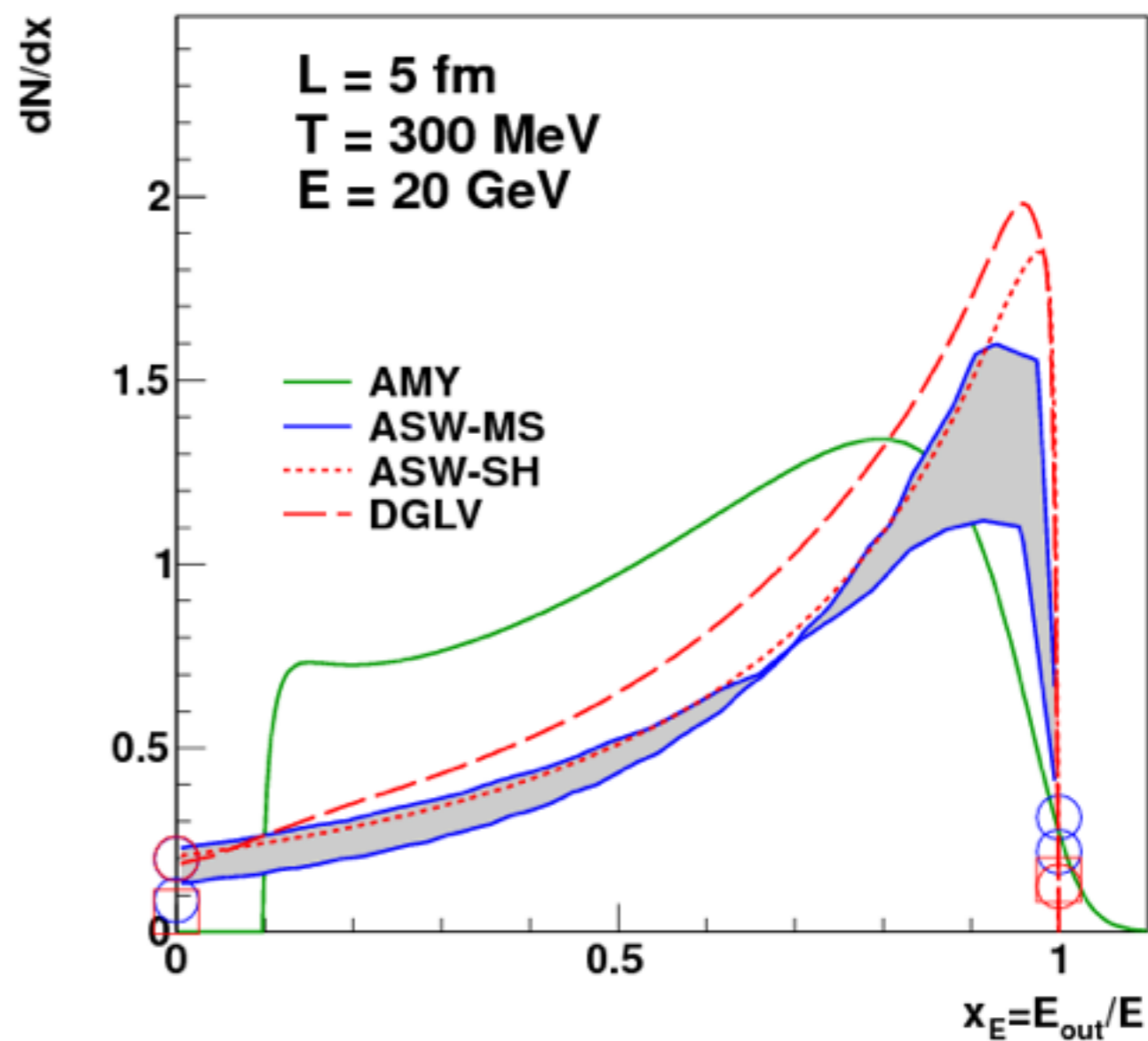
Energy loss distributions

Radiated gluon distribution



Main theory uncertainty:
Large angle radiation

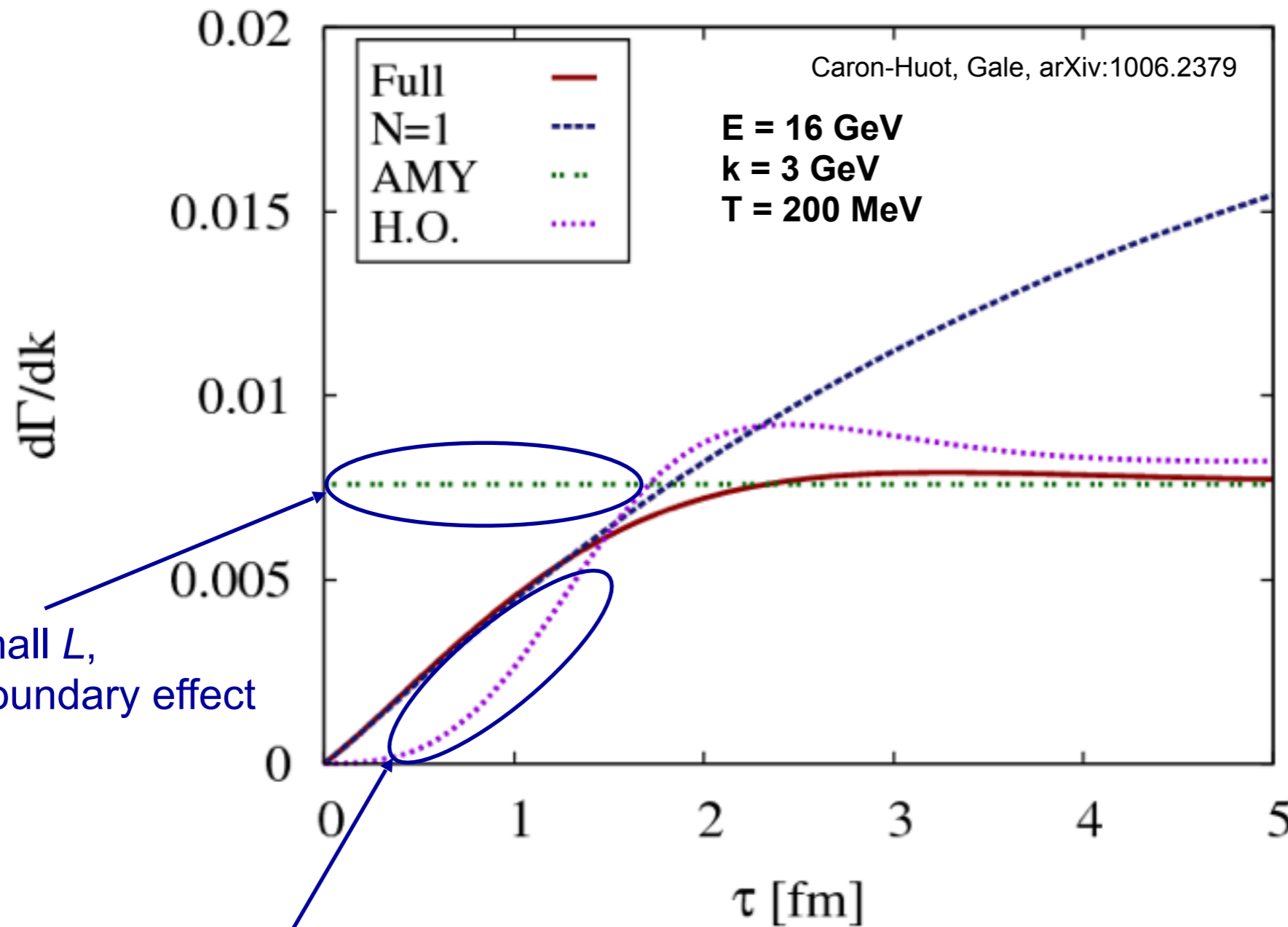
Energy loss probability distribution



Broad distribution
Significant contributions at $\Delta E=0$, $\Delta E=E$

L -dependence; regions of validity?

Emission rate vs τ ($=L$)



GLV $N=1$
 Too much radiation
 at large L
 (no interference
 between scatt centers)

Full =
 numerical solution of
 Zakharov path integral
 = 'best we know'

AMY, small L ,
 no L^2 , boundary effect

H.O. = ASW/BDMPS like (harmonic oscillator)
 Too little radiation at small L
 (ignores 'hard tail' of scatt potential)

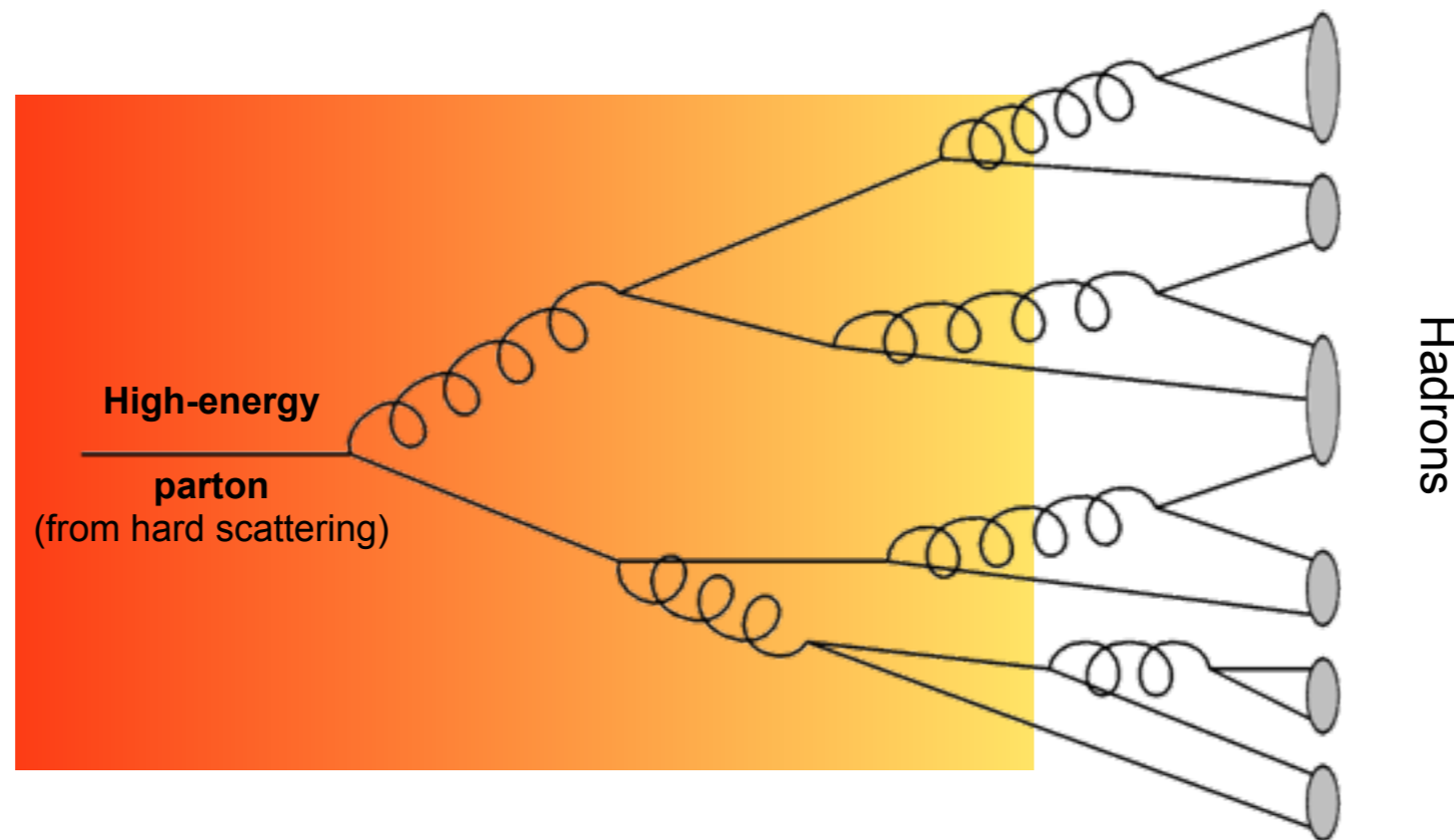
Energy loss formalisms

- Large differences between formalisms understood
 - Large angle cut-off
 - Length dependence (interference effects)
- Mostly (?) ‘technical’ issues; can be overcome
 - Use path-integral formalism
 - Monte Carlo: exact E, p conservation
 - Full 2→3 NLO matrix elements
 - Include interference
- Next step: interference in multiple gluon emission

Many new developments; see Carlos’ lectures for more
Plenty of room for interesting and relevant theory work!

In-medium showers: energy loss MC

Theory calculations on previous slides: 'factorised' approach, $P(\Delta E)$ FF



Alternative (more realistic):

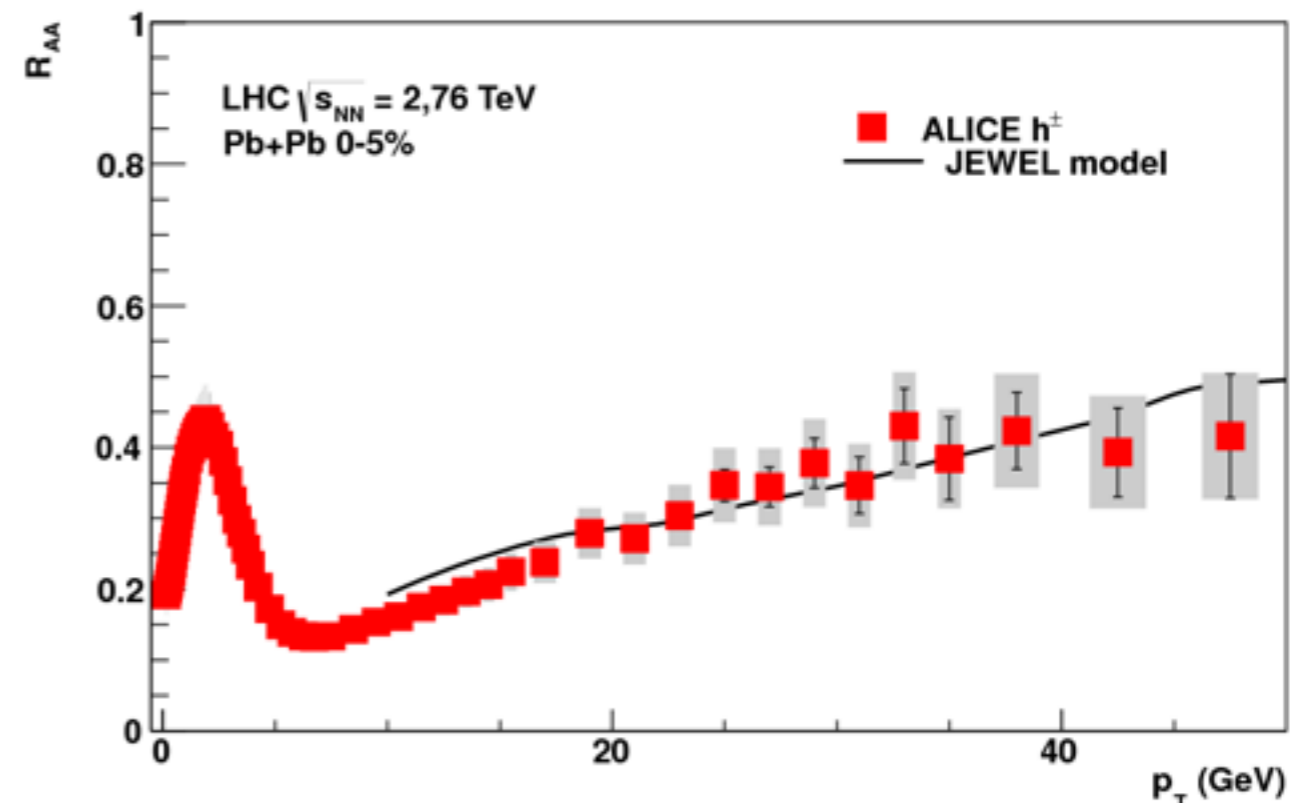
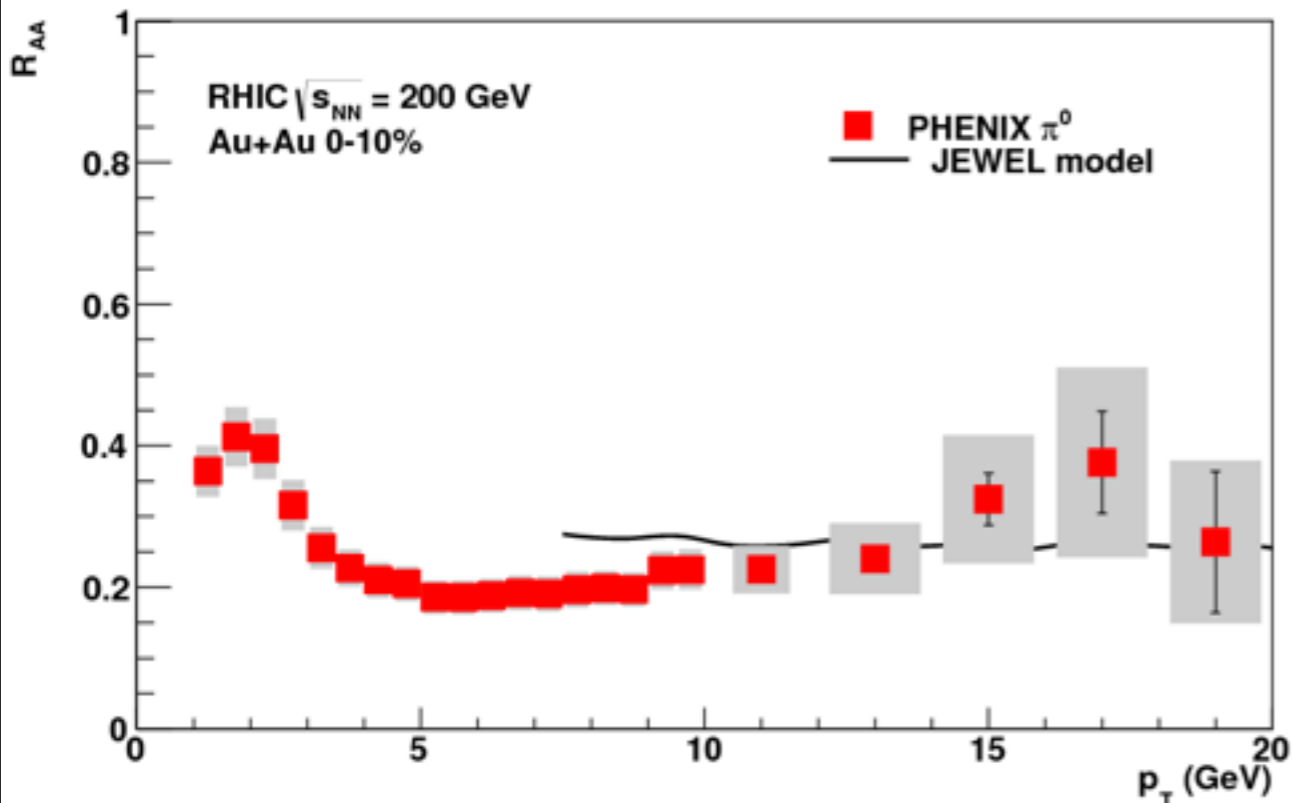
in-medium shower: every radiation is affected by the medium

