

ex. 5.3

Consider again $X^2 - A = 0$

and the Denman-Beavers method (1976):

$$\left\{ \begin{array}{l} X_{k+1} = \frac{1}{2} (X_k + Y_k^{-1}) \\ Y_{k+1} = \frac{1}{2} (Y_k + X_k^{-1}) \end{array} \right\} k = 0, 1, 2, \dots$$

with $\begin{cases} X_0 = A \\ Y_0 = I \end{cases}$.

a) write a Matlab file DB.m that performs the Denman-Beavers iterations.

b) test your code for the matrix:

$$A = \begin{pmatrix} 10 & 7 & 8 & 7 \\ 7 & 5 & 6 & 5 \\ 8 & 6 & 10 & 9 \\ 7 & 5 & 9 & 10 \end{pmatrix}$$

Compare with matrix-Newton*.

* Use 20 iteration steps.