# Lecture 3: Jets 

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## Jets and parton energy loss

Motivation: understand parton energy loss by tracking the gluon radiation


Qualitatively two scenarios:

1) In-cone radiation: $R_{A A}=1$, change of fragmentation
2) Out-of-cone radiation: $R_{A A}<1$

## Jets at LHC



And a lot of uncorrelated 'soft' background

## Jet reconstruction algorithms

Two categories of jet algorithms:

- Sequential recombination $\mathrm{k}_{\mathrm{T}}$, anti- $\mathrm{k}_{\mathrm{T}}$, Durham
- Define distance measure, e.g. $\mathrm{d}_{\mathrm{ij}}=\min \left(\mathrm{p}_{\mathrm{T},}, \mathrm{p}_{\mathrm{T}}\right)^{*} \mathrm{R}_{\mathrm{ij}}$
- Cluster closest
- Cone
- Draw Cone radius R around starting point
- Iterate until stable $\eta, \varphi_{j e t}=\langle\eta, \varphi\rangle_{\text {particles }}$


## Sum particles inside jet

Different prescriptions exist, most natural: E-scheme, sum 4-vectors

Jet is an object defined by jet algorithm
If parameters are right, may approximate parton

## Collinear and infrared safety



Jet Def $^{n}$
jet 1
jet 2
jet 1


parton shower

$$
\text { Jet } \| \text { Def }^{n}
$$

$$
\text { jet } 1
$$



hadron level
Jet $\mid$ Def ${ }^{n}$
jet 1
jet 2


Jets should not be sensitive to soft effects (hadronisation and E-loss)

- Collinear safe
- Infrared safe


## Collinear safety

Collinear Safe


Infinities cancel

Collinear Unsafe


Infinities do not cancel

Note also: detector effects, such as splitting clusters in calorimeter ( $\pi^{0}$ decay)

## Infrared safety

Soft emission, collinear splitting are both infinite in pert. QCD.
Infinities cancel with loop diagrams if jet-alg IRC safe


IRC unsafe

sum is infinite

Some calculations simply become meaningless

Infrared safety also implies robustness against soft background in heavy ion collisions

## Clustering algorithms $-k_{T}$ algorithm

Majority of QCD branching is soft \& collinear, with following divergences:

$$
\left[d k_{j}\right]\left|M_{g \rightarrow g_{i} E_{j}}^{2}\left(k_{j}\right)\right| \simeq \frac{2 \alpha_{\mathrm{s}} C_{A}}{\pi} \frac{d E_{j}}{\min \left(E_{i}, E_{j}\right)} \frac{d \theta_{i j}}{\theta_{i j}}, \quad\left(E_{j} \ll E_{i}, \theta_{i j} \ll 1\right) .
$$

To invert branching process, take pair with strongest divergence between them - they're the most likely to belong together.

This is basis of $\mathrm{k}_{\mathrm{t}} /$ Durham algorithm $\left(e^{+} e^{-}\right)$:

1. Calculate (or update) distances between all particles $i$ and $j$ :

$$
y_{i j}=\frac{2 \min \left(E_{i}^{2}, E_{j}^{2}\right)\left(1-\cos \theta_{i j}\right)}{Q^{2}}
$$

2. Find smallest of $y_{i j}$

NB: relative $k_{t}$ between particles

- If $>y_{\text {cut }}$, stop clustering
- Otherwise recombine $i$ and $j$, and repeat from step 1

Catani, Dokshitzer, Olsson, Turnock \& Webber '91

## $\mathrm{k}_{\mathrm{T}}$ algorithm

Various distance measures have been used, e.g. Jade, Durham, Cambridge/Aachen

Current standard choice:

- Calculate
- For every particle $i$ : distance to beam $\quad d_{i B}=p_{t, i}^{2}$
- For every pair $i, j$ : distance $\quad d_{i j}=\min \left(p_{t, i}^{2}, p_{t, j}^{2}\right) \frac{R_{i j}^{2}}{R^{2}}$
- Find minimal d
- If $d_{i B}, i$ is a jet
- If $d_{i j}$, combine $i$ and $j$
- Repeat until only jets