(N.B.: coherence effects may be more complicated; see Carlos' lectures)

Implemented in MC codes: JEWEL, YaJEM

R_{AA} at LHC and JEWEL

- JEWEL: Monte Carlo event generator with radiative+collisional energy loss
- Modified showers with MC-LPM implementation
 - Geometry: expanding Woods-Saxon density



JEWEL energy loss model agrees with measurements
(tuned at RHIC, LHC 'parameter-free')

Effects in R_{AA}

- **Parton p_T spectra**
 - Less steep at LHC \rightarrow less suppression
 - Steepness decreases with p_T : R_{AA} rises
- **Quark vs gluon jets**
 - More gluon jets at LHC \rightarrow more suppression
 - More quark jets at high p_T : R_{AA} rises
- **Medium density (profile)**
 - Larger density at LHC \rightarrow more suppression (profile similar?)
 - Path length dependence of energy loss
- **Parton energy dependence**
 - Expect slow (log) increase of ΔE with $E \rightarrow R_{AA}$ rises with p_T
 - Running of α_S (A Buzzatti@QM2012) ?
- **Energy loss distribution**
 - Expect broad distribution $P(\Delta E)$; kinematic bounds important

‘Known’,
external
input

Energy loss
theory

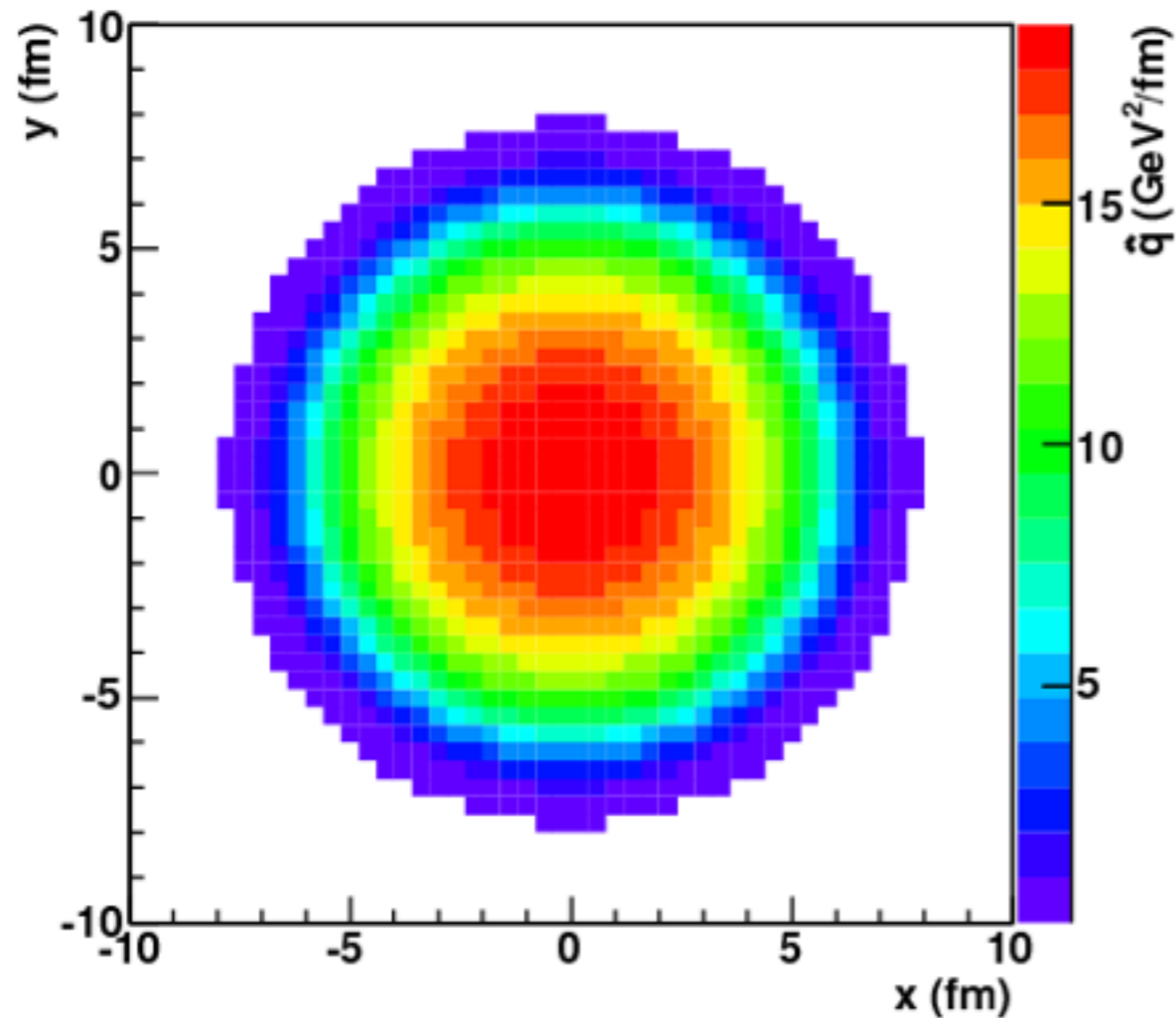
Determine/
constrain from
measurements

Use different observables to disentangle effects contributions

Part II: Path length dependence

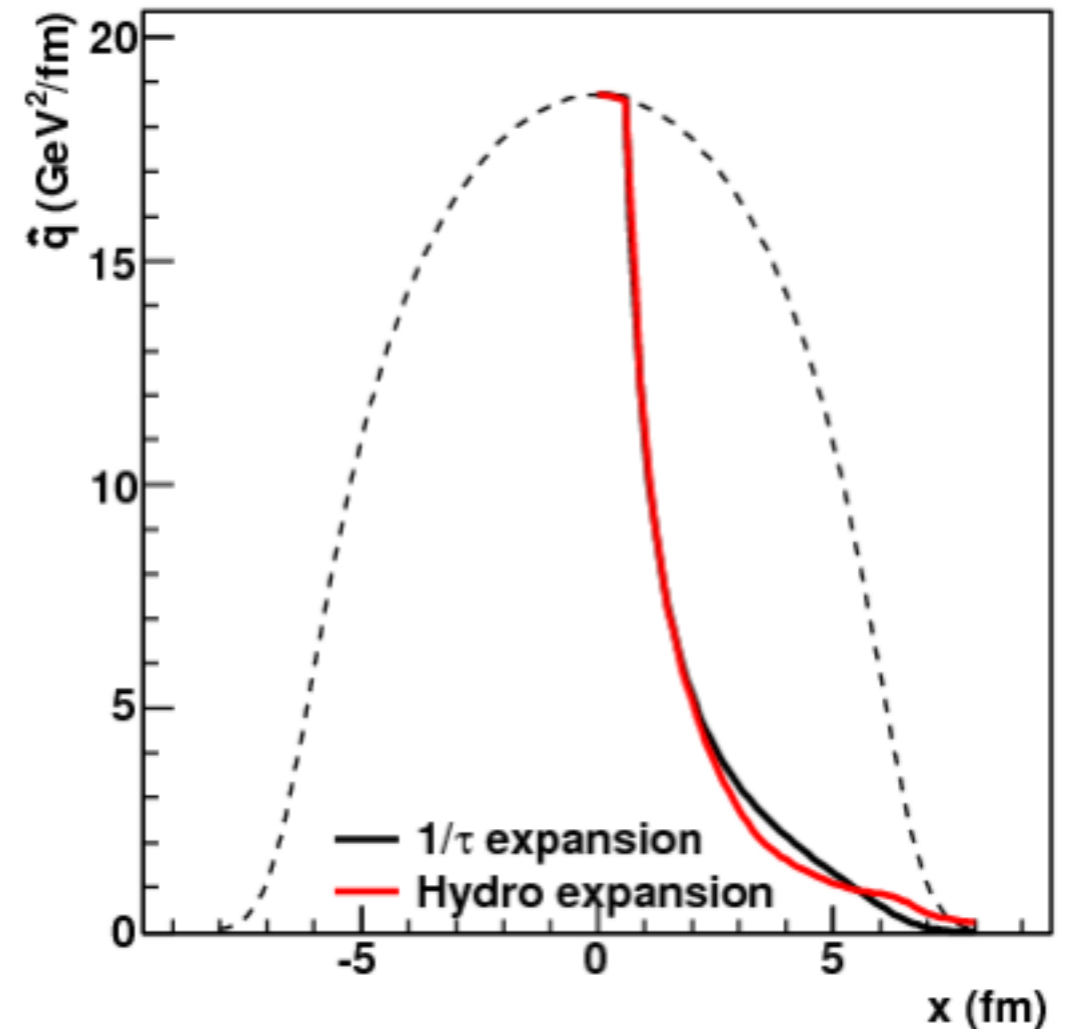
Geometry

Density profile



Profile at $\tau \sim \tau_{\text{form}}$ known

Density along parton path



Longitudinal expansion
dilutes medium
⇒ Important effect

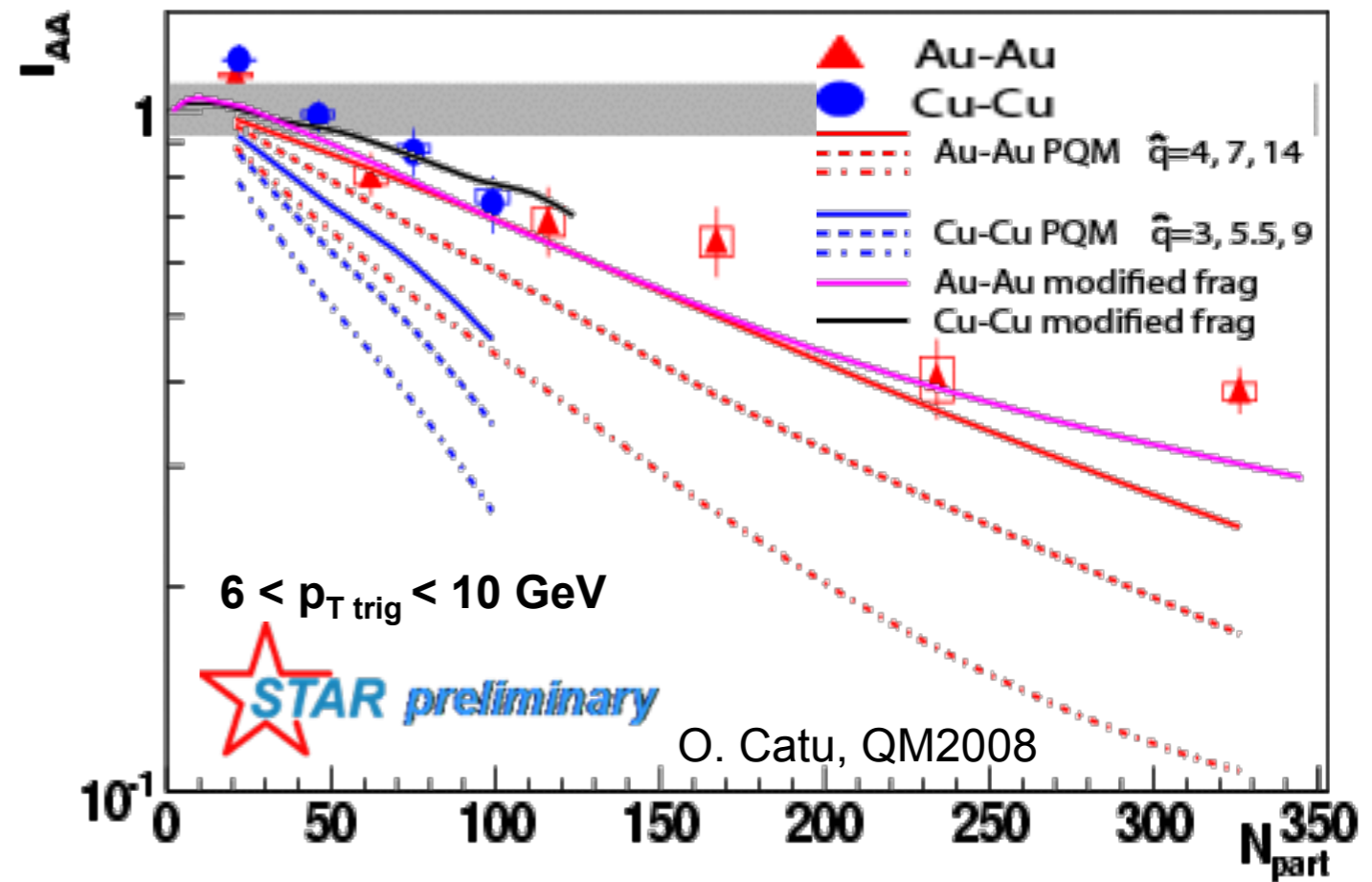
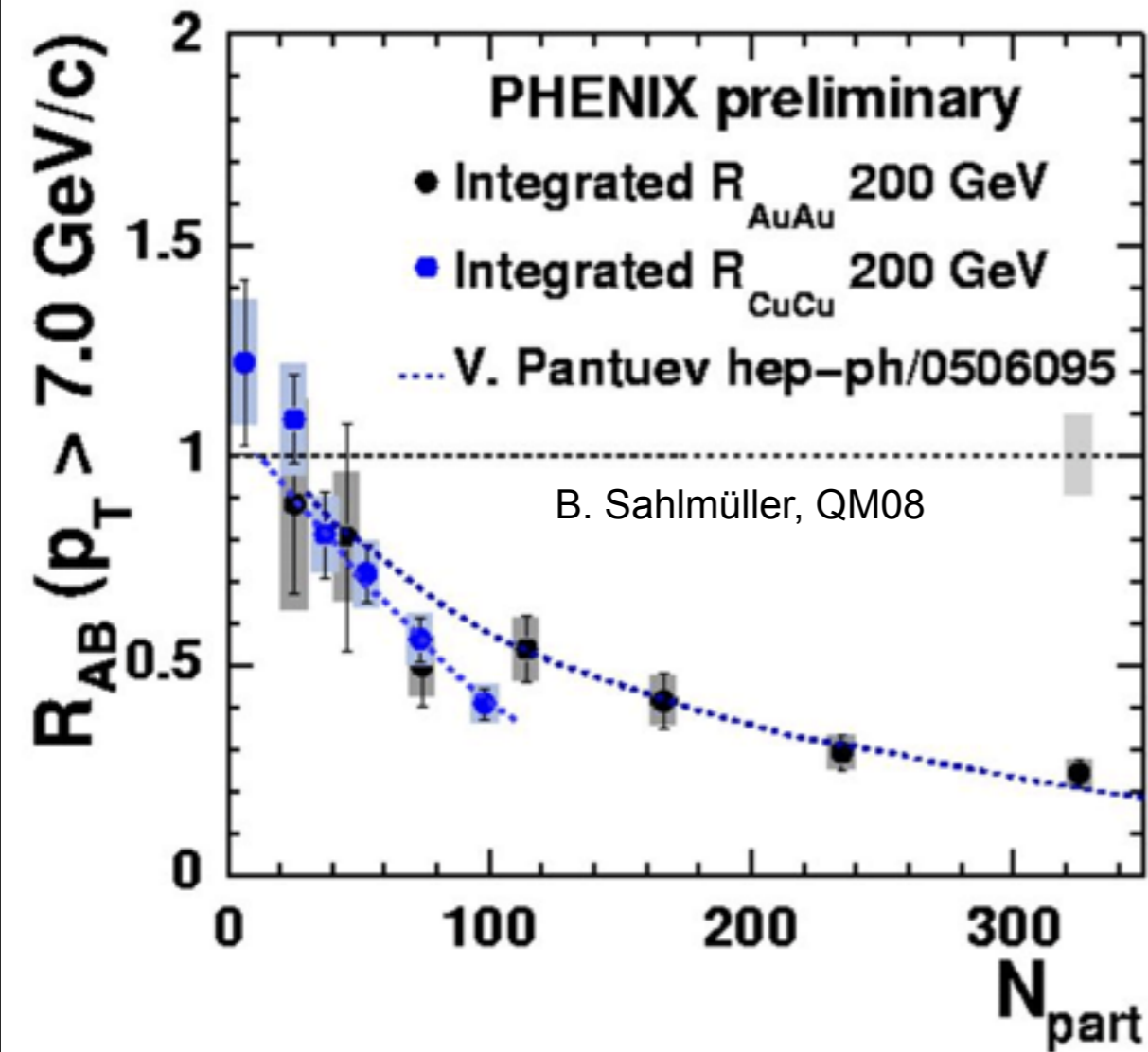
Most models take space-time evolution into account

Path length I: centrality dependence

Comparing Cu+Cu and Au+Au

R_{AA} : inclusive suppression

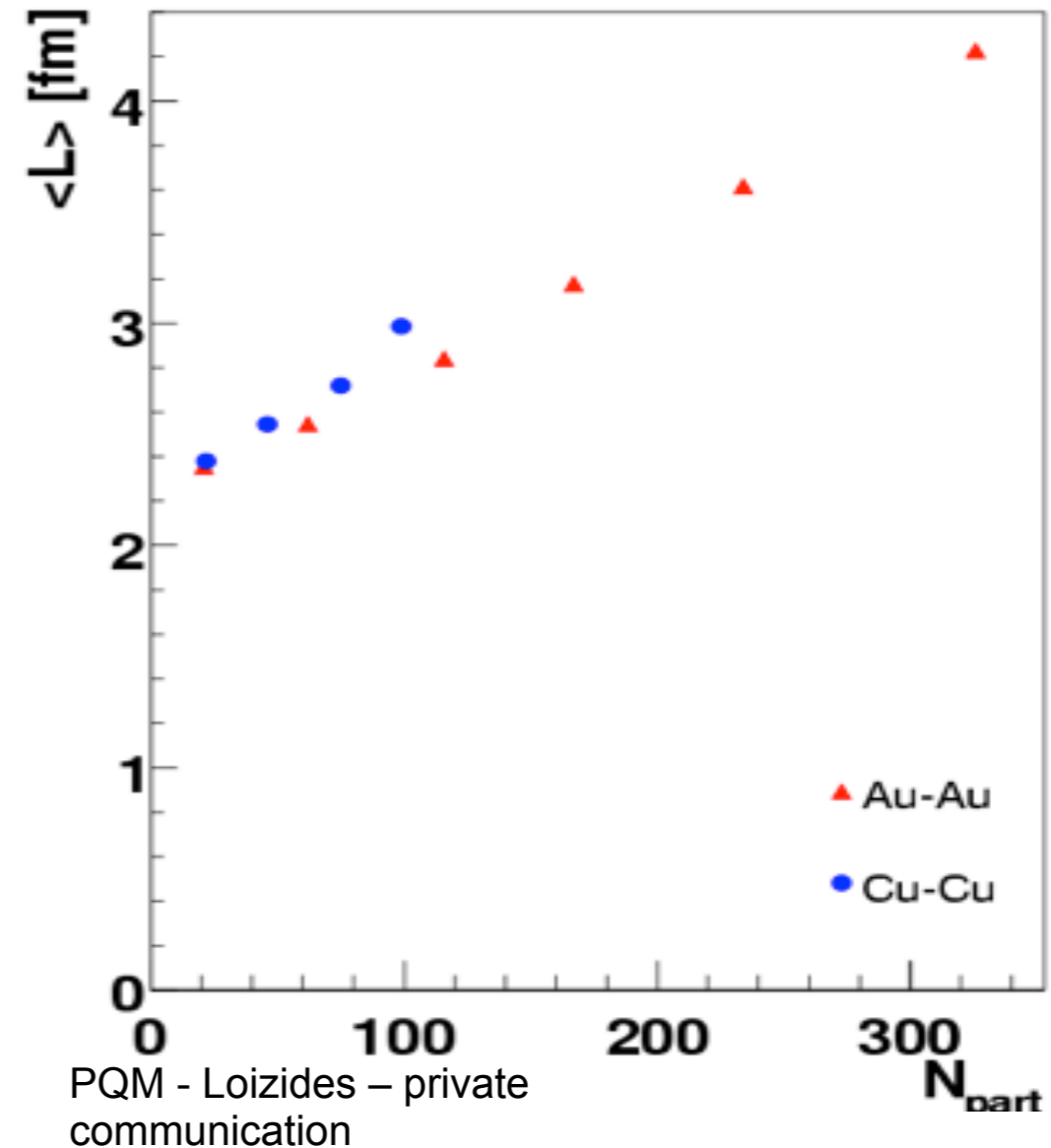
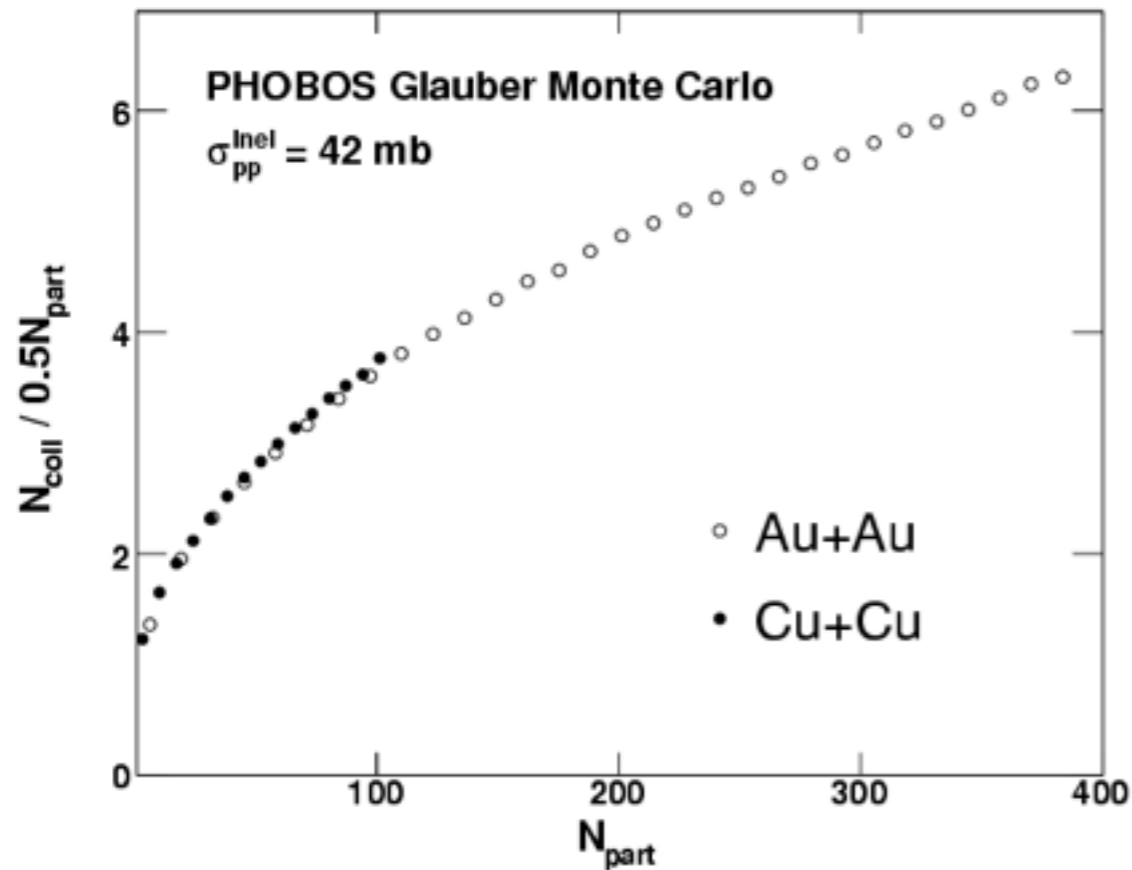
Away-side suppression



Modified frag: nucl-th/0701045 - H.Zhang, J.F. Owens, E. Wang, X.N. Wang

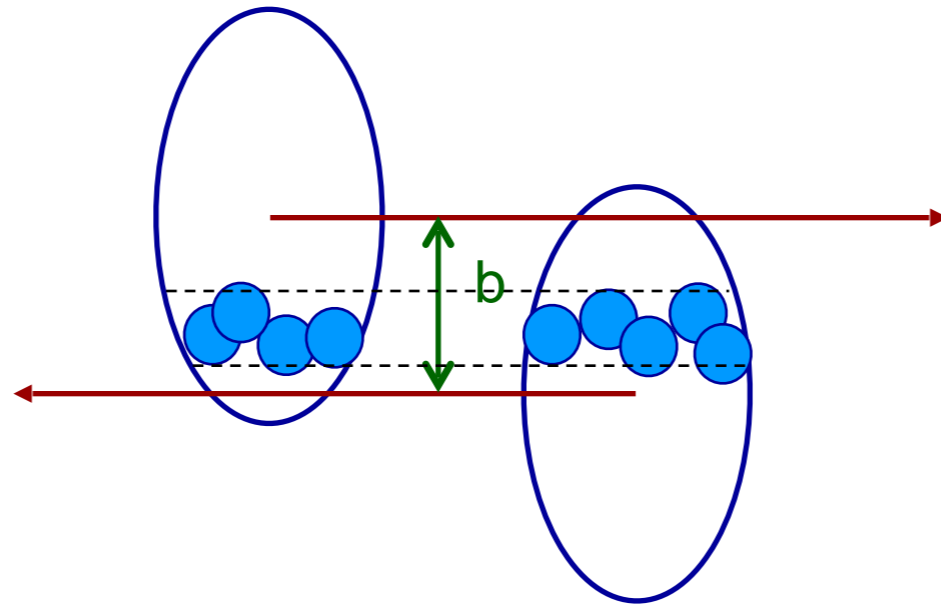
Inclusive and di-hadron suppression seem to scale with N_{part}

N_{part} scaling?



Geometry (thickness, area) of
central Cu+Cu similar to peripheral Au+Au
Cannot disentangle density vs path length

Nuclear geometry: N_{part} , N_{coll}

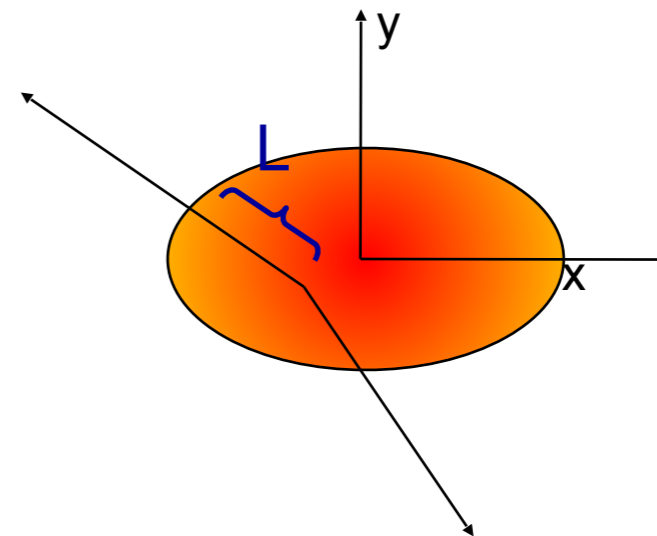


Non-central collisions: eccentric matter distribution
Transverse view

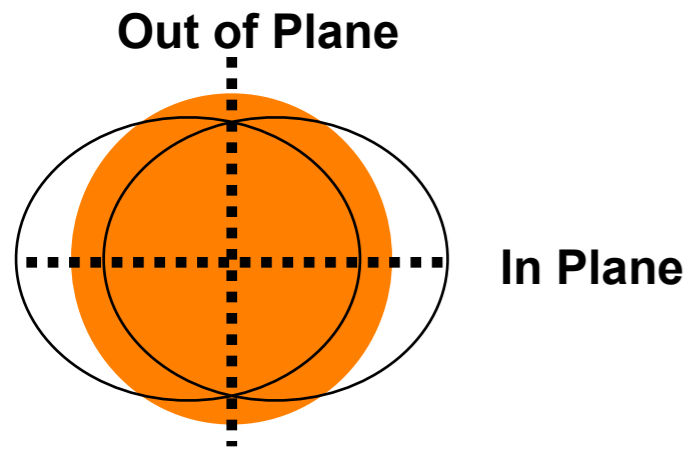
Density profile ρ : ρ_{part} or ρ_{coll}