## $\mathrm{k}_{\mathrm{T}}$ algorithm demo



## $\mathrm{k}_{\mathrm{T}}$ algorithm properties

- Everything ends up in jets
- $\mathrm{k}_{\mathrm{T}}$-jets irregular shape
- Measure area with 'ghost particles'
- $\mathrm{k}_{\mathrm{T}}$-algo starts with soft stuff
- 'background' clusters first, affects jet
- Infrared and collinear safe
- Naïve implementation slow ( $\mathrm{N}^{3}$ ). Not necessary $\rightarrow$ Fastjet

Alternative: anti- $\mathrm{K}_{\mathrm{T}} \quad d_{i j}=\min \left(\frac{1}{p_{t, i}^{2}}, \frac{1}{p_{t, j}^{2}}\right) \frac{R_{i j}^{2}}{R^{2}} \quad d_{i B}=\frac{1}{p_{t, i}^{2}}$
Cambridge-Aachen: $\quad d_{i j}=\frac{R_{i j}^{2}}{R^{2}}$

## Cone algorithm

- Jets defined as cone
- Iterate until stable:
$(\eta, \varphi)_{\text {Cone }}=\langle\eta, \varphi\rangle_{\text {particles in cone }}$
- Starting points for cones, seeds, e.g. highest $p_{T}$ particles
- Split-merge prescription for overlapping cones


## Cone algorithm demo



## Seedless cone



1D: slide cone over particles and search for stable cone
Key observation: content of cone only changes when the cone boundary touches a particle

Extension to 2D ( $\eta, \varphi$ )


Limiting cases occur when two particles are on the edge of the cone

## Jet algorithm examples

simulated $p+p$ event




Measuring the jet spectrum

## PbPb jet background

Jet finding illustration


Many 'background jets'

Background density vs multiplicity


Background contributes up to $\sim 180 \mathrm{GeV}$ per unit area
Subtract background: $\quad p_{T, j e t}^{s u b}=p_{T, j e t}^{r a w}-\rho A$
Statistical fluctuations remain after subtraction

## PbPb jet background




Main challenge: large fluctuations of uncorrelated background energy
Size of fluctuations depends on $\mathrm{p}_{\mathrm{T}}$ cut, cone radius

## Background jets

Raw jet spectrum
Event-by-event background subtracted

Low $\mathrm{p}_{\mathrm{T}}$ : ‘combinatorial jets’

- Can be suppressed by requiring leading track
- However: no strict distinction at low $\mathrm{p}_{\mathrm{T}}$ possible

Next step: Correct for background fluctuations and detector effects by unfolding/deconvolution


## Removing the combinatorial jets

Raw jet spectrum


Fully corrected jet spectrum


Correct spectrum and remove combinatorial jets by unfolding
Results agree with biased jets: reliably recovers all jets and removed bkg

## PbPb jet spectra

Charged jets, $R=0.3$

$\mathrm{R}_{\mathrm{CP}}$, charged jets, $R=0.3$


Jet reconstruction does not 'recover' much of the radiated energy

Jet spectrum in $\mathrm{Pb}+\mathrm{Pb}$ : charged particle jets Two cone radii, 4 centralities

## $\mathrm{Pb}+\mathrm{Pb}$ jet $\mathrm{R}_{\mathrm{AA}}$

Jet $\mathrm{R}_{\mathrm{AA}}$ measured by ATLAS, ALICE, CMS

Good agreement between experiments

Despite different methods:
ATLAS+CMS: hadron+EM jets
ALICE: charged track jets

$R_{\text {AA }}<1$ : not all produced jets are seen; out-of-cone radiation and/or 'absorption'
For jet energies up to $\sim 250 \mathrm{GeV}$; energy loss is a very large effect

## Comparing hadrons and jets



Suppression of hadron (leading fragment) and jet yield similar Is this 'natural'? No (visible) effect of in-cone radiation?