Eccentricity

$$\varepsilon = \frac{\sigma_y^2 - \sigma_x^2}{\sigma_y^2 + \sigma_x^2}$$



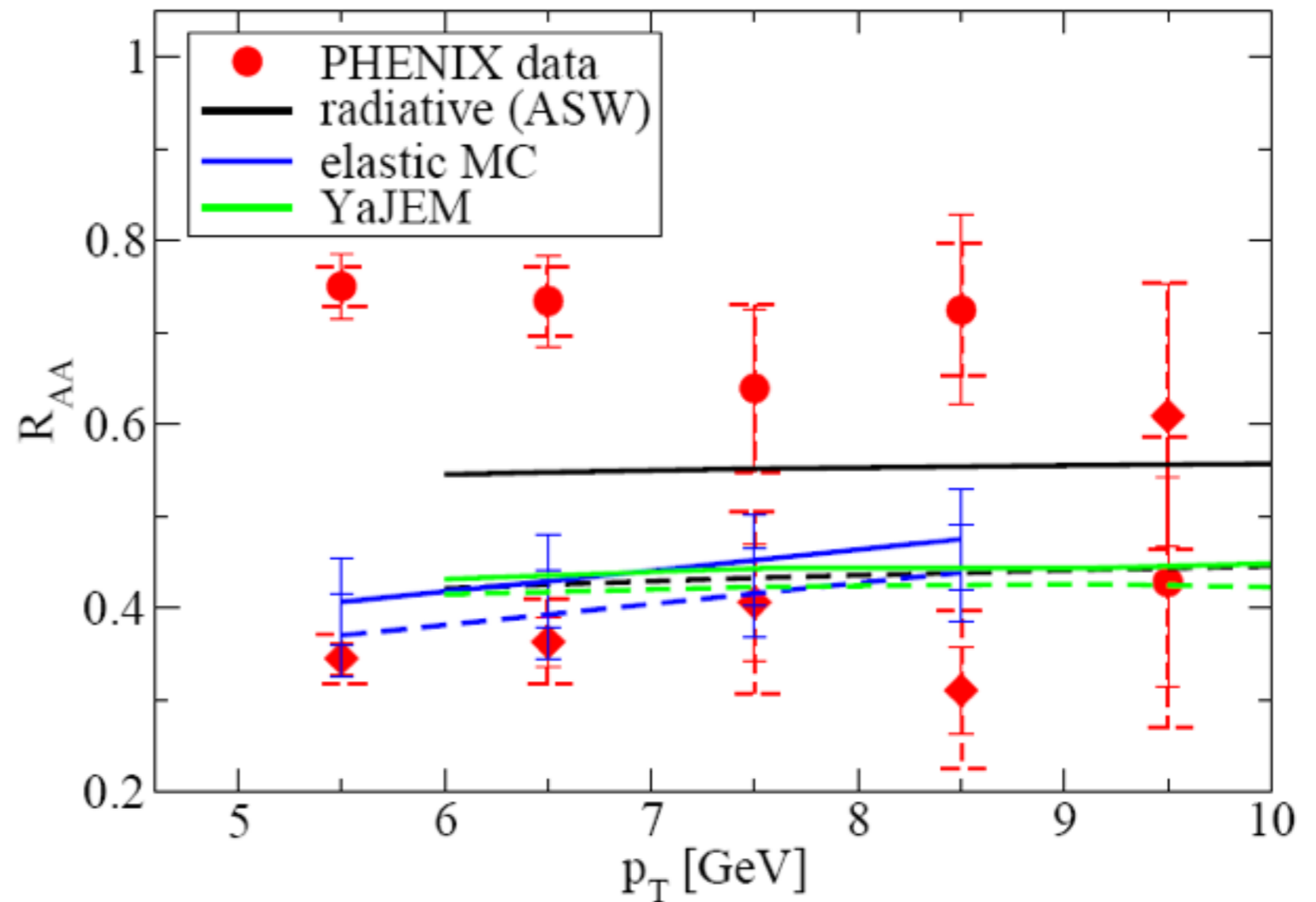
R_{AA} vs φ and elastic e-loss



Elastic E-loss gives small v_2

Data require L^2 or stronger path length dependence

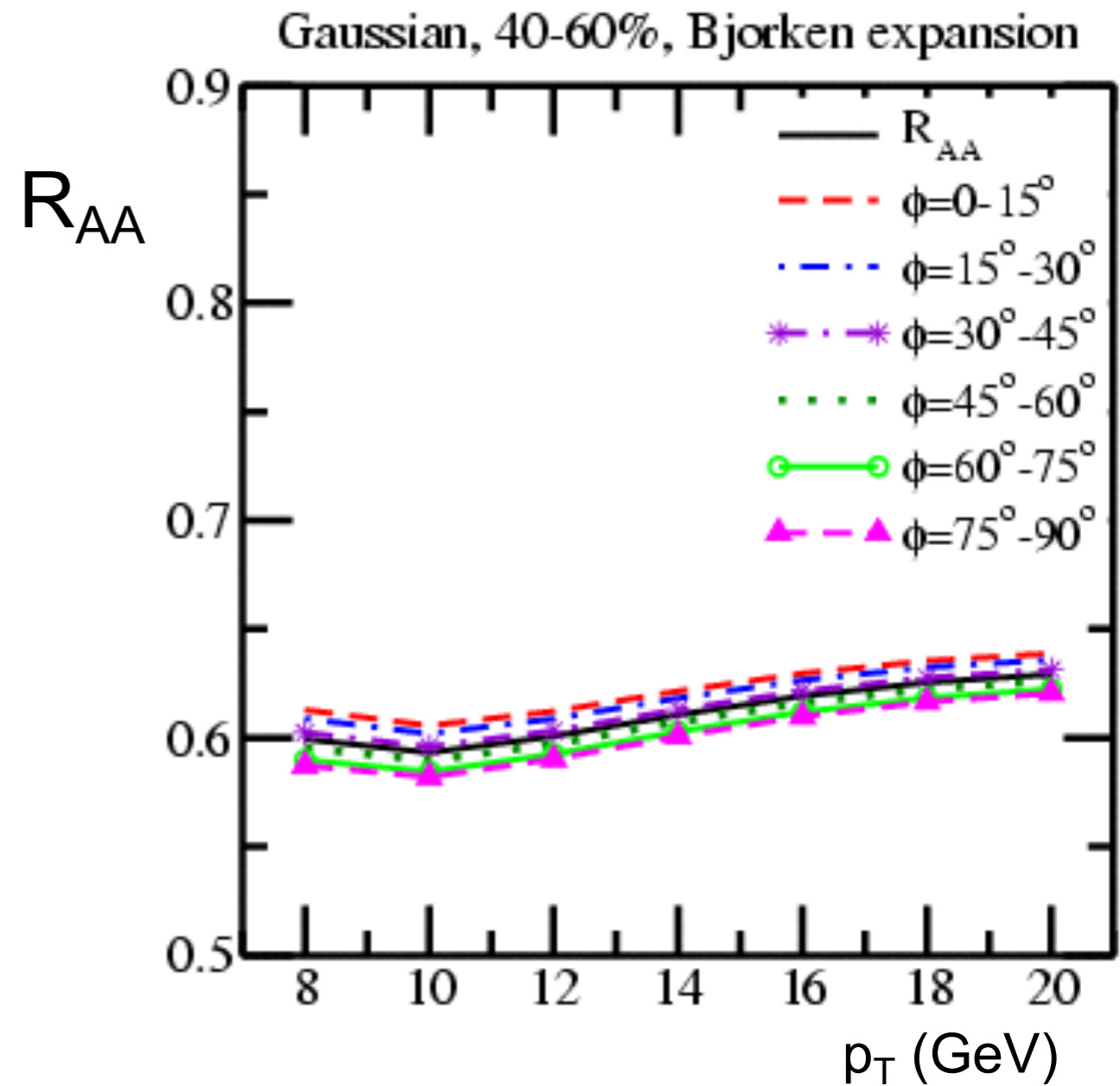
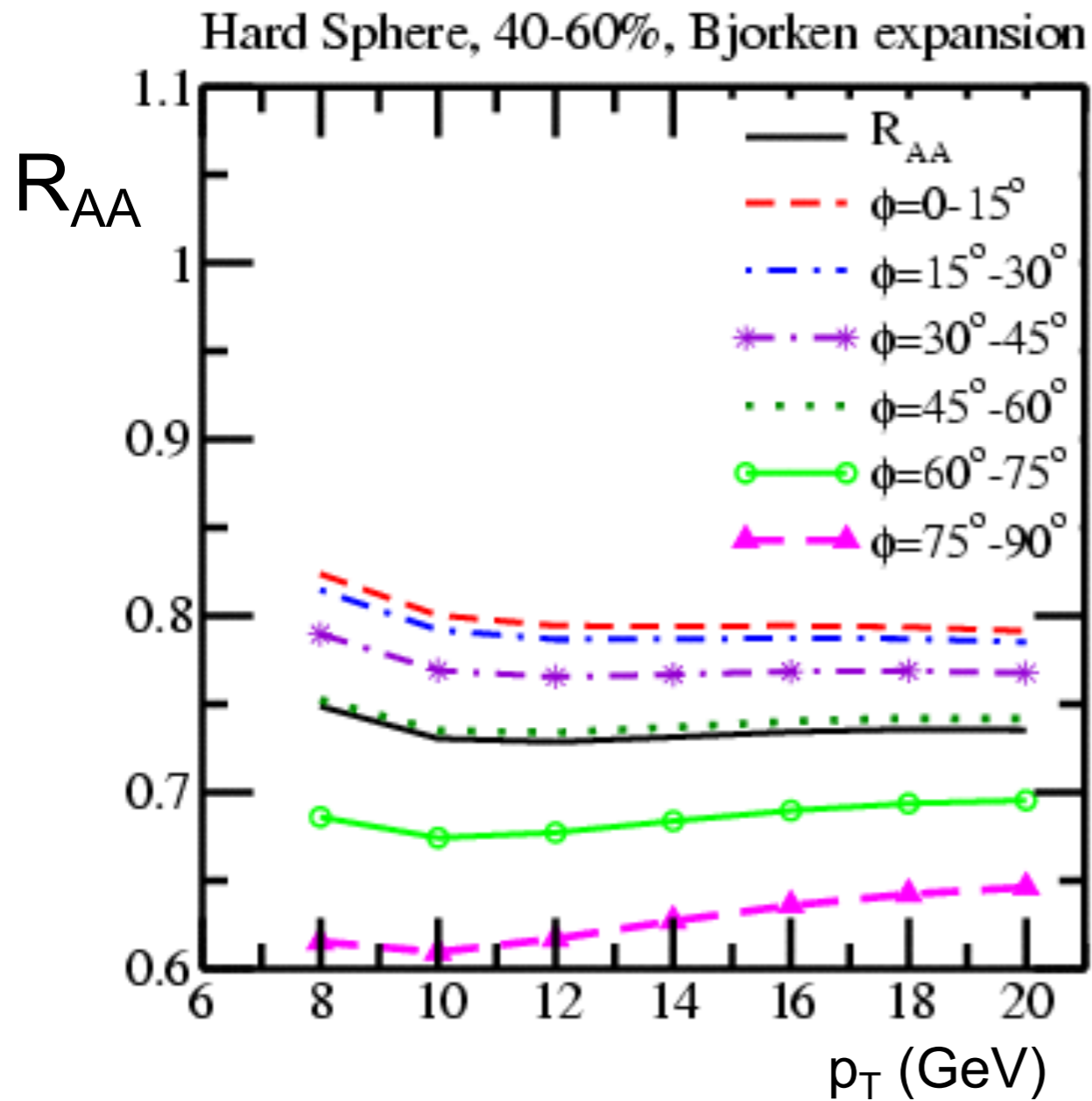
AuAu 200 AGeV, 40 - 50 %



However, also quite sensitive to medium density evolution

Modelling azimuthal dependence

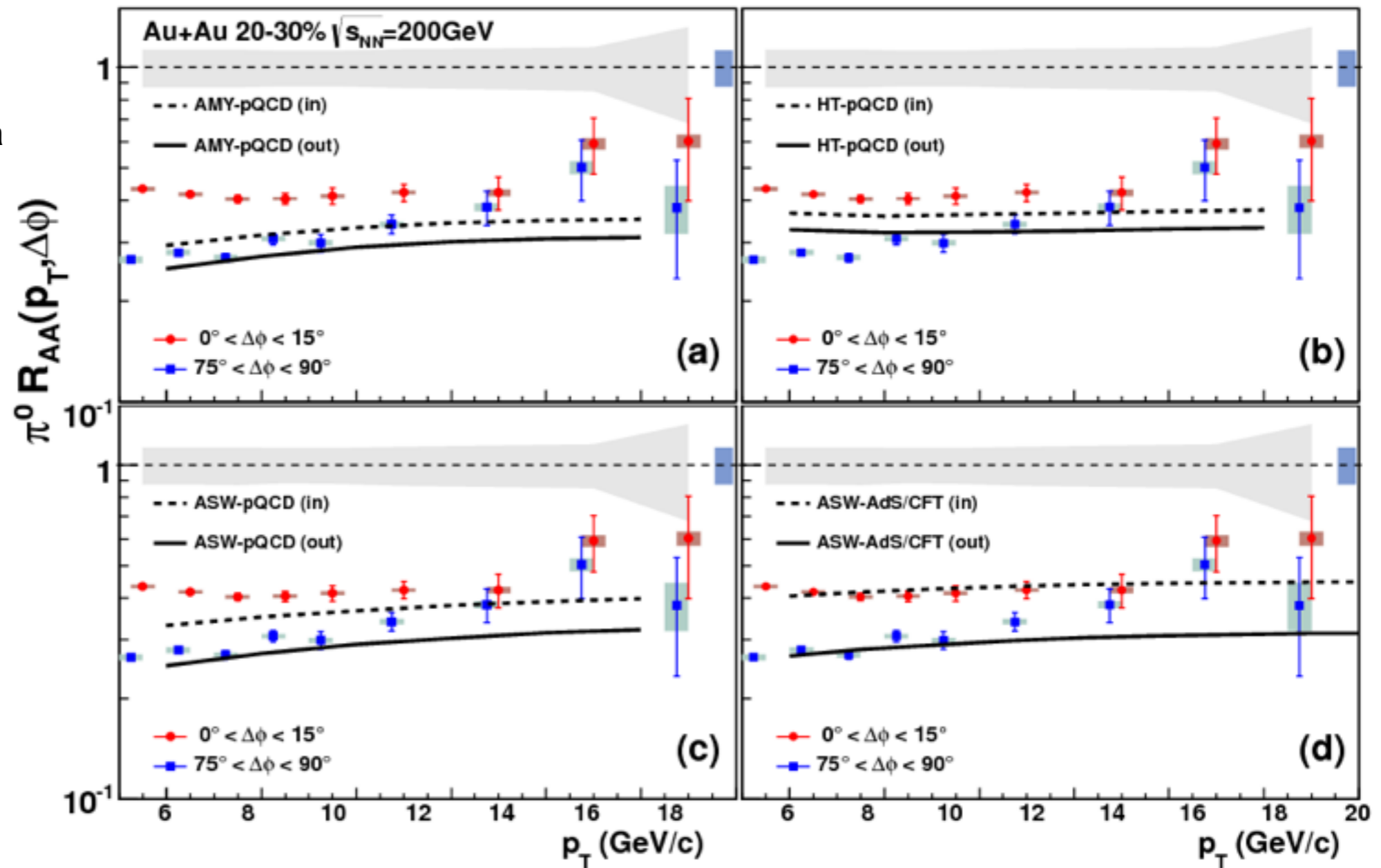
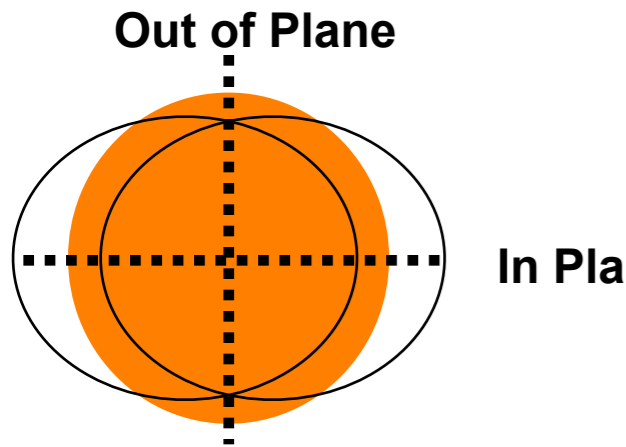
A. Majumder, PRC75, 021901



R_{AA} vs reaction plane sensitive to geometry model

Path length dependence: R_{AA} vs φ

PHENIX, arXiv:1208.2254

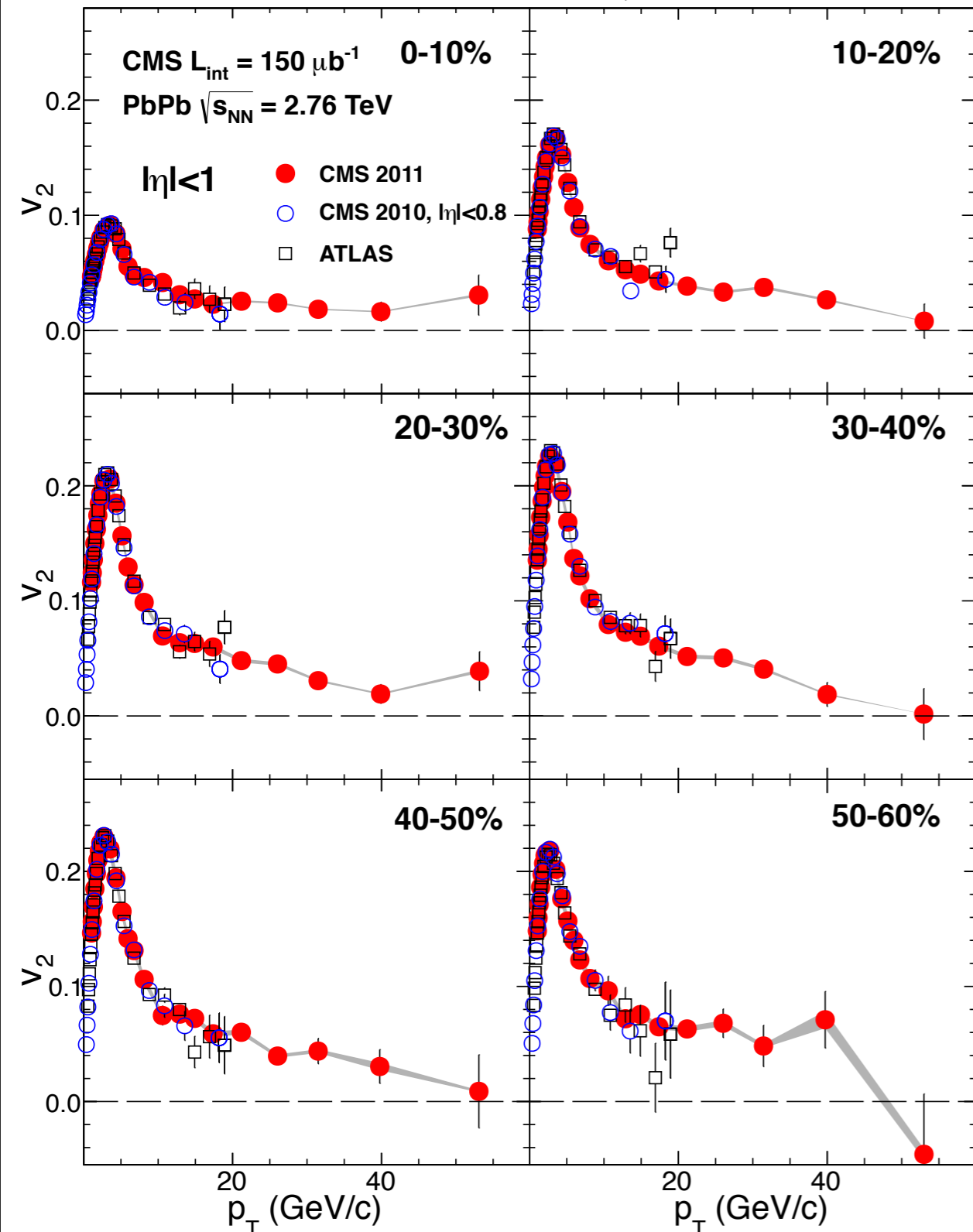


Suppression depends on angle, path length

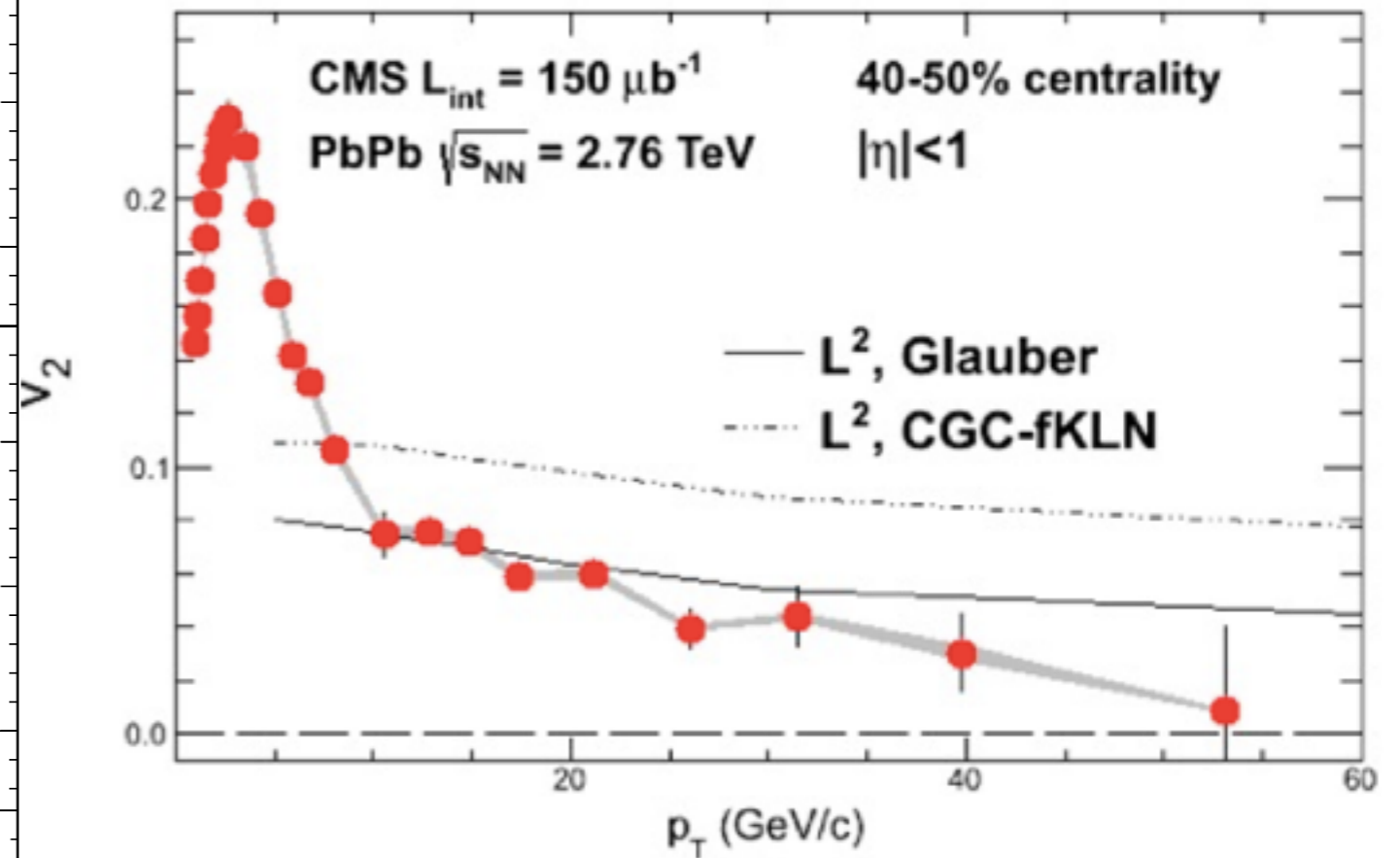
Not so easy to model: calculations give different results

Reaction plane dependence at LHC: High- p_T v_2

CMS, arXiv:1204.1850



Model: B. Betz, M. Gyulassy, arXiv:1201.0281

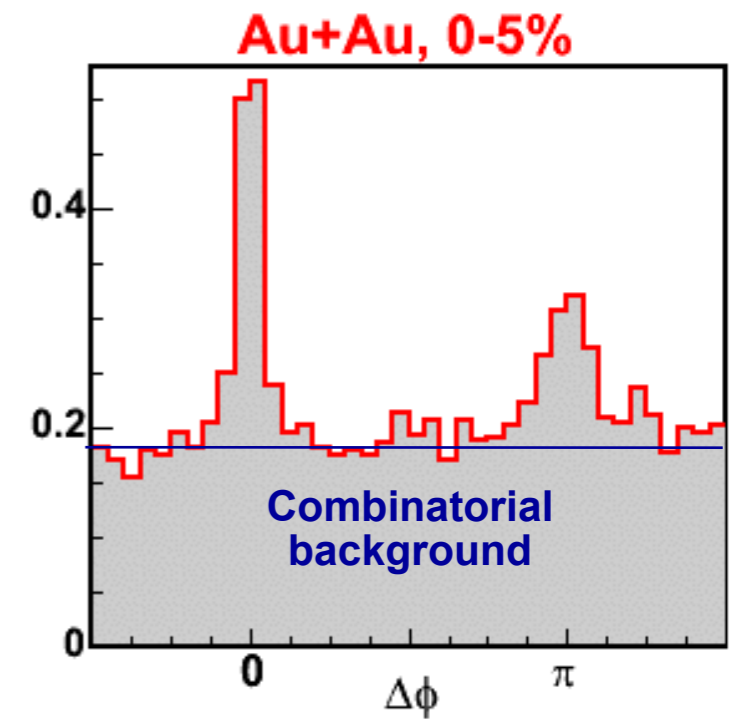
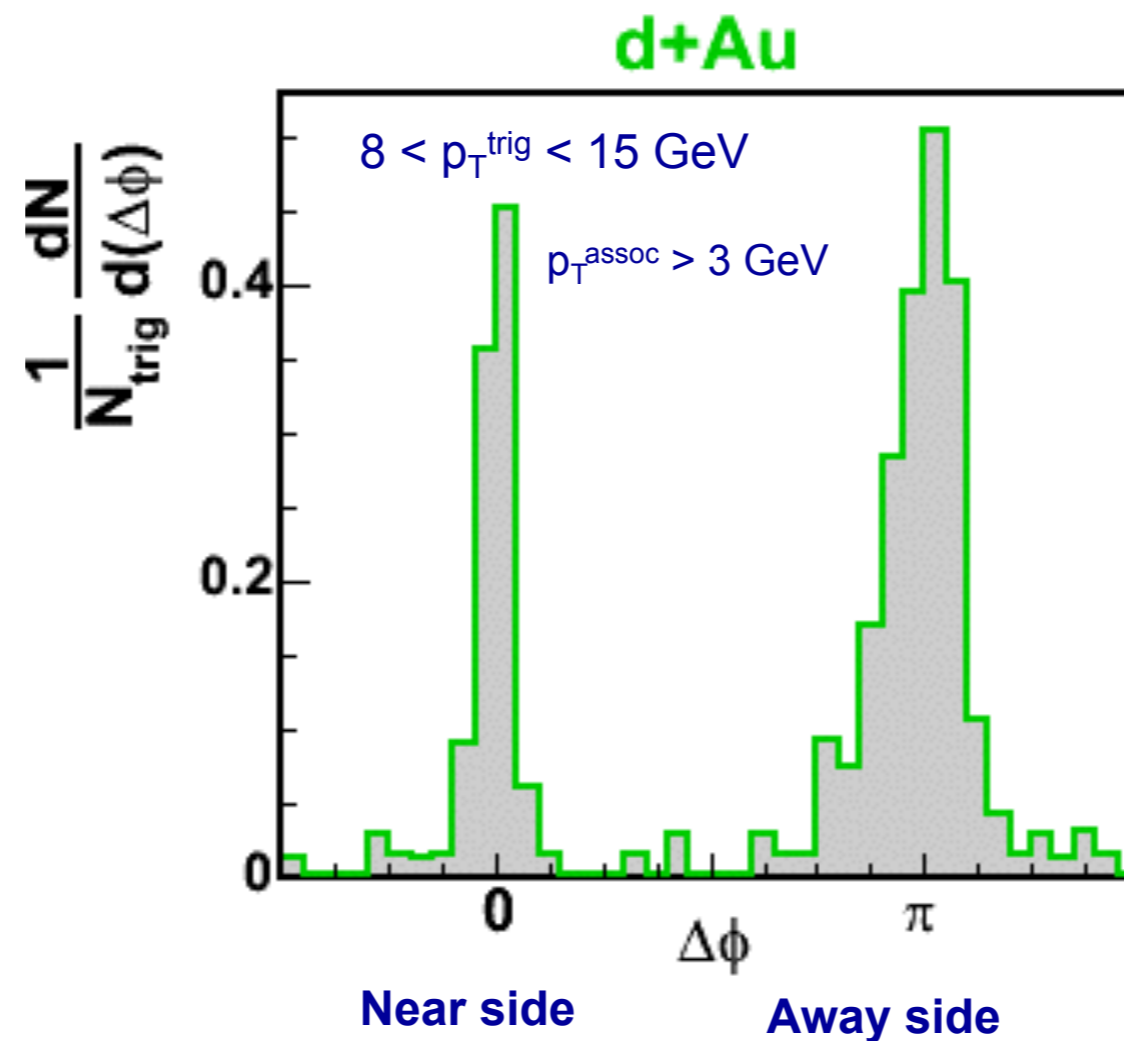
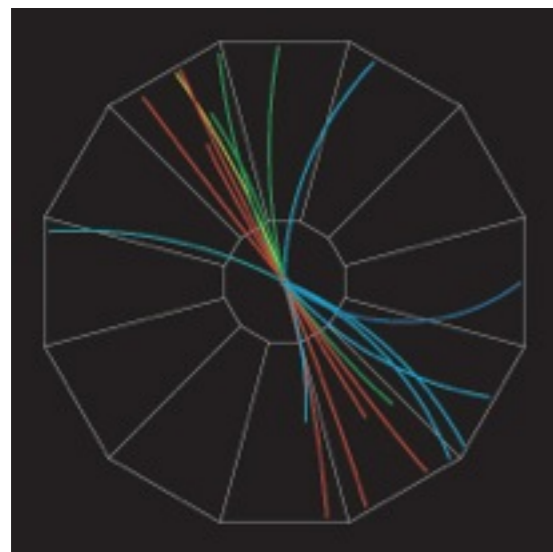
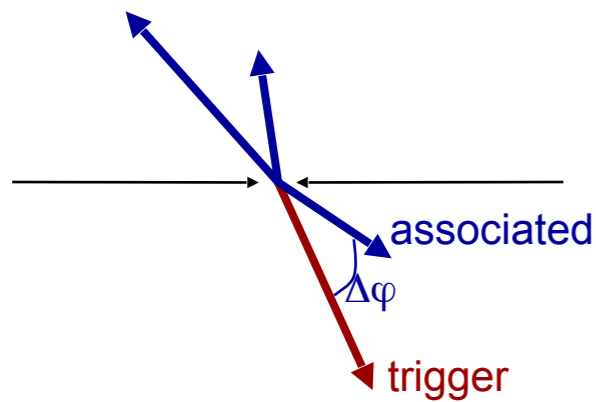


Reasonable agreement between calculation and data for $p_T > 10 \text{ GeV}$

(NB: simplified geometry, E-loss; paper claims scale-dependence of α_s main effect)

**A unexpected angle on path length
dependence: di-hadron correlations**

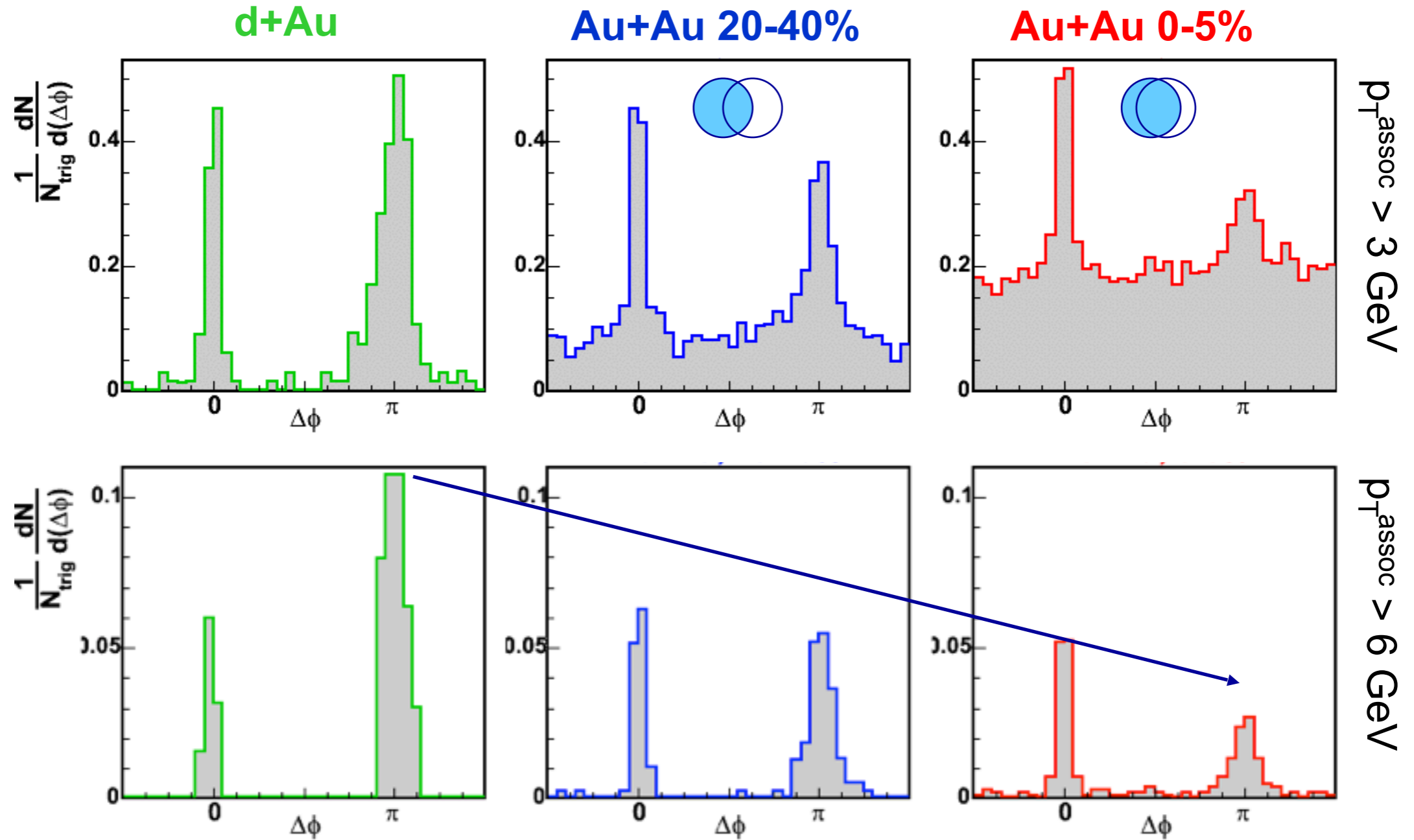
Dihadron correlations



Use di-hadron correlations to probe the jet-structure in p+p, d+Au

and Au+Au

Di-hadrons at high- p_T : recoil suppression



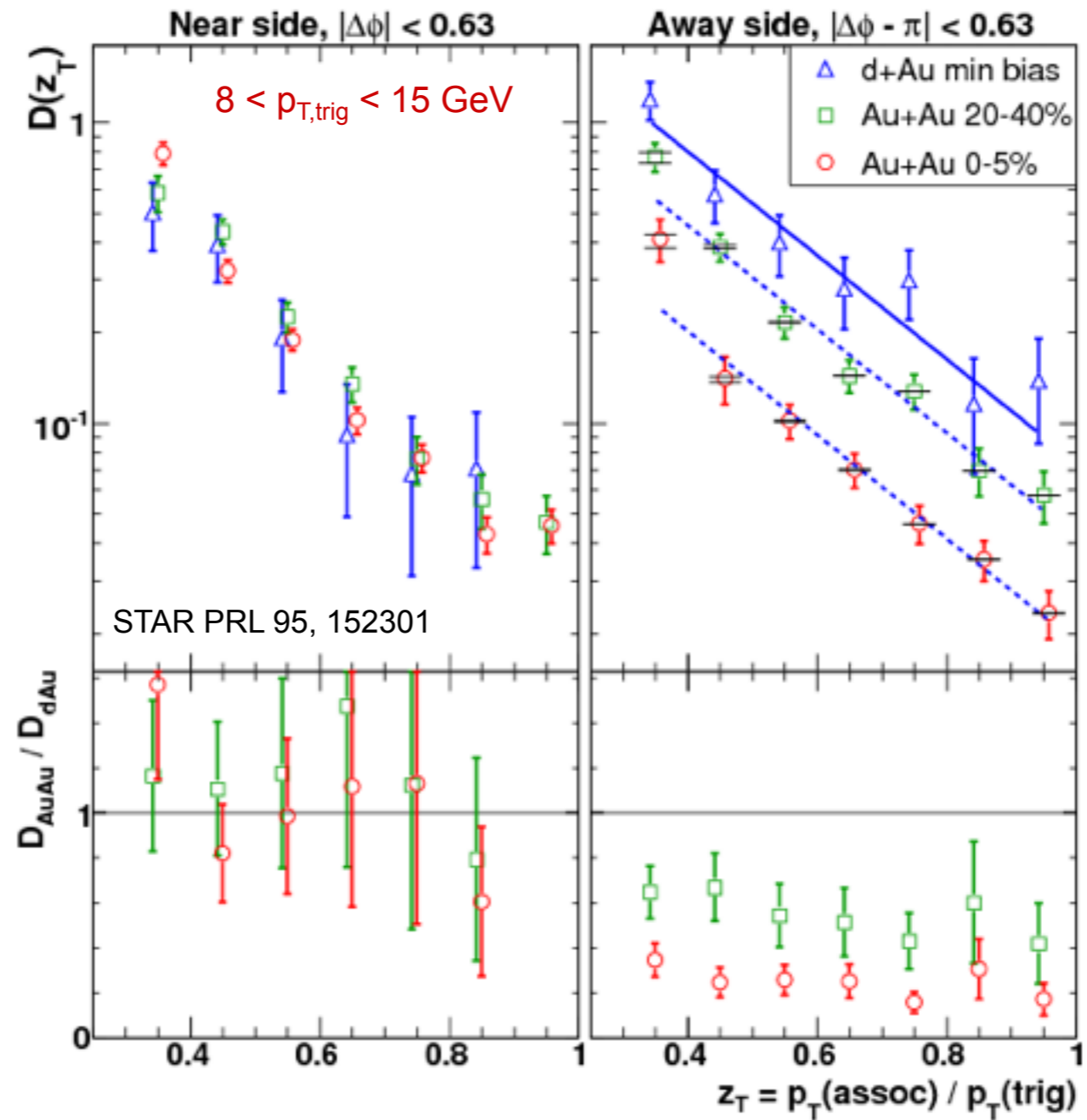
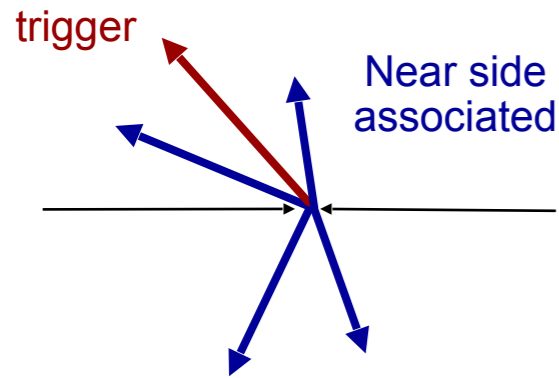
High- p_T hadron production in Au+Au dominated by (di-)jet fragmentation

Suppression of away-side yield in Au+Au collisions: energy loss

Dihadron yield suppression

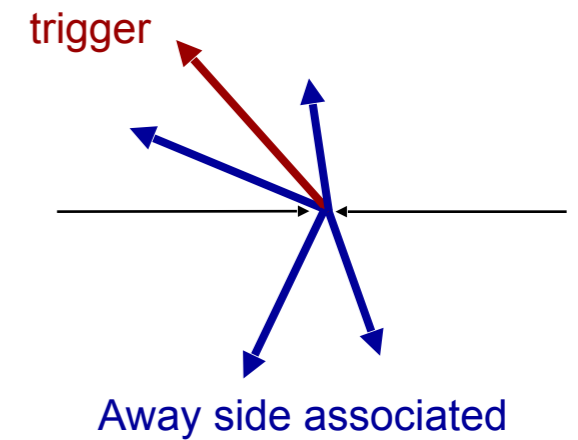
Near side

Yield of additional particles in the jet



Away side

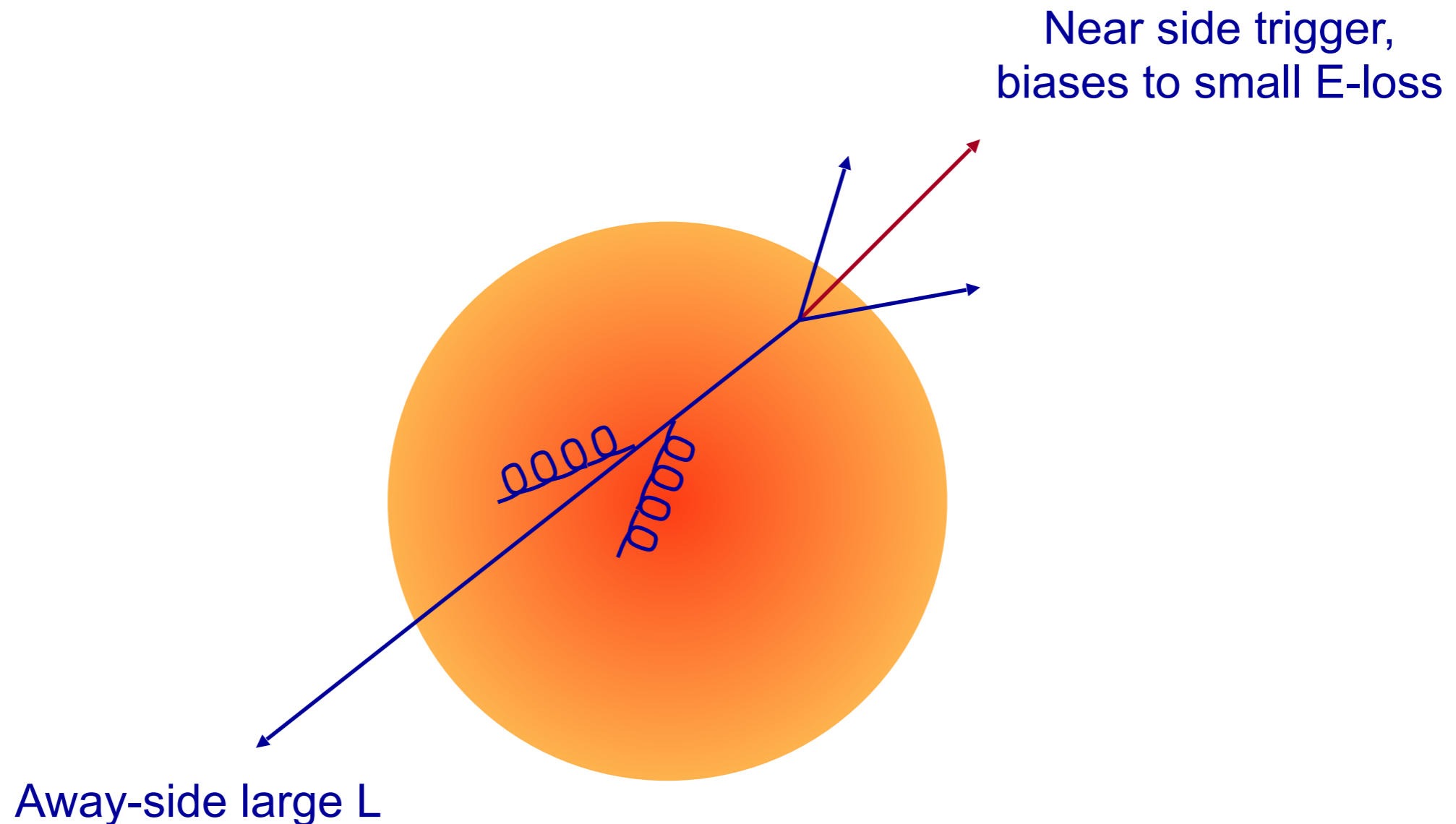
Yield in balancing jet, after energy loss



Near side: No modification
 \Rightarrow Fragmentation outside medium?