## Comparison to JEWEL energy loss MC





## Generic expectations from energy loss



- Longitudinal modification:
- out-of-cone $\Rightarrow$ energy lost, suppression of yield, di-jet energy imbalance
- in-cone $\Rightarrow$ softening of fragmentation
- Transverse modification
- out-of-cone $\Rightarrow$ increase acoplanarity $\mathrm{k}_{\mathrm{T}}$
- in-cone $\Rightarrow$ broadening of jet-profile


## Jet broadening: transverse fragment distributions


(89) Jet broadening: radiation at large angles

## Jet broadening: R dependence of $\mathrm{R}_{\mathrm{AA}}$



Jet $\mathrm{R}_{\mathrm{AA}}$ increases with R (but slowly)

## Jet broadening: $R$ dependence



Larger jet cone: 'catch' more radiation $\rightarrow$ Jet broadening

Ratio of spectra with different $R$


However, $R=0.5$ still has $R_{A A}<1$

- Hard to see/measure the radiated energy


## Comparing to JEWEL energy loss MC




JEWEL gets the right suppression for $R=0.2$,
but not the increase with $R$
May be treatment of recoil patrons

## Recap

- So, jet $R_{A A}$ is not close to 1
- Large out-of-cone radiation
- Also means: measured jet energy $=$ initial parton energy!

Next sections: more jet measurements

## Why so many?

- Different observables sensitive to different aspects of energy loss
- Finding a balance between what you want to know and what you can measure


## Generic expectations from energy loss



- Longitudinal modification:
- out-of-cone $\Rightarrow$ energy lost, suppression of yield, di-jet energy imbalance
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- Transverse modification
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## Jet fragment distributions

## PbPb measurement



NB: $z$ is wrt observed $E_{\text {jet }} \neq$ initial $E_{\text {parton }}$

Ratio to pp

M. Rybar@QM2012

1
Low $p_{T}$ enhancement:
soft radiation
Intermediate z:
depletion: E-loss

## Jet fragment distributions



Low $p_{T}$ enhancement: soft radiation

Intermediate $z, p_{\mathrm{T}}$ :
depletion: E-loss

## Azimuthal modulation of R $\mathrm{RAA}^{\text {'jet flow’ }}$

## Path length dependence: elliptic flow of Jets

ATLAS, arXiv:1306.6469


Significant azimuthal modulation of jet yield
jet $\mathrm{v}_{2} \sim 0.03$ at high $\mathrm{p}_{\mathrm{T}}$

## Comparing to JEWEL energy loss MC

5-10\% centrality


40-50\% centrality


Good agreement between JEWEL and jet $\mathrm{v}_{2}$ results Geometry: Glauber overlap with Bjorken expansion

Di-jet imbalance measurements

## Di-jet asymmetry



Observation: some events have two jets with different energy (However: one swallow does not make spring)

## Jet energy asymmetry

Centrality



Jet-energy asymmetry $A_{J}=\frac{E_{2}-E_{1}}{E_{2}+E_{1}}$


Large asymmetry seen for central events

Suggests large energy loss: many GeV
~ compatible with expectations from RHIC+theory
However:

- Only measures reconstructed di-jets (don't see lost jets)
- Not corrected for fluctuations from detector+background
- Both jets are interacting - Not a simple observable


## Energy dependence of asymmetry


(Relative) asymmetry decreases with energy
However: difference pp vs PbPb remains - energy loss finite at large E

## Energy dependence of $\mathrm{A}_{\lrcorner}$



Asymmetry decreases for larger jet energy Similar effect in pp (Pythia): difference stays ~constant

## Studying the imbalance

In Cone $\mathrm{R}<0.8 \quad$ Out of Cone $\mathrm{R}>0.8$


## $\gamma$-jet imbalance

Centrality
CMS, arXiv:1502.0206

$\gamma$-jet asymmetry $\quad x_{J_{\gamma}}=\frac{p_{T}^{\text {jet }}}{p_{T}^{\gamma}}$

Advantage: $\gamma$ is a parton: know parton kinematics Disadvantage: low rate (+background $\pi^{0} \rightarrow \gamma \gamma$ )


Translates into: low $\mathrm{p}_{\mathrm{T}, r}$ cut $>60 \mathrm{GeV}$
Dominant contibution: $q g \rightarrow q \gamma$

## Hadron-recoil jet measurements

## Hadron trigger vs jet trigger

Hadron trigger: strong "surface bias" maximizes recoil path length
(T.Renk, private com.)