Away-side: Suppressed by factor 4-5
 \Rightarrow large energy loss

Path length II: 'surface bias'

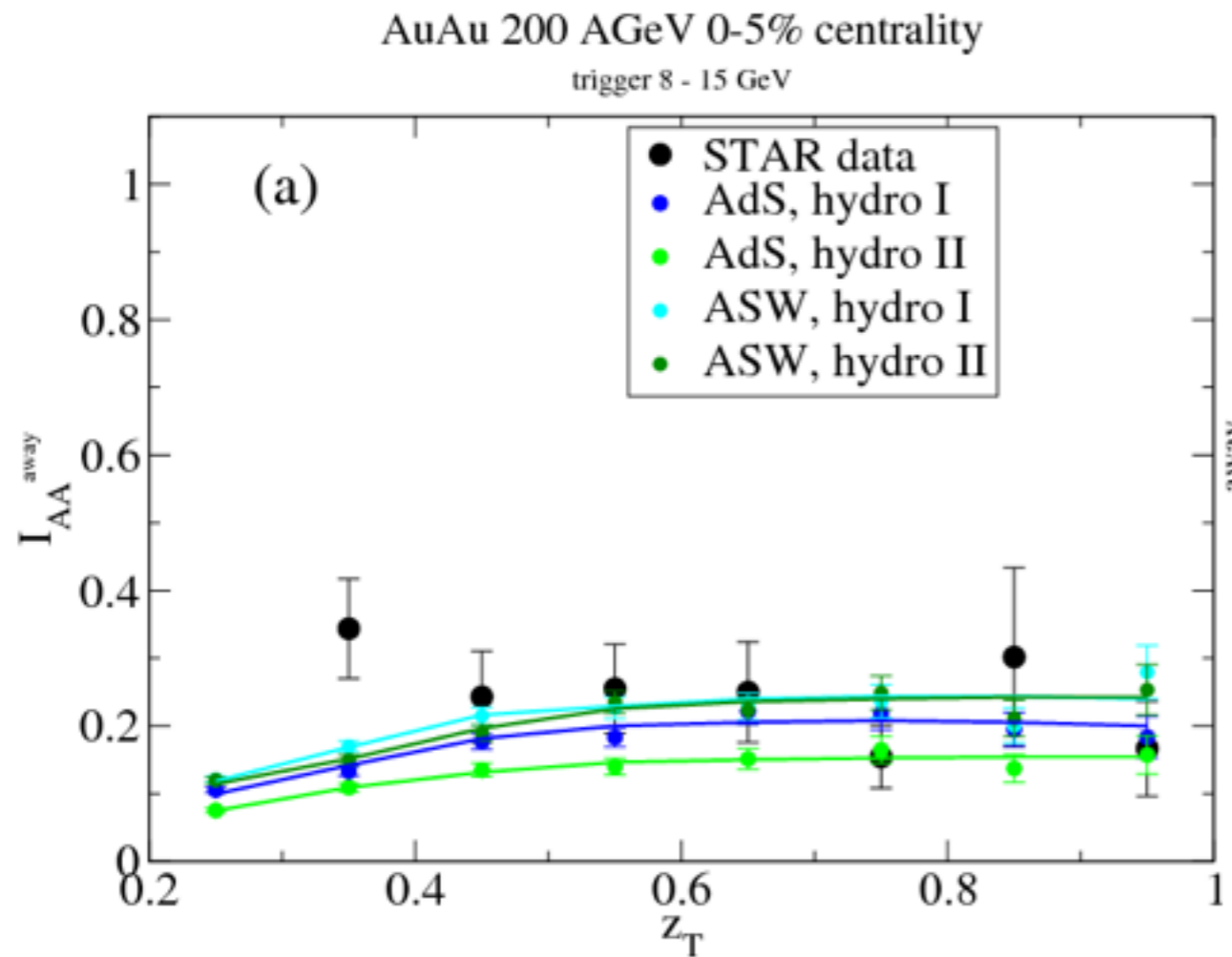


Away-side (recoil) suppression I_{AA} samples longer path-lengths
than inclusives R_{AA}

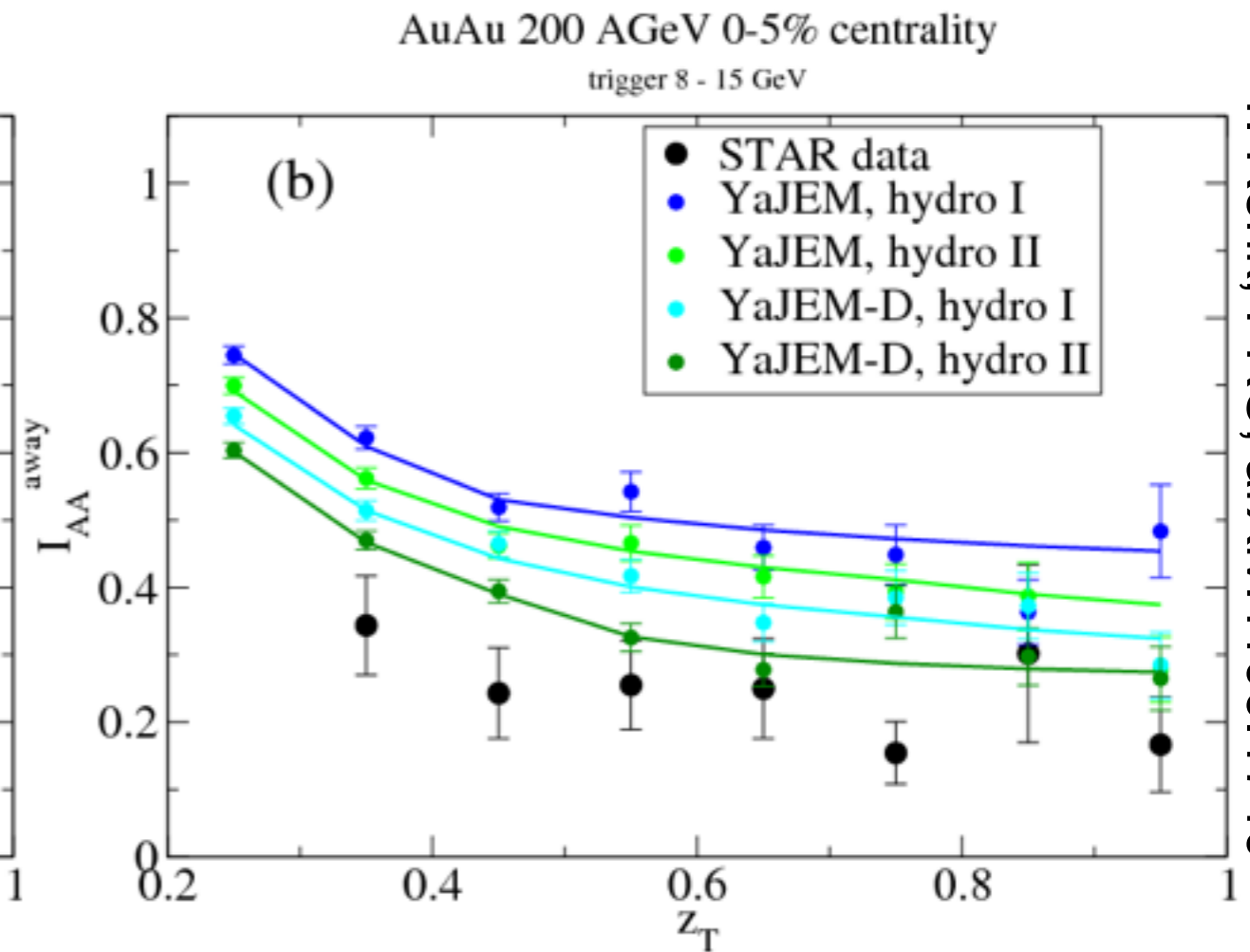
NB: other effects play a role: quark/gluon composition, spectral shape (less steep for recoil)

Di-hadron modeling

Model 'calibrated' on single hadron R_{AA}



L^2 (ASW) fits data
 L^3 (AdS) slightly below



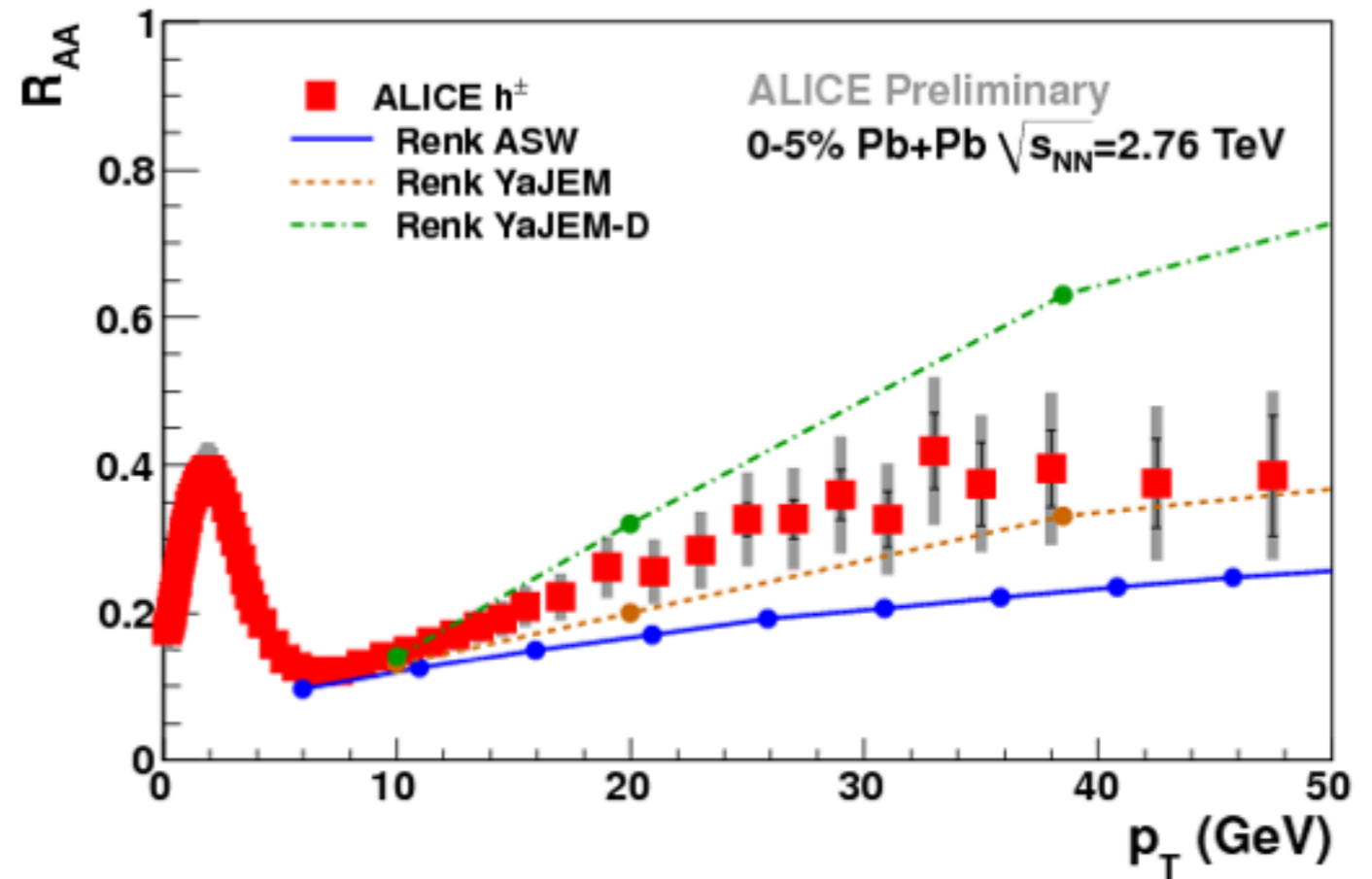
L (YaJEM): too little suppression
 L^2 (YaJEM-D) slightly above

Modified shower
generates increase at low z_T

Di-hadrons and single hadrons at LHC

Need simultaneous comparison to several measurements to constrain geometry and E-loss

Here: R_{AA} and I_{AA}

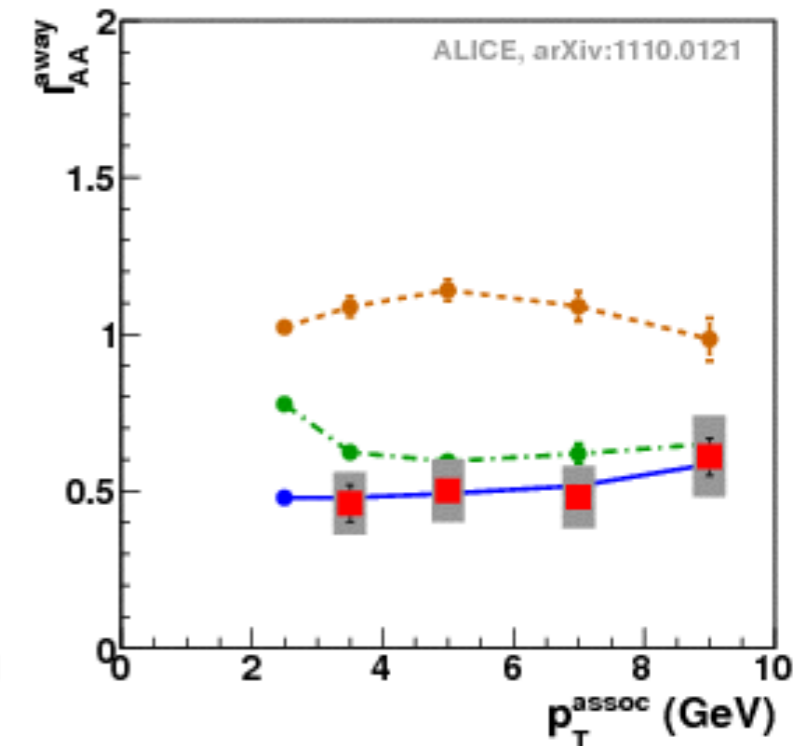
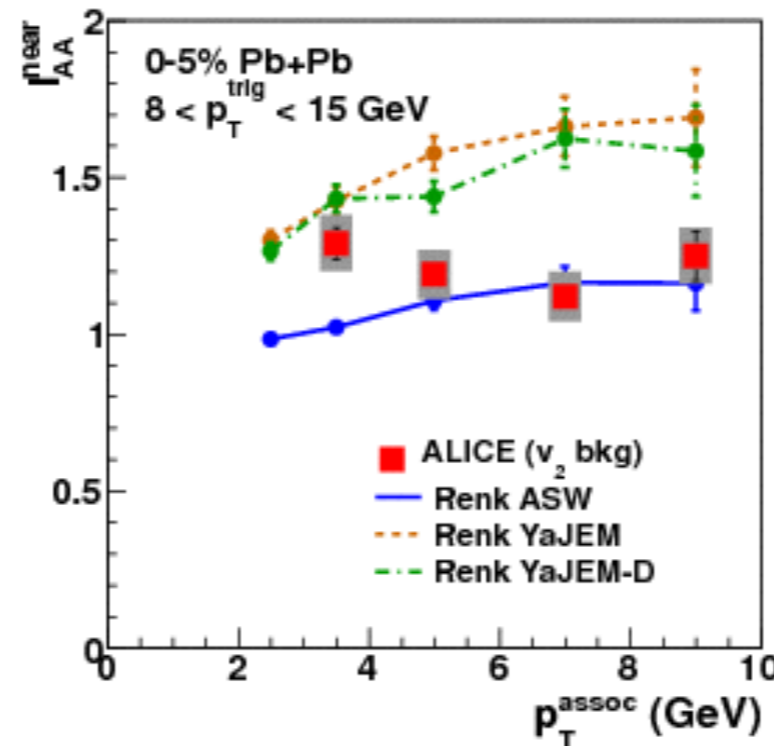


Three models:

ASW: radiative energy loss

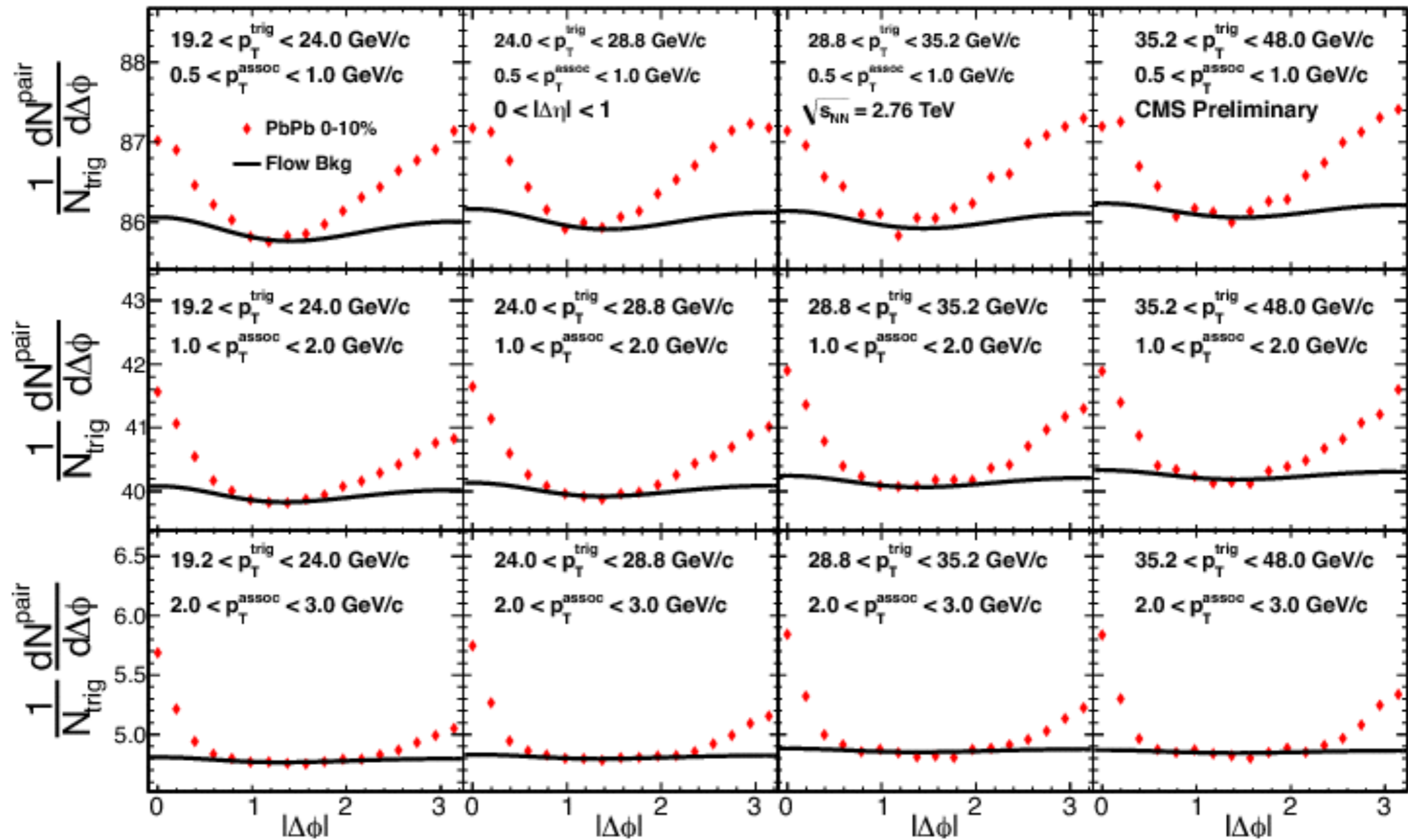
YaJEM: medium-induced virtuality

YaJEM-D: YaJEM with L-dependent virtuality cut-off (induces L^2)



Di-hadron with high- p_T trigger

p_T^{trig} (GeV): 19.2 - 24.0 GeV 14.0 - 28.8 GeV 28.8-35.2 GeV 35.2-48.0 GeV



$p_t^{\text{trig}} > 20$ GeV at LHC: strong signals even at low p_T^{assoc} 1-3 GeV

CMS di-hadrons: near side

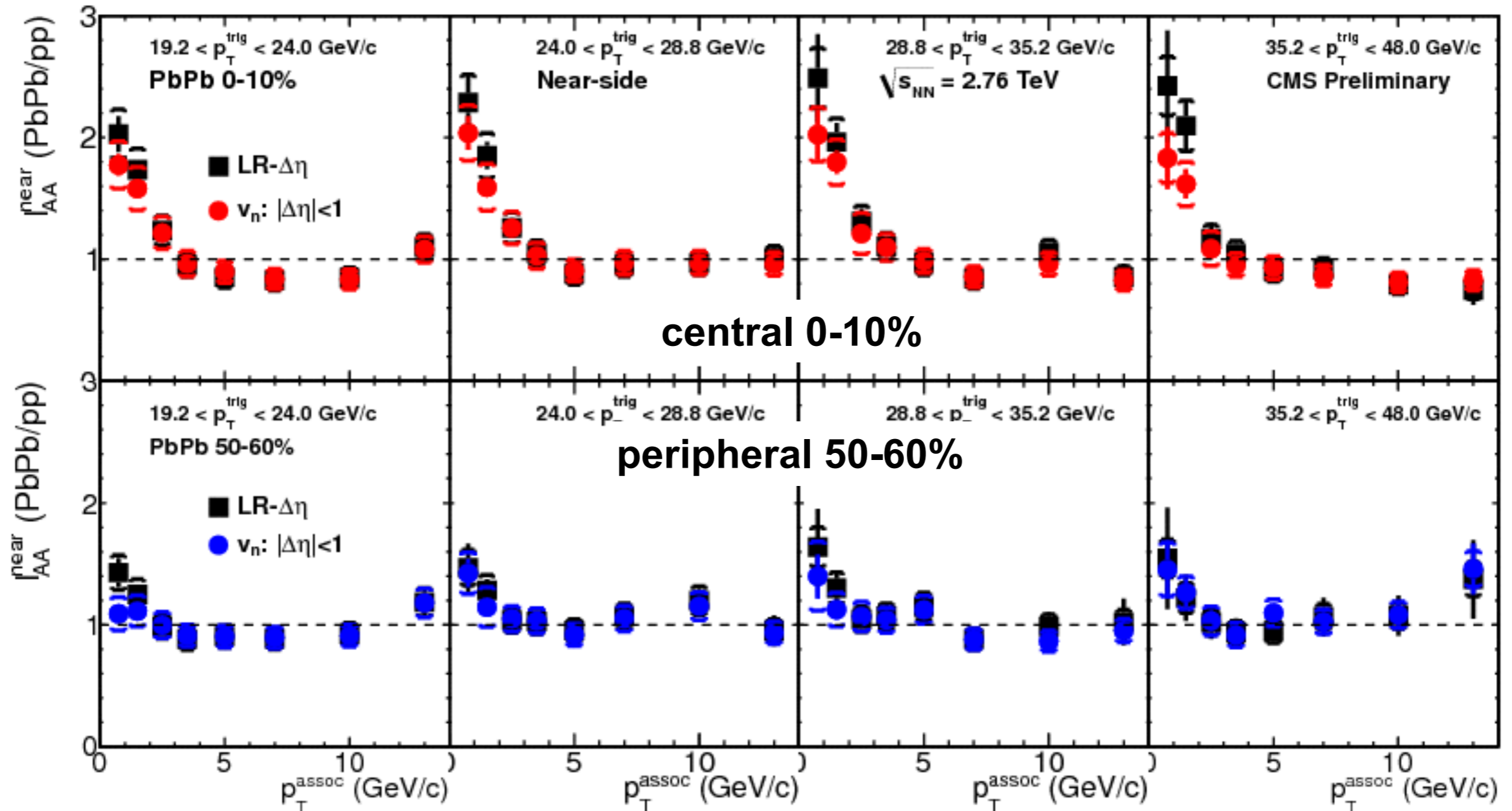
p_T^{trig} (GeV):

19.2 - 24.0 GeV

14.0 - 28.8 GeV

28.8-35.2 GeV

35.2-48.0 GeV



Transition enhancement \rightarrow suppression @ $p_T \sim 3$ GeV

also compatible with $I_{AA}=1$ at $p_T > 3$ GeV?

CMS di-hadrons: away side

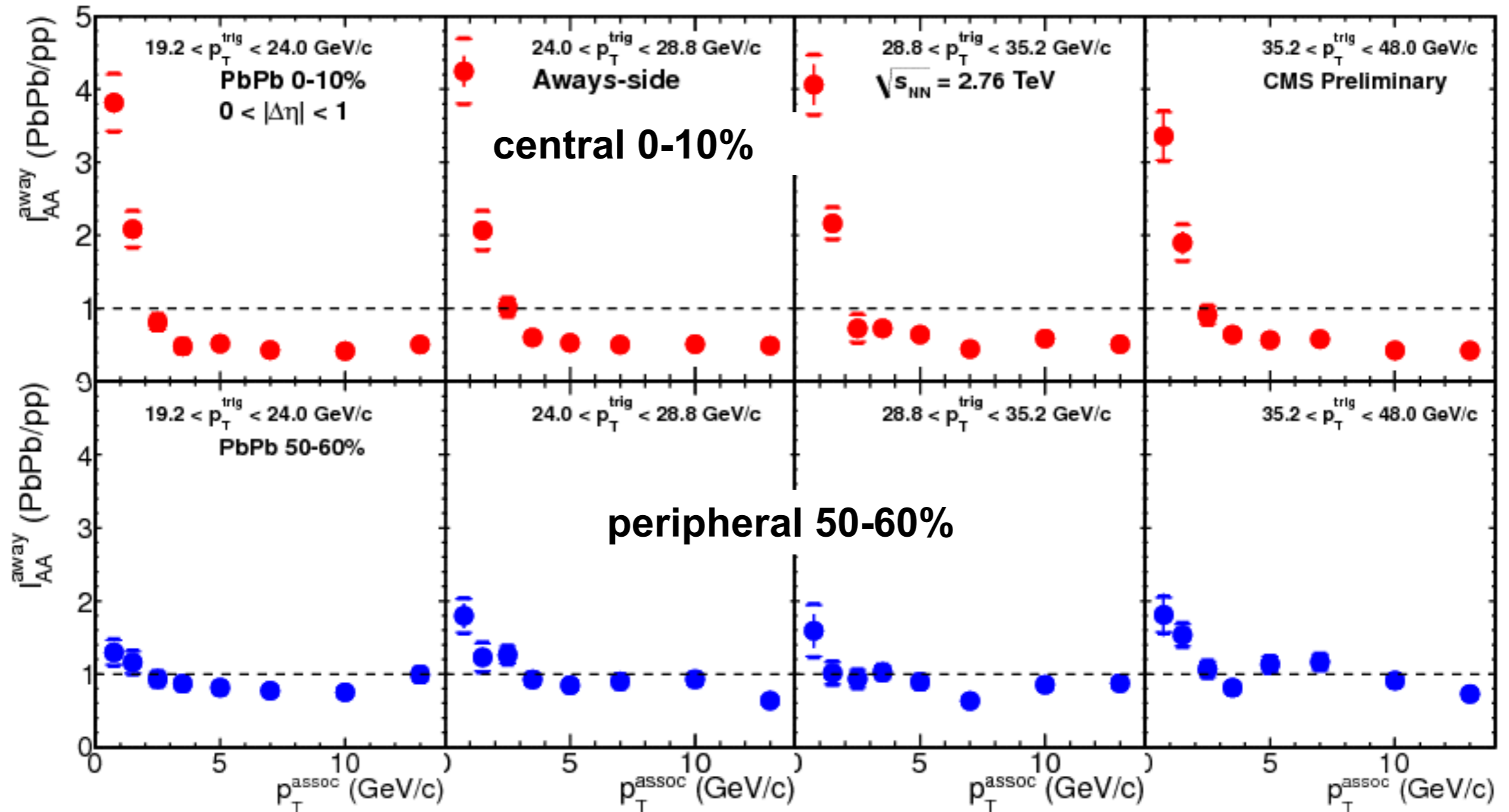
p_T^{trig} (GeV):

19.2 - 24.0 GeV

14.0 - 28.8 GeV

28.8-35.2 GeV

35.2-48.0 GeV



CMS-PAS-HIN-12-010

Transition enhancement \rightarrow suppression @ $p_T \sim 2$ GeV

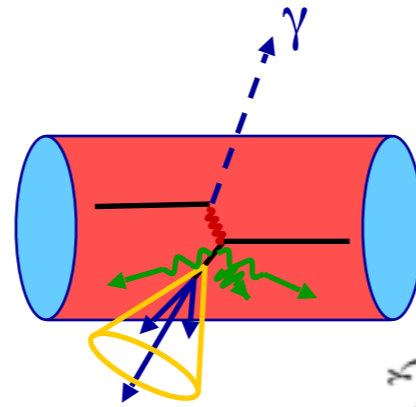
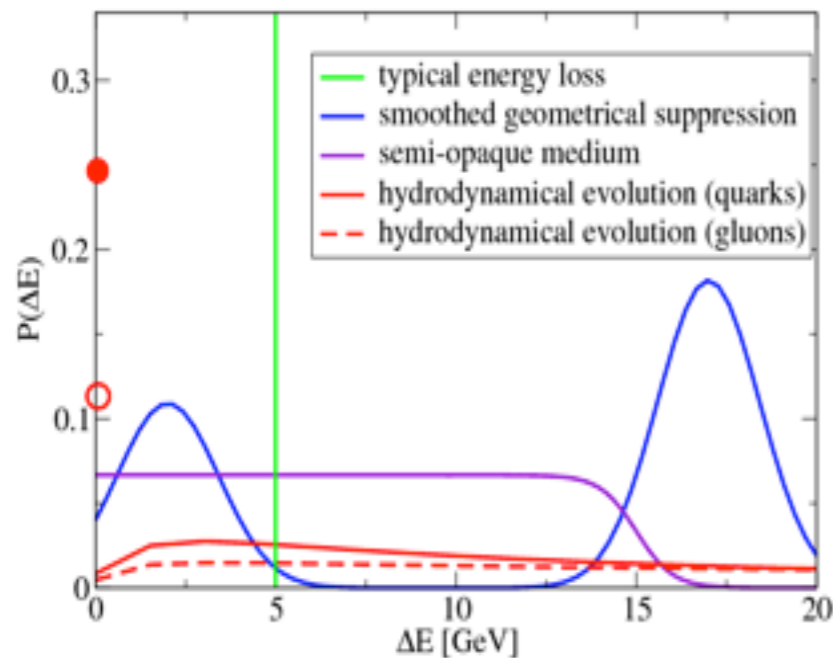
Summary R_{AA} , I_{AA}

- Energy loss is a large effect: fractional loss $\sim 0.2-0.3$, several GeV
- For radiative energy loss: momentum exchange with medium \sim several GeV
- Quantitative relation between medium density and energy loss not (yet) available
- Path length dependence: L^2 strongly favoured by comparing inclusive and recoil data

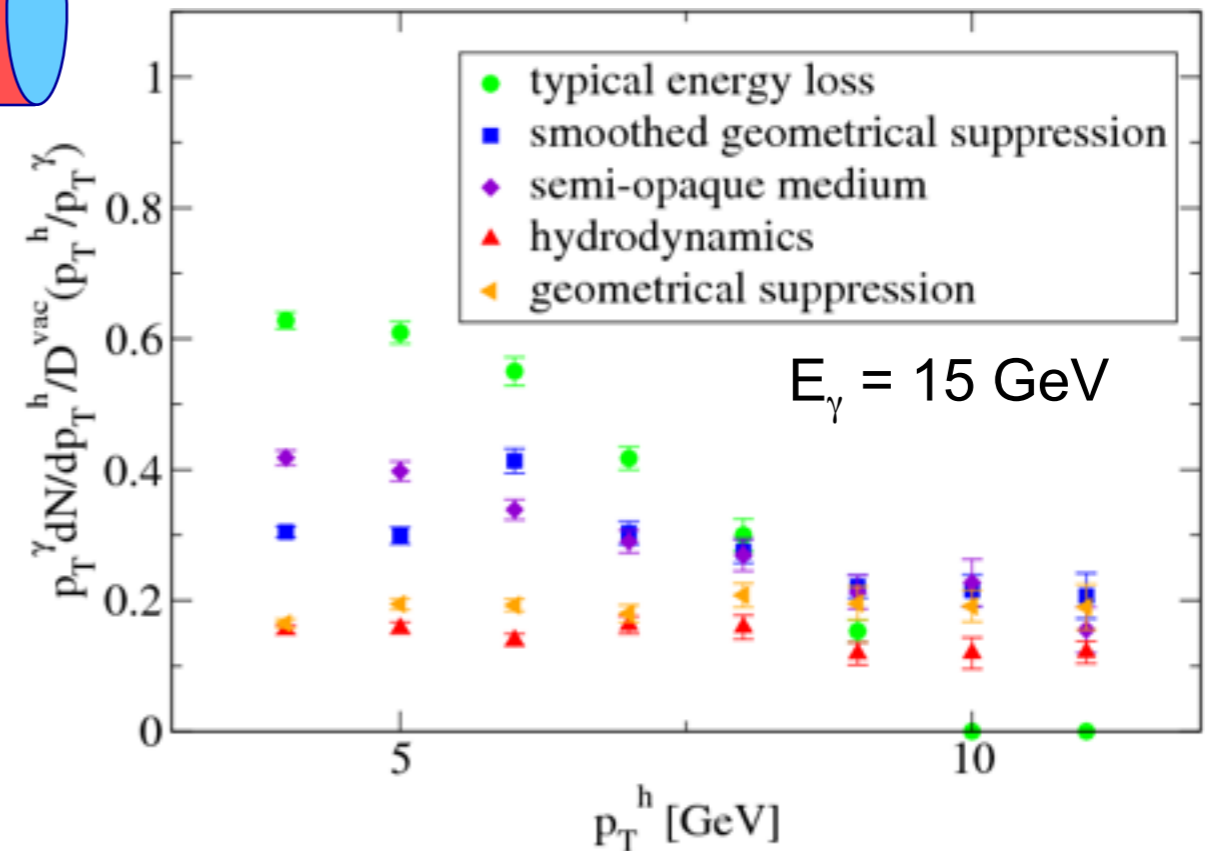
Fixing the parton energy with γ -jet events

T. Renk, PRC74, 034906

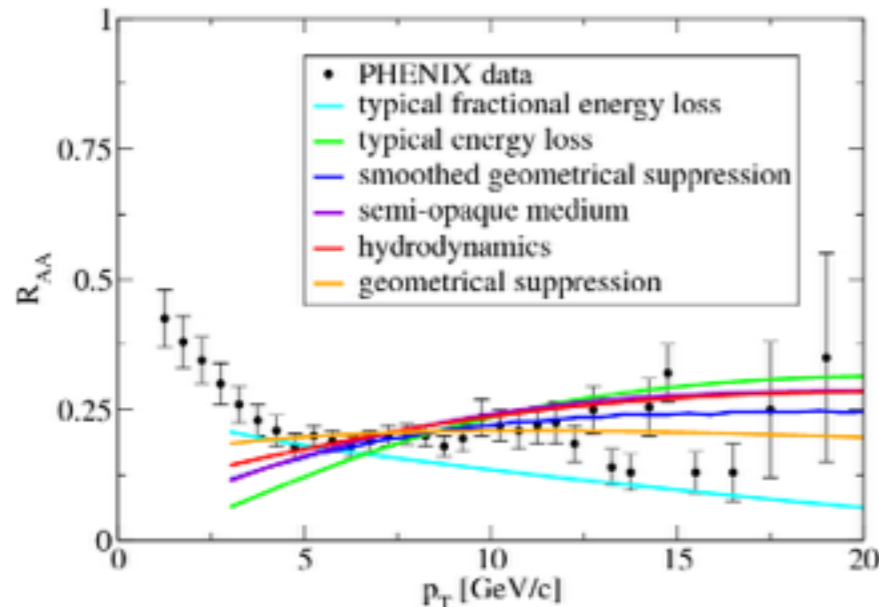
Input energy loss distribution



Away-side spectra in γ -jet



Nuclear modification factor



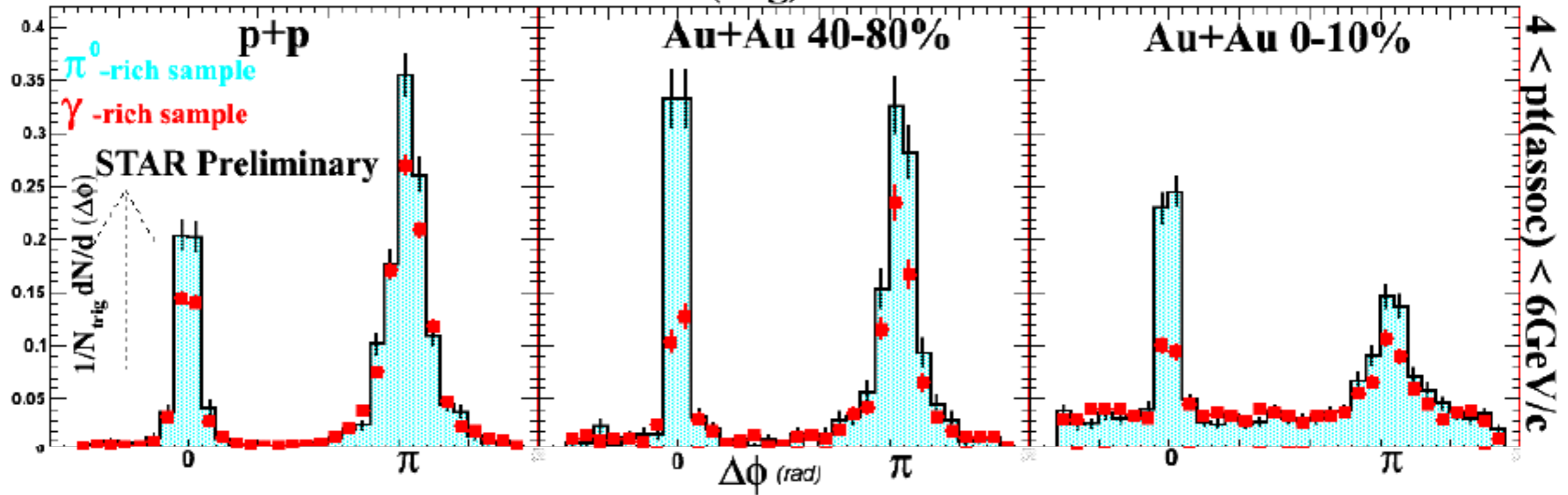
R_{AA} insensitive to $P(\Delta E)$

Away-side spectra for γ -jet are sensitive to $P(\Delta E)$

γ -jet: know jet energy \Rightarrow sensitive to $P(\Delta E)$

γ -jet in Au+Au

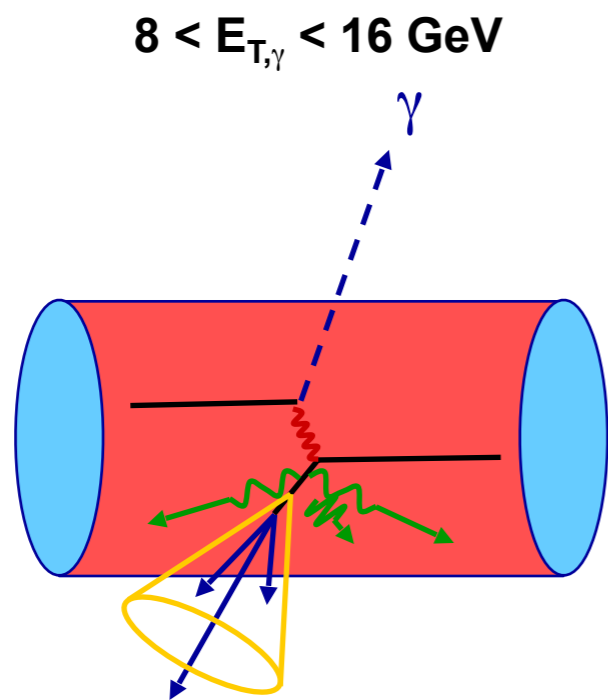
$8 < Et(\text{trig}) < 16\text{GeV}$



Use shower shape in EMCal to form π^0 sample and γ -rich sample

Combinatorial subtraction to obtain direct- γ sample

Direct- γ recoil suppression

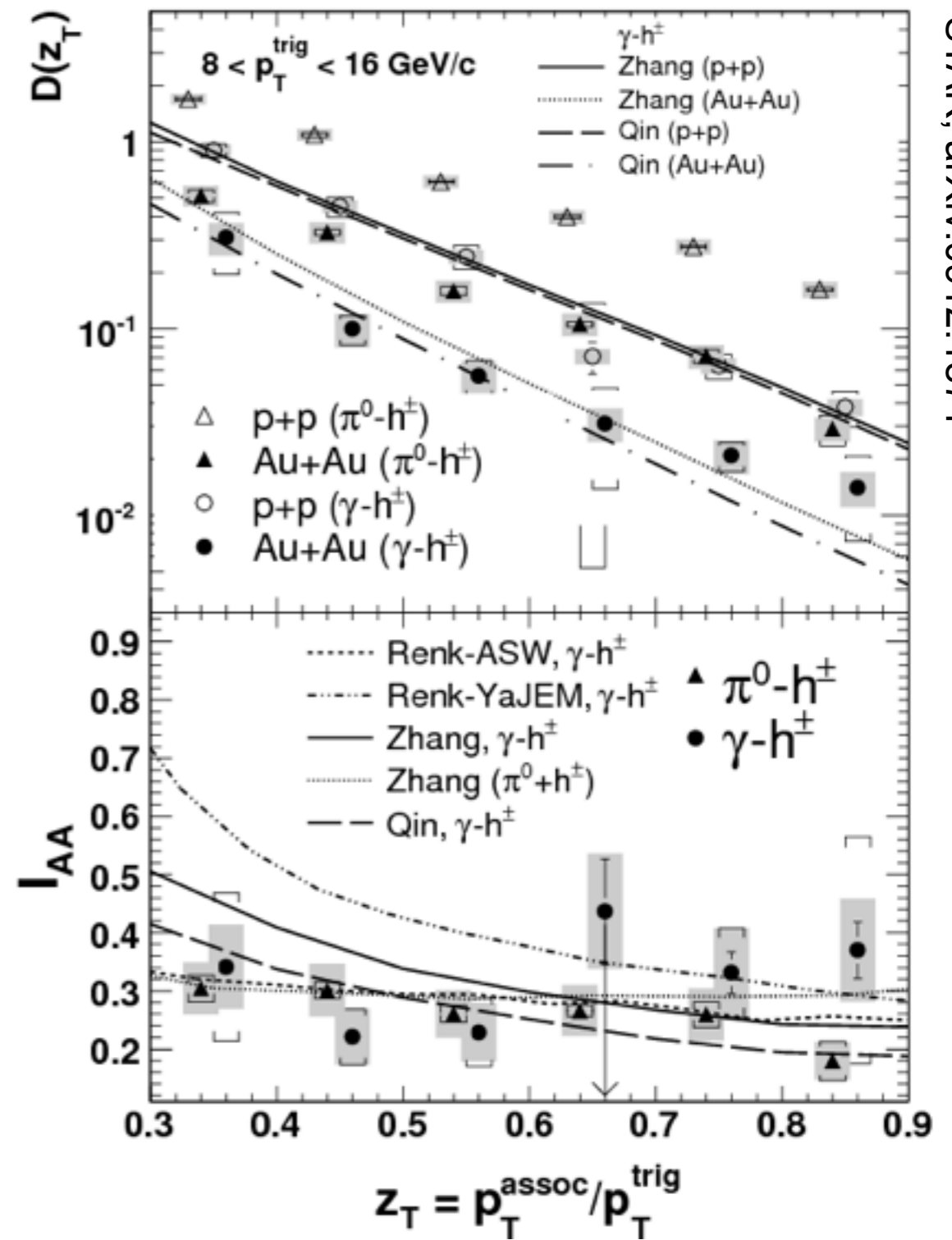


$$I_{AA}(z_T) = \frac{D_{AA}(z_T)}{D_{pp}(z_T)}$$

Large suppression for away-side: factor 3-5

Reasonable agreement with model predictions

NB: gamma $p_T =$ jet p_T still not very large



Extra slides

Questions about energy loss

- What is the dominant mechanism: radiative or elastic?
 - Heavy/light, quark/gluon difference, L^2 vs L dependence
- How important is the LPM effect?
 - L^2 vs L dependence
- Can we use this to learn about the medium?
 - Density of scattering centers?
 - Temperature?
 - Or 'strongly coupled', fields are dominant?

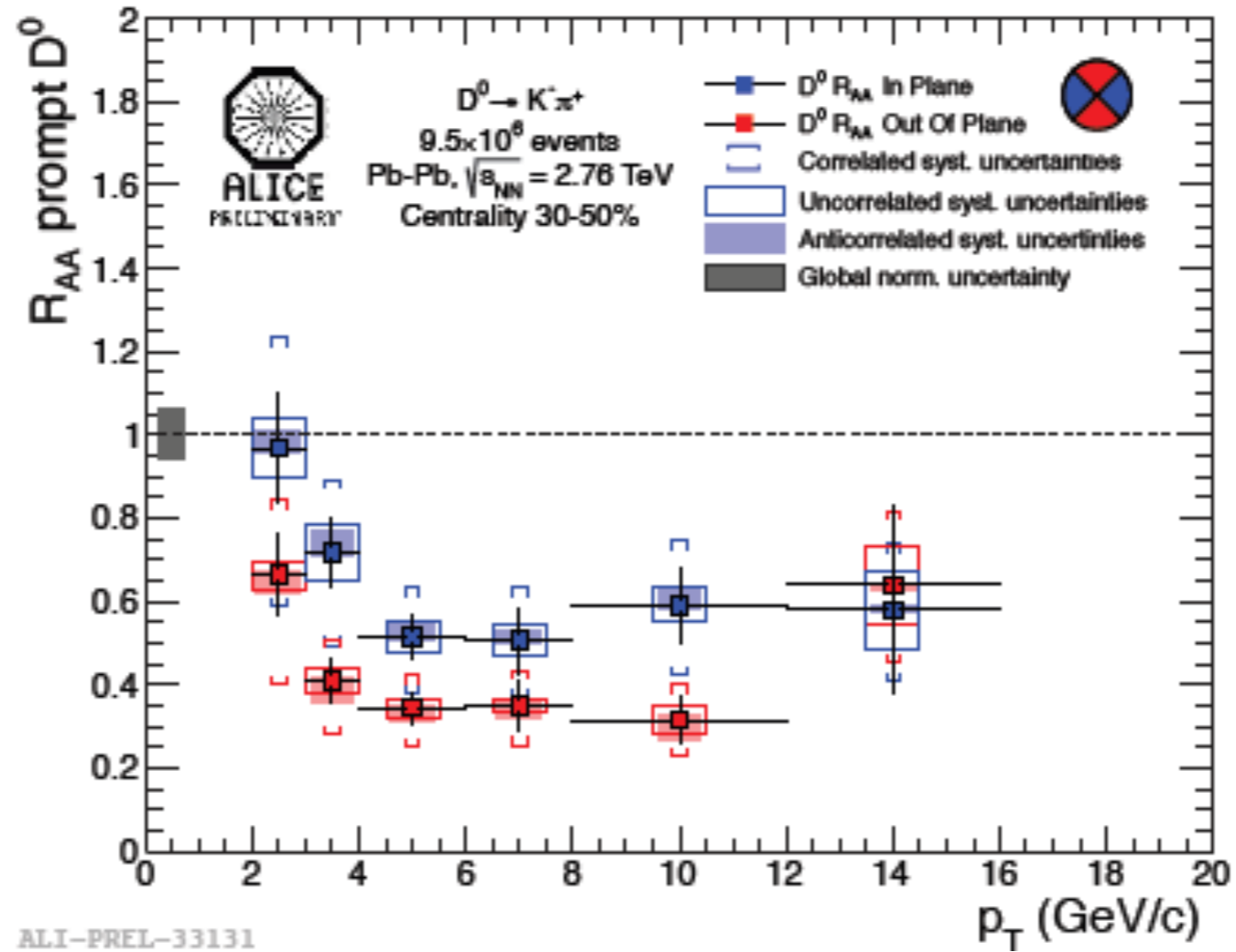
Phenomenological questions:

Large vs small angle radiation

Mean ΔE ?

How many radiations?

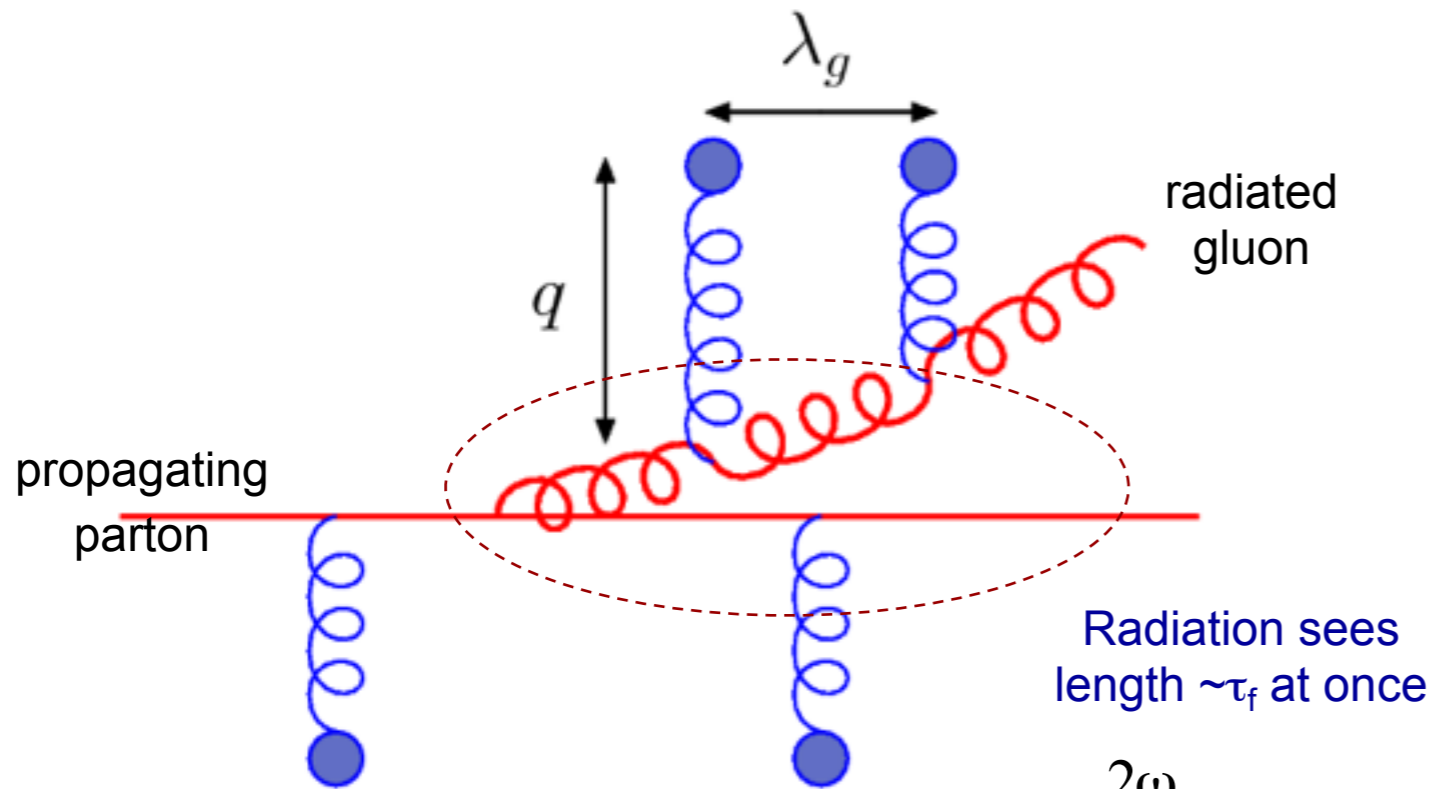
Virtuality evolution/interplay with fragmentation?



In- vs out-of-plane difference also seen for charm
 → Additional constraint for models?

Medium-induced radiation

Landau-Pomeranchuk-Migdal effect
Formation time important



$$\tau_f = \frac{2\omega}{k_T^2}$$

Energy loss depends on density: $\lambda \propto \frac{1}{\rho}$

and nature of scattering centers
(scattering cross section)

Transport coefficient $\hat{q} \equiv \frac{\langle q_{\perp}^2 \rangle}{\lambda}$

Energy loss

$$\Delta E_{med} \sim \alpha_S C_R \hat{q} L^n F(m, E)$$

C_R : color factor (q, g)

\hat{q} : medium density

L : path length

m : parton mass (dead cone eff)

E : parton energy

Path-length dependence L^n

$n=1$: elastic

$n=2$: radiative (LPM regime)

$n=3$: AdS/CFT (strongly coupled)