Full jet trigger: no geom. bias
partially cancelled by bkg fluctuations

Centrality and reaction plane biases:


- Finite, but only weak trigger $p_{T}$ dependence for high $p_{T}$ trig


## Hadron-triggered recoil jet distributions

G. de Barros et al., arXiv:1208.1518


## Background subtraction: $\Delta_{\text {recoil }}$

Remove background by subtracting spectrum with lower $p_{T}$ trig:
$\Delta_{\text {recoil }}=[(20-50)-(15-20)]$

Reference spectrum (15-20) scaled by $\sim 0.96$ to account for conservation of jet density

$\Delta_{\text {recoil }}$ measures the change of the recoil spectrum with $p_{T}$ trig
Unfolding correction for background fluctuations and detector response

## Ratio of Recoil Jet Yield $\Delta I_{A A}$ PYTHIA

pp reference: PYTHIA (Perugia 2010)
$\mathrm{R}=0.4$
Constituents:
$p_{\text {T }}$ const $>0.15 \mathrm{GeV} / \mathrm{c}$
no additional cuts
(fragmentation bias) on recoil jets


Recoil jet yield $\Delta \mathrm{I}_{\mathrm{AA}}{ }^{\text {PYTHA }} \approx 0.75$, approx. constant with jet $p_{\mathrm{T}}$

## Recoil Jet $\Delta I_{A A}$ PYTHIA: R dependence

$\mathrm{R}=0.4$


## $\mathrm{R}=0.2$



Similar $\Delta \mathrm{I}_{\mathrm{AA}} \mathrm{PYTHIA}$ for $\mathrm{R}=0.2$ and $\mathrm{R}=0.4$
No visible broadening within $\mathrm{R}=0.4$
(within exp uncertainties)

## Hadrons vs jets II: recoil

Hadrons


Hadron $I_{A A}=0.5-0.6$
In approx. agreement with models; elastic E-loss would give larger I ${ }_{\text {AA }}$

Jets


Jet $\mathrm{I}_{\mathrm{AA}}=0.7-0.8$ Jet $I_{A A}>$ hadron $I_{A A}$ Not unreasonable

NB/caveat: very different momentum scales !

## Model comparison $\mathrm{I}_{\mathrm{AA}}$

JEWEL: Zapp et al., EPJ C69, 617


JEWEL correctly describes inclusive jet $\mathrm{R}_{\mathrm{AA}}$


Predicts $\Delta \mathrm{I}_{\mathrm{AA}} \sim 0.4$, below measured

## A consistent view of jet quenching

G. Roland@QM2012






## A consistent view of jet quenching



Consistent message from charged hadron $\mathrm{R}_{\mathrm{AA}}$, inclusive jet $R_{A A}$ and fragmentation functions!

## Summary

- Jets: a new tool for parton energy loss measurements
- Large out-of-cone radiation ( $\mathrm{R}=0.2-0.4$ )
- Energy asymmetry
- $\mathrm{R}_{\mathrm{AA}}<1$
- $\mathrm{I}_{\mathrm{AA}}<1$
- Radial shapes
- Remaining jet is pp-like:
- Fragment distribution at large z same as pp
- $\mathrm{R}_{\mathrm{AA}}$ similar for jets and hadrons
- Most of the radiation is at low $p_{T}$
- Scale set by medium temperature?
- Direct photons
- $\gamma$-jet allows to measure initial parton energy; jet asymmetry seen

JEWEL energy loss MC agrees with many of the observed effects Does this constrain the energy loss mechanism(s)?
Need to test for kinematic effects/alternative explanations (e.g. YaJEM)

## Extra slides

## $\gamma$, hadrons, jets compared

$\gamma$, hadrons


Jets


Suppression of hadron (leading fragment) and jet yield similar Is this 'natural'? No effect of in-cone radiation?

## Model comparison



At least one model calculation reproduces the observed suppression $\Rightarrow$ Understand mechanism for out-of-cone radiation?